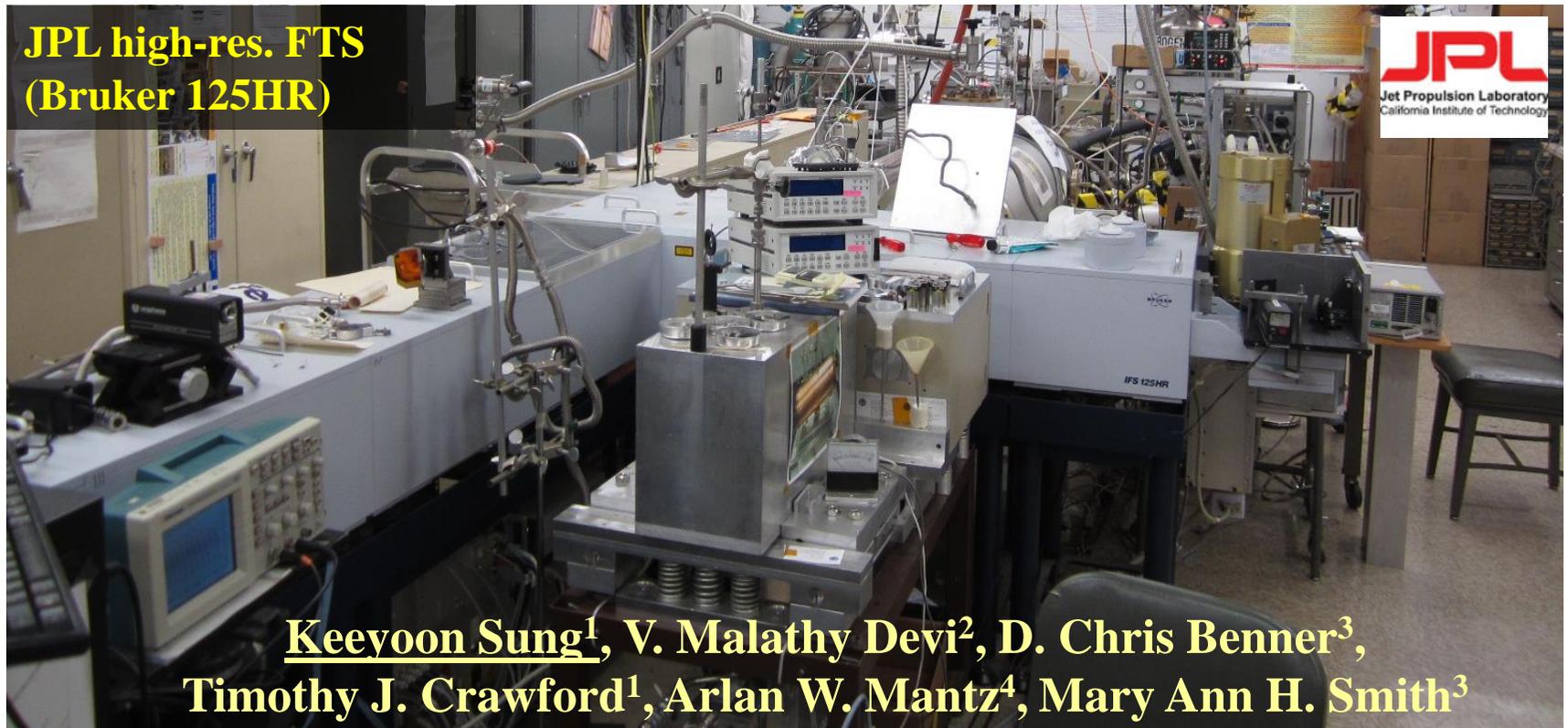




Progress in the measurement on temperature-dependence of H₂-broadening of cold and hot CH₄



**JPL high-res. FTS
(Bruker 125HR)**



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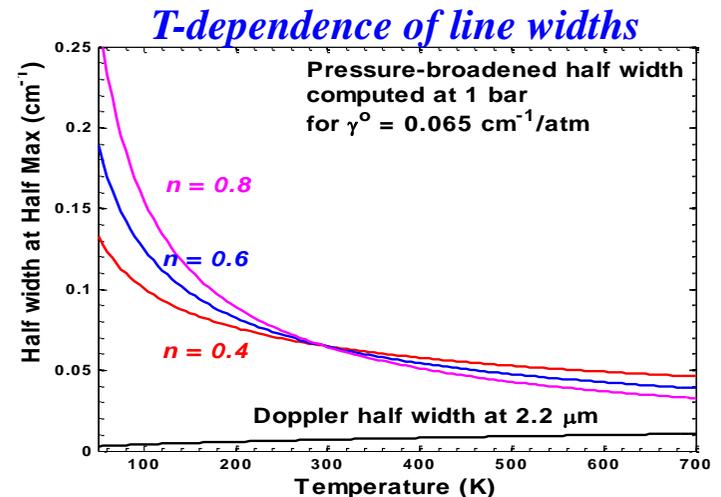
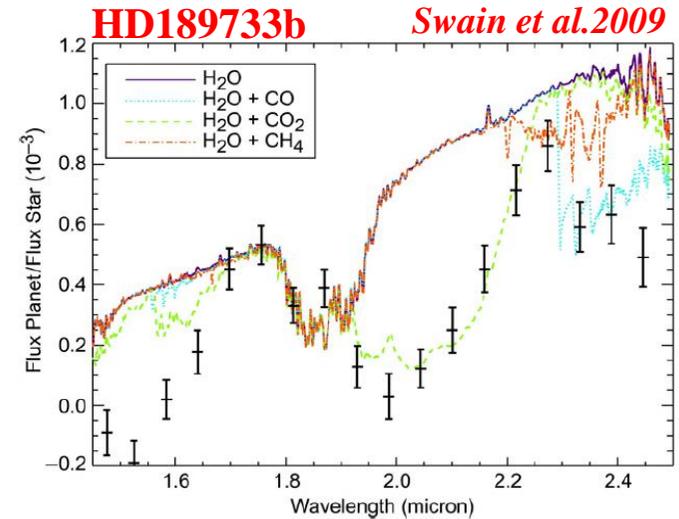
❖ Significance of H₂ pressure broadening

- H₂ : dominant atmospheric constituent in the giant gaseous bodies
- Cold Jovian planets, Hot Jupiter exoplanets, low mass brown dwarfs
- Key spectroscopic parameter in atmospheric opacity calculations
- Characterization of exoplanets

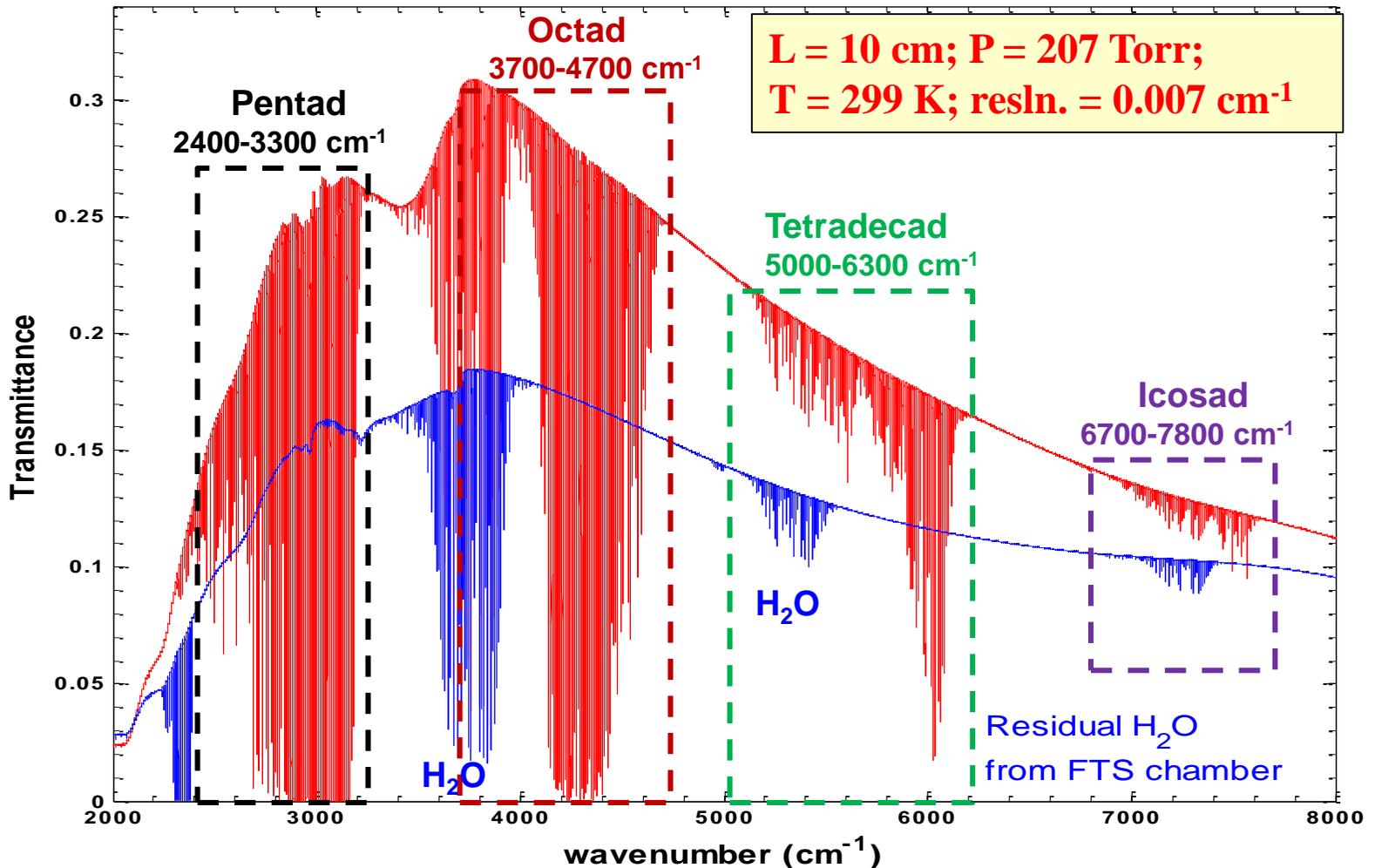
❖ Measurements of line shape parameters

- Broad temperature range: 80 – 400 K
- Study of their temperature dependence
- Check the validity of the power law for width
- Provide constraints for theoretical model for line widths
- T-dep. up to ~2000 K will be covered by the model calculations

❖ In support of various NASA missions TEXES, SOFIA, HST, JWST, etc.



Overview of Infrared CH₄ spectrum





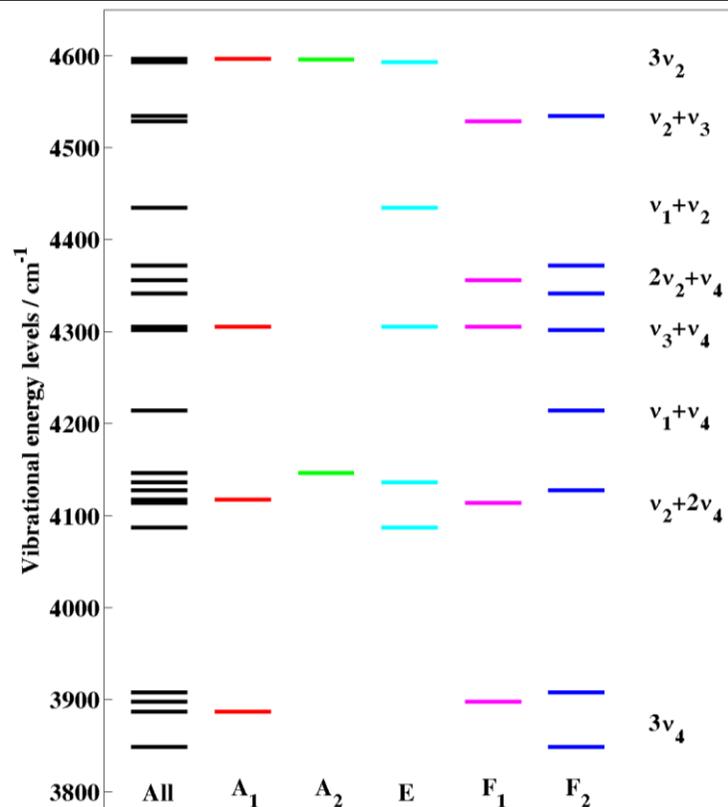
□ Vibrational States

Polyads, P_n and name		Range (cm ⁻¹)	# vib levels	# sub-levels
P_0	GS	< 200	1	1
P_1	Dyad	1200 – 1700	2	2
P_2	Pentad	2400 – 3200	5	9
P_3	Octad	3700 – 4700	8	24
P_4	Tetradecad	5000 – 6200	14	60
P_5	Icosad	6500 – 7700	20	134

□ Some characteristics

- Eight different vibrational bands
- Most have multiple components of vib. sym.species. (i.e., A , E , F)
- Only F_2 is inherently IR active.
- All others borrow intensities through interactions.
- A tends to borrow less while F_1 and E borrows more.

□ Octad vibrational states for ¹³CH₄



Brown et al. (MJ14) ISMS 2015

High-Reso

High-Resolution Infrared Spectroscopy Lab (JPL)

copy Lab (JPL)



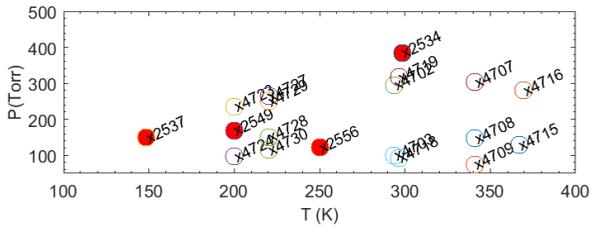
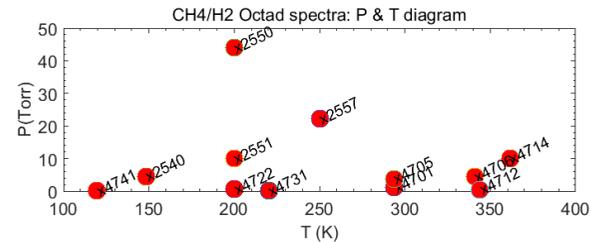
Our gas absorption chambers

Cells	path lengths (in meters)	Temperatures	Wavelength
1	0.02, 0.06, 0.15, 0.20, 0.25 (fixed path)	T ~ 296 K (room)	2 - 50 μm
2	6.6 - 32.5 multipass	T ~ 296 K (room)	0.7 - 50 μm
3	20 - 180 multipass	T ~ 296 K (room)	0.7 - 1.6 μm
4	3.9 m + (0.76 or 0.35 m) <i>no color</i> (fixed)	T ~ 296 K (room)	IR and MW
5	0.204 (fixed) gas absorption chamber	80 < T < 297 K	1.6 - 15 μm
6	21 - Herriott Cells (fixed)	296 < T < 250 K	1.6 - 8 μm
7	4 - 52 multipass	80 < T < 296 K	15 - 500 μm
8	0.8 (fixed) <i>no color</i> (fixed)	80 < T < 297 K	0.7 - 18 μm
9	Extra vacuum chamber using Emission port	30 < T < 250 K 230 - 296 K (420 K)	0.7 - 15 μm
10	Heatable multipass 2.2 - 22 m (to be installed)	296 < T < 420 K	0.7 - 8 μm

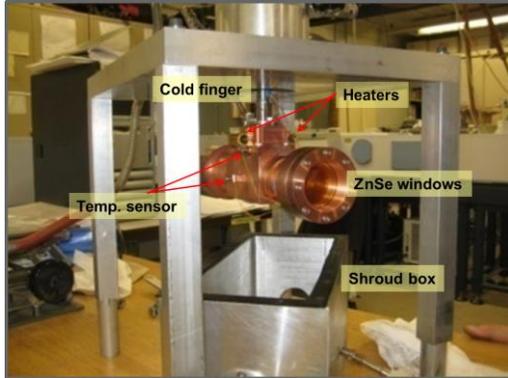
Experimental conditions for CH₄+H₂ spectra

Gas sample	¹² CH ₄
Spectral region	4100 - 4750 cm ⁻¹
Resolution(B)	0.0044 cm ⁻¹
Total pressures	130 - 300 Torr
Path lengths	20.4 cm - 22 m
mixing ratios	0.002 - 1.000
Temperatures	80 - 370 K

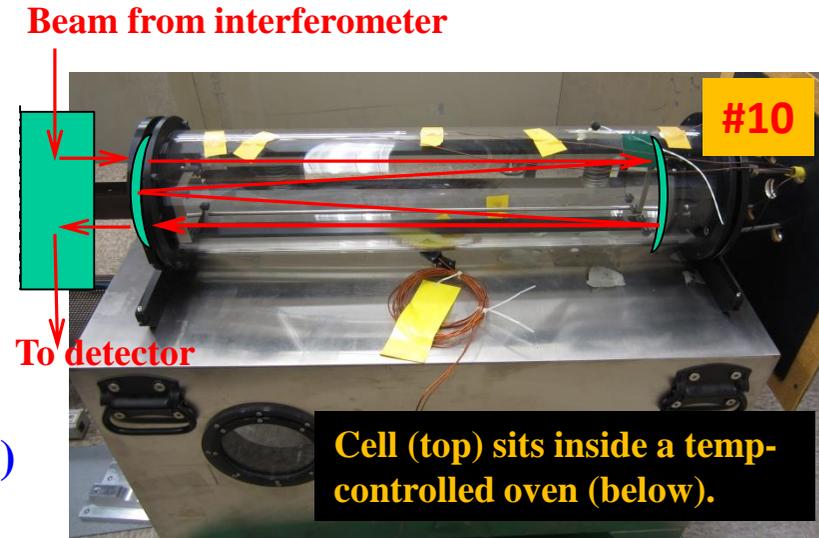
P&T distribution of the observed spectra



(1) Short cold cell (20.38 cm)



(3) White-type hot cell (2.2 – 22 m)



(2) Cryogenic Herriott cell (20.94 m, fixed)



☐ Three gas absorption cells

- Variable pathlength, 0.2038 cm - 22 m
- Temperature, 80 – 500 K
- Spectral coverage, 0.7 – 8 μm
- Transfer optics designed & developed
 - Beam intercept and guiding
 - Heat-insulated stainless steel tubing



Three bands observed in this work



CH₄+H₂ mixture spectra

4000 – 4700 cm⁻¹.

200 – 370 K

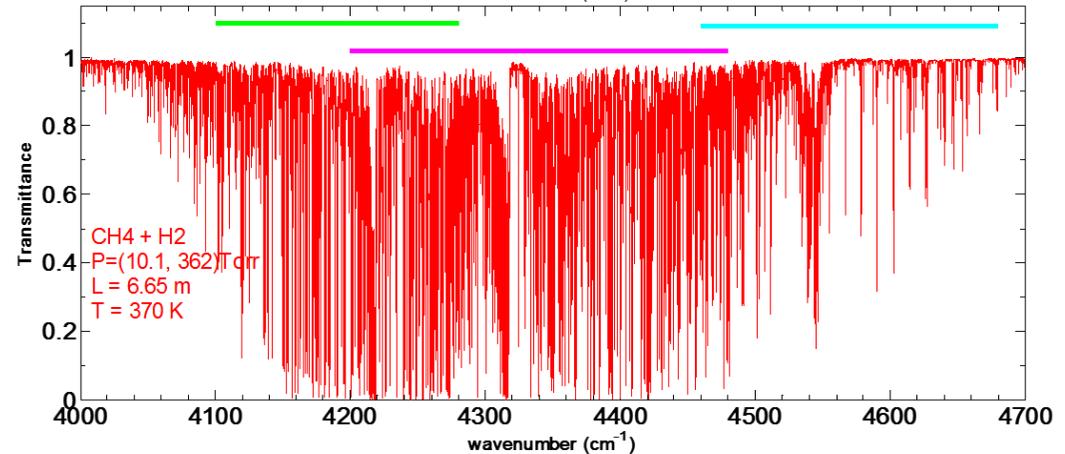
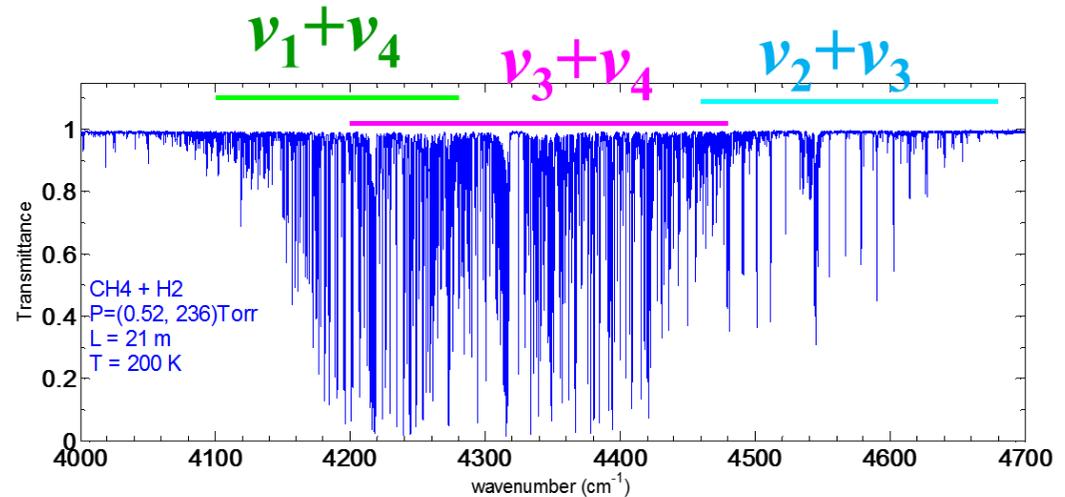
Three bands:

$\nu_1+\nu_4$ (*strong*),

$\nu_3+\nu_4$ (*strong*),

$\nu_2+\nu_3$ (*weak*)

Atmospheric H₂O & CO₂
overlap with $\nu_1+\nu_4$.



❖ $^{12}\text{CH}_4$ in the Octad

- Positions and intensities
- Broadening (Self, Air, O_2 , N_2) [*Pine, 1992*]
- Model calculations of the widths

❖ H_2 -broadening of $^{12}\text{CH}_4$

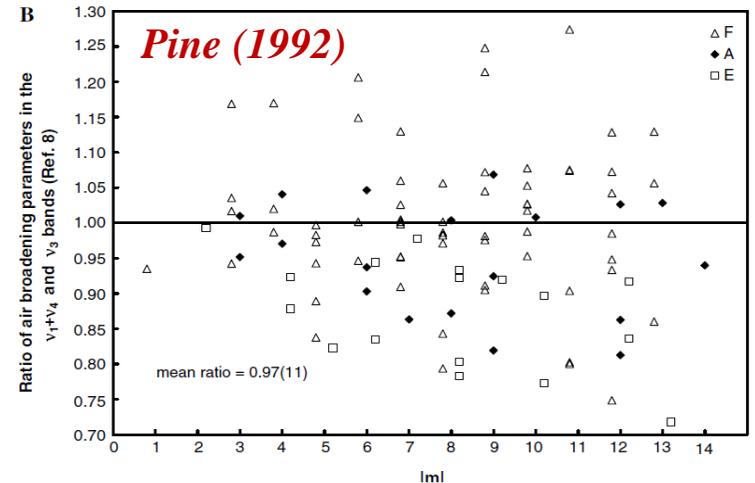
- First measurements on $\nu_1 + \nu_4$ [*Margolis (1993)*]
- Calculations [*R. Gamache, T. Garbard, H. Tran*]
- Compilations [*HITRAN 2016*]

❖ Various dependences

- Vibrational dependence – [*Margolis, 1993*]
- Temperature dependence
- Symmetry dependence

❖ Line mixing

- Measurements and calculations





Some basic equations for spectrum descriptions



□ **Transmittance:** $\tau(\nu; \nu_0) = \exp[-k(\nu) \cdot N \cdot \xi \cdot l]$

□ **Line shape profile (Voigt):** $f(\nu - \nu_0) = V(x, y) = \frac{1}{\gamma_D} \sqrt{\frac{\ln 2}{\pi}} \frac{y}{\pi} \int_{-\infty}^{\infty} \frac{e^{-t^2}}{y^2 + (x-t)^2} dt$

$$x = \frac{[\sqrt{\ln 2} \cdot |\nu - \nu_0|]}{\gamma_D}; \quad y = \sqrt{\ln 2} \cdot \gamma_L / \gamma_D;$$

□ **Temperature dependence of the line shape parameters:**

$$\gamma_{p,T} = P \times \gamma_{p_0,T_0}^o \left(\frac{T_0}{T} \right)^n \quad \delta_{p,T} = P \times \left[\delta_{p_0,T_0}^o + \delta' \times (T - T_0) \right]$$

□ **Voigt profile, represented by Fadeeva function,**

$$W(z) = \frac{i}{\pi} \int_{-\infty}^{\infty} \frac{e^{-t^2}}{z-t} dt \quad K(x, y) = \frac{\sqrt{\ln 2}}{\lambda_D \sqrt{\pi}} \cdot \text{Re}[W(z)]$$

□ **Speed-dependent narrowing profile**

$$K_s(x, y, s, H) = \frac{2}{\pi} \int_{-\infty}^{\infty} \nu \cdot e^{-\nu^2} \cdot \tan^{-1} \left(\frac{x + \nu}{y(\tilde{\nu})[1 + s(\nu^2 - 1.5)] + H} \right) d\nu$$

□ Full Line mixing

$$I(\nu) = (1/\pi) \cdot \text{Im}[\mathbf{X}^T \mathbf{G}^{-1} \boldsymbol{\rho} \mathbf{X}]$$

$$\mathbf{G}(\nu) = (\nu - \nu_0) - i\mathbf{W},$$

$$W_{ii} = \gamma_{Li} + i\delta_i$$

$$X_i = \sqrt{[(S_i/\rho_i)]}$$

$$\rho_i = (2J+1) \exp(-C_2 E''_i/T)$$

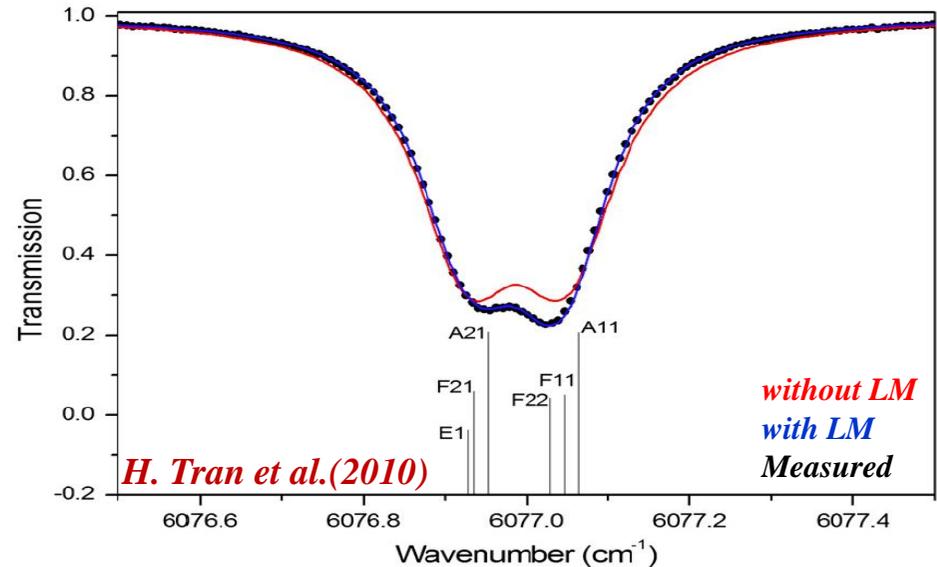
$$C_2 = 2^{\text{nd}} \text{ boltzman constant}$$

□ Labfit to solve for W_{ik} , the off-dia. Relaxation Matrix

(Assumed linear P & exponential T dependences)

$$W_{ik} = p \sum_j^{N_{\text{gases}}} \frac{g_k}{g_i} W_{ikj}^0 \chi_j \left(\frac{T_0}{T} \right)^{m_j}$$

Effect of line mixing: $\text{CH}_4(2\nu_3) \text{ R}(6)$



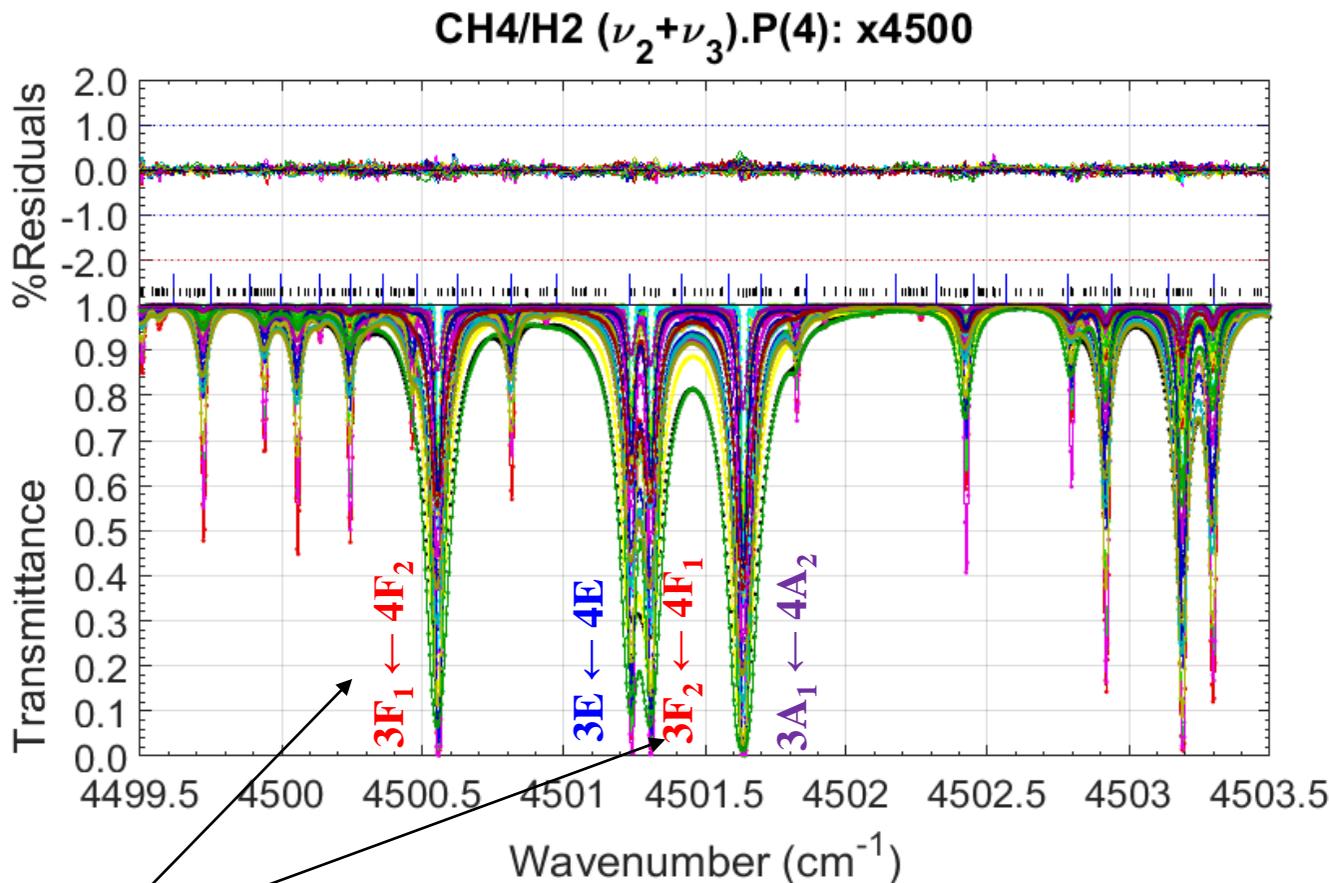
❖ Some statistics

- 29 spectra
- 8 at RT
- 5 at 200 K
- 5 at 220 K
- 2 at 250 K
- 9 at T = 340-370K

➤ 288 transitions

- positions,
- intensities,
- widths & T-dep
- shifts & T-dep
- speed-dep.

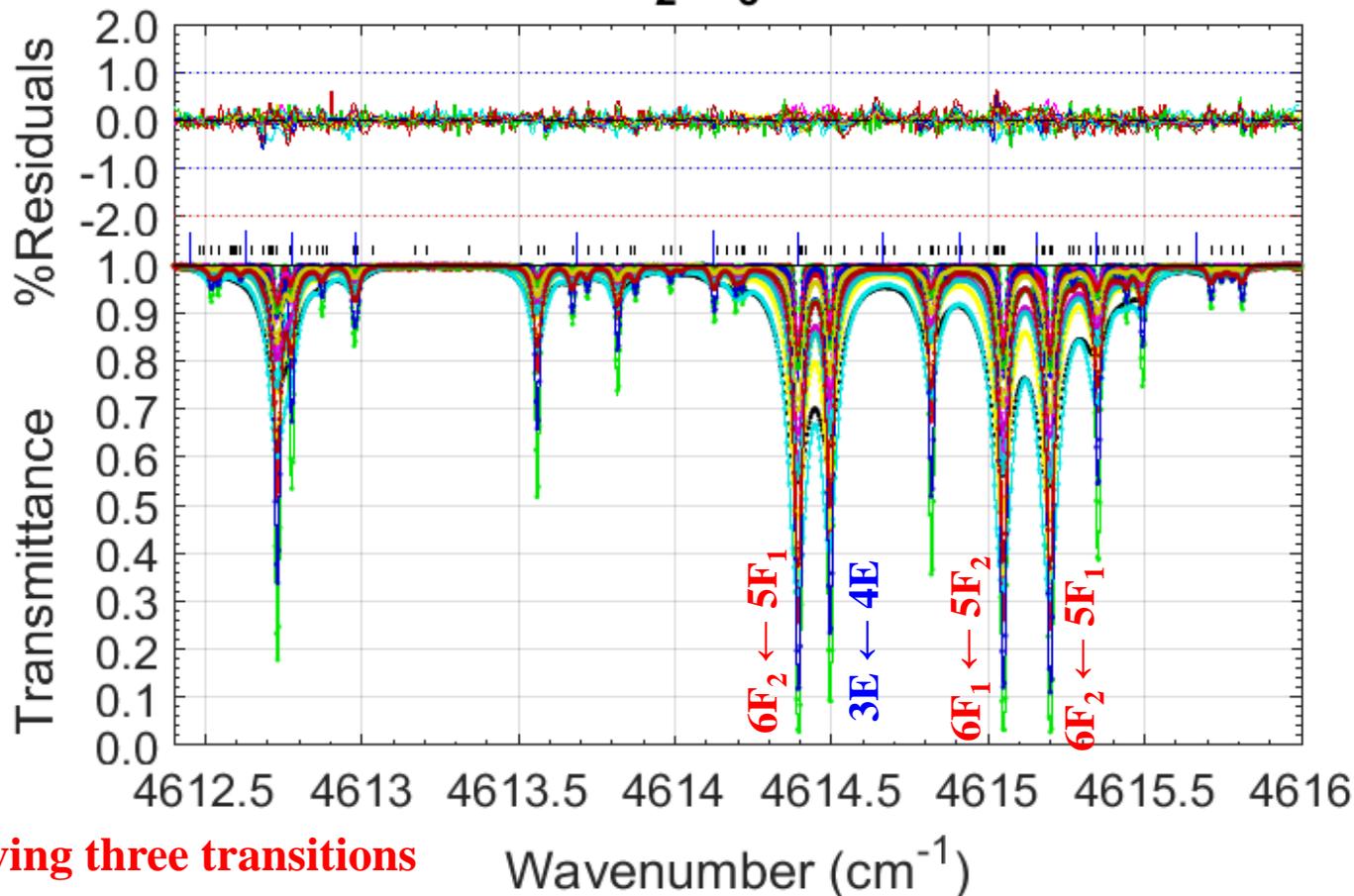
- **one pair of line mixing**



CH₄/H₂ ($\nu_2 + \nu_3$).R(5): x4612

- ❖ **Some statistics**
 - 19 spectra
 - 5 at RT
 - 5 at 200 K
 - two at 220 K
 - two at 200 K
 - 5 at T=340-370K

- **142 transitions**
 - positions,
 - intensities,
 - widths & T-dep
 - shifts & T-dep
 - speed-dep.
 - **line mixing involving three transitions**



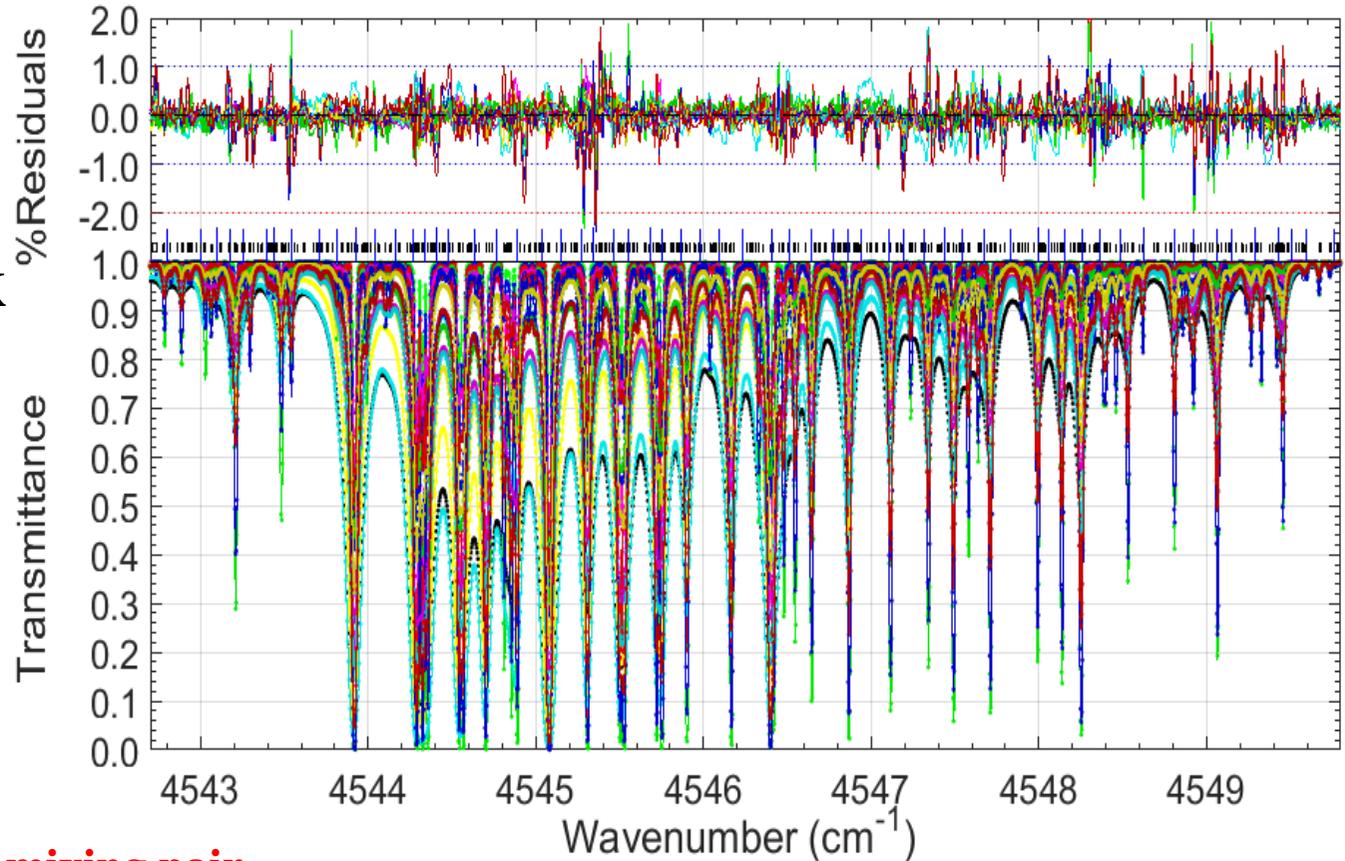
❖ Some statistics

- 19 spectra
- 5 at RT
- 5 at 200 K
- two at 220 K
- two at 200 K
- 5 at T=340-370K

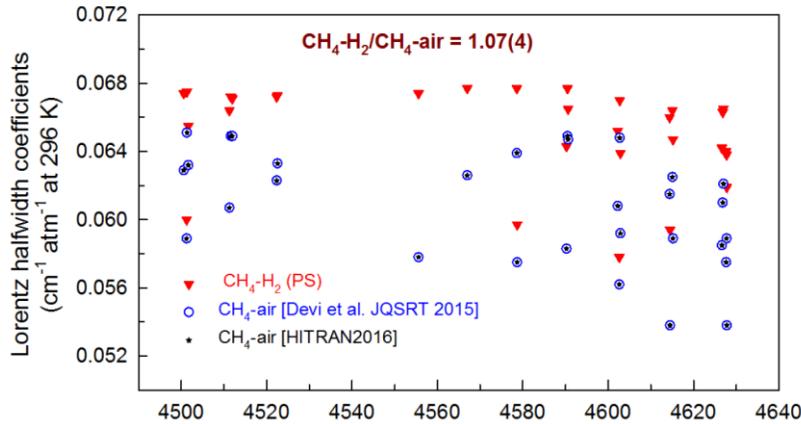
- 742 transitions
- positions,
- intensities,
- widths & T-dep
- shifts & T-dep
- speed-dep.

➤ **three sets of line mixing pair**

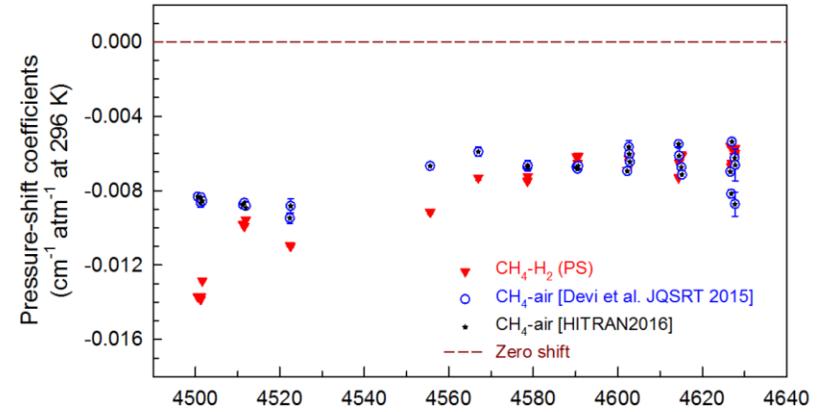
$^{12}\text{CH}_4 (v_2+v_3): Q(1) - Q(9)$



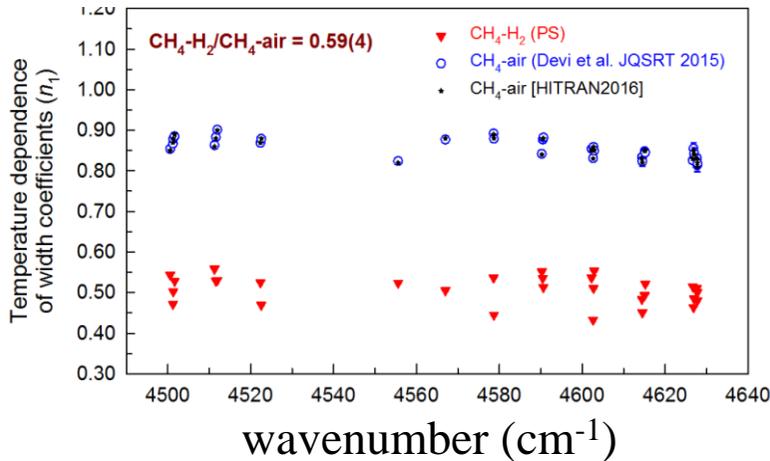
H₂-broadened width coefficients



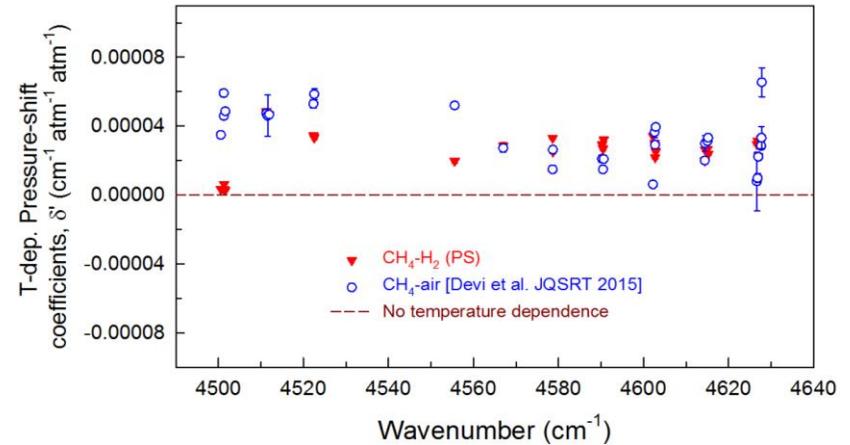
H₂-pressure-induced freq. shift coefficients



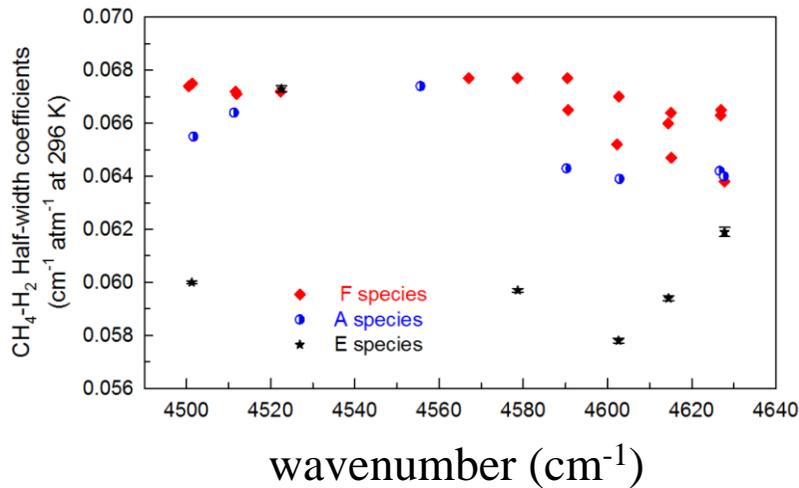
H₂-broadened width T-dep.



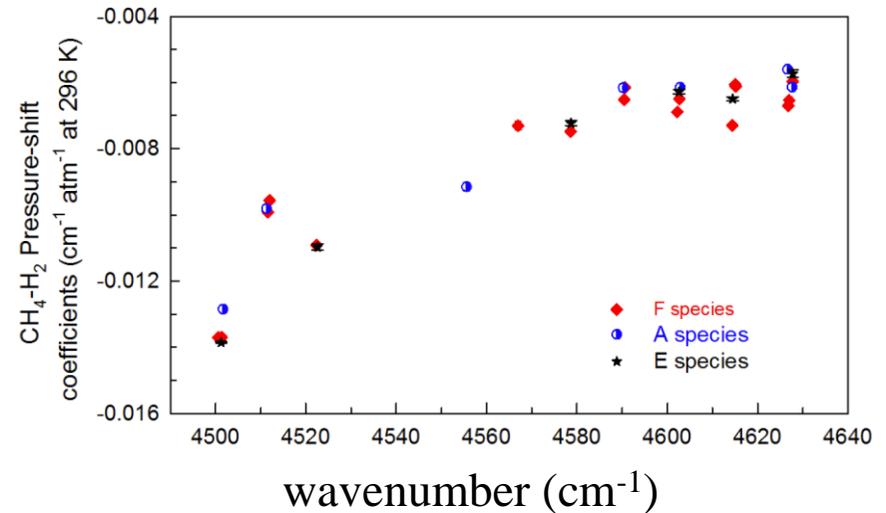
H₂-freq. shift T-dep.



H₂-broadened width coefficients



H₂-pressure-induced freq. shift coefficients





Preliminary results on Line Mixing



Measured Off-diagonal Relaxation Matrix Element coefficients

Pairs	Line ID	Positions (cm ⁻¹)	ORME coefficients (cm ⁻¹ /atm at T ₀ = 296 K)	
P(4)	3F1 ← 4F2	4500.555	0.0065(2)	0.045(9)
	3F2 ← 2F1	4501.310		
P(3)	2F1 ← 3F2	4511.595	0.0055(1)	0.086(8)
	2F2 ← 3F1	4511.929		
Q(3)	3F2 ← 3F1	4544.345	0.0107(3)	0.8 (Fixed)
	3F1 ← 3F2	4544.701		
Q(6)	6F1 ← 6F2	4545.900	0.0077(3)	0.8 (Fixed)
	6F2 ← 6F1	4546.166		
Q(9)	9F2 ← 9F1	4547.993	0.0156(5)	0.8 (Fixed)
	9F1 ← 9F2	4548.138		
R(3)	4F1 ← 3F2	4590.463	0.0058(1)	0.453(64)
	4F2 ← 3F1	4590.610		
R(4)	5F1 ← 4F2	4602.228	0.0065(3)	1.47(15)
	5F2 ← 4F1	4602.723		
R(5)	6F2 ← 5F1	4614.394	0.0007(1)	0.8 (Fixed)
	6F1 ← 5F2	4615.049	0.0100(3)	0.8 (Fixed)
	6F2 ← 5F1	4615.199		
R(6)	7F2 ← 6F1	4626.815	0.0051(2)	2.80(15)
	7F1 ← 6F2	4626.934		



Summary and further work



☐ Measured line shape parameters of H₂-Pressure broadened CH₄ spectra

- Obtained a series of spectra at 80 – 370 K of CH₄ pure and mixtures with H₂.
- Used a new version of Labfit_GUI (Graphic User Interface) [*Drouin, Benner, et al.*]
- Retrieved widths and shifts along with their T-dep. for 40 transitions from the $\nu_2+\nu_3$ band for the first time.
 - **Results show distinctive difference from Air-broadening**
 - **also, show A/E/F rotational symmetry species dependence for pressure broadening**
- Retrieved Line mixing coefficients for 19 transitions from 9 manifolds, including Q-br.

☐ Future work

- Supplied this measurement to theoretical models
- Continue to include the spectra at T < 200 K for this band.
- Measure the line shape parameters for $\nu_3+\nu_4$ band
- Make comparison with theoretical calculations
- Suggest the parameters for high temperatures based on the combined efforts

Acknowledgements

Research described in this talk was performed under the National Aeronautics and Space Administration. We thank Drs. B. J. Drouin, A. Guillaume, M. Cich for the GUI version of the Labfit.