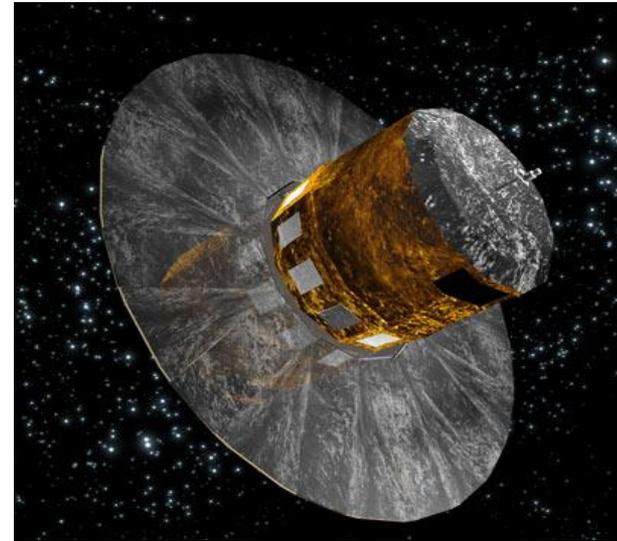
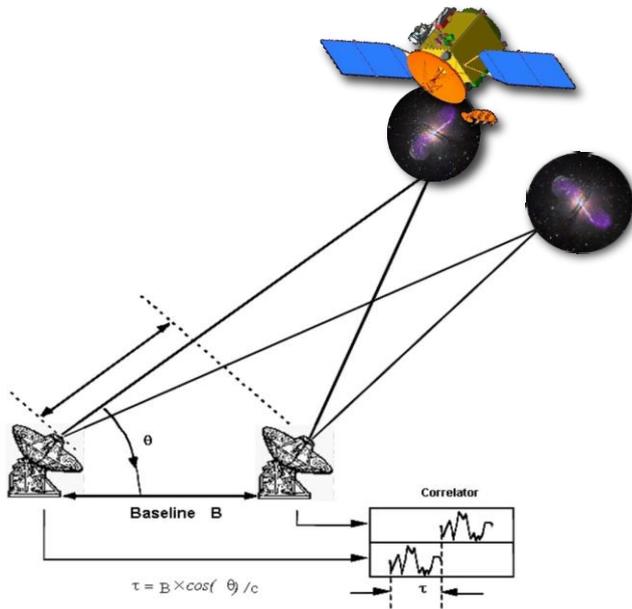




# Tying multiple Radio Wavelength Celestial Frames to the Gaia Optical Frame



**Christopher S. Jacobs,** *Jet Propulsion Laboratory, California Institute of Technology*

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L. Snedeker, G. Bourda, P. Charlot.



# Overview: Optical vs. Radio Celestial Frames

- **History:** VLBI at SX (8 GHz, 3.6cm) has been only sub-mas frame until last 10 years  
(e.g. *Ma+*, *ICRF1*, 1998, *Ma+*, *ICRF2*, 2009)
- K-band (24 GHz, 1.2cm) now sub-mas (*Lanyi+*, 2010; *de Witt+*, 2016)
- X/Ka (32 GHz, 9mm) also sub-mas (*Jacobs+*, 2016)
- Gaia optical: data release #1 is sub-mas for auxiliary quasar solution  
(*Prusti+*, 2017)
- Precision is excellent allowing 3-D rotational alignment precision of 10 to 20  $\mu\text{as}$
- Accuracy limited by VLBI systematics due to weak southern geometry, troposphere, etc. at few 100  $\mu\text{as}$
- Gaia precision limited to  $\sim 500 \mu\text{as}$  by short span of data in DR#1.



# What objects can we use?



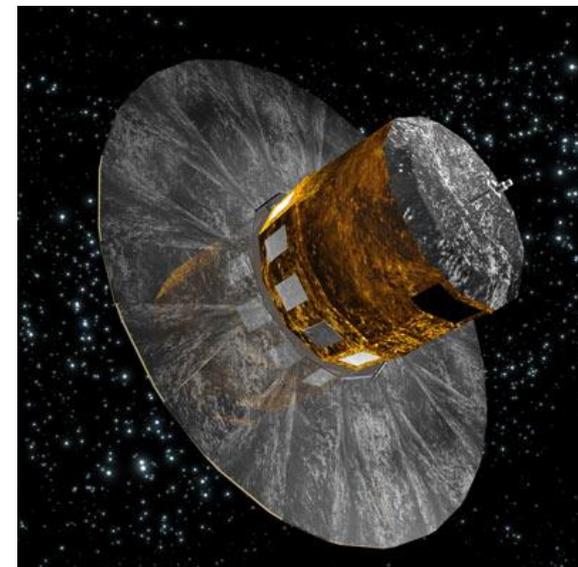
## Methods for Tying Optical and Radio Celestial Frames

- Need common objects well measured in both optical and radio
- **Radio stars:** Previous generation used galactic stars that emit in radio,  
**Crude by today's standards: difficult to achieve desired accuracy level.**  
e.g. Lestrade et al. (1995).
- **Thermal emission from regular stars:**  
350 GHz astrometry using Atacama Large Millimeter Array (ALMA)  
Fomalont et al. (pilot observations)  
Verifies bright end of optical, **but likely limited to 500 – 1000  $\mu$ as (2.5 to 5 ppb).**
- **Extra-galactic Quasars:** detectable in both radio and optical  
potential for better than 100  $\mu$ as to 20  $\mu$ as (0.5 to 0.1 ppb).  
**Strengths: extreme distances (> 1 billion light years) means no parallax or proper motion**

# The Gaia Optical Frame

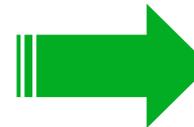
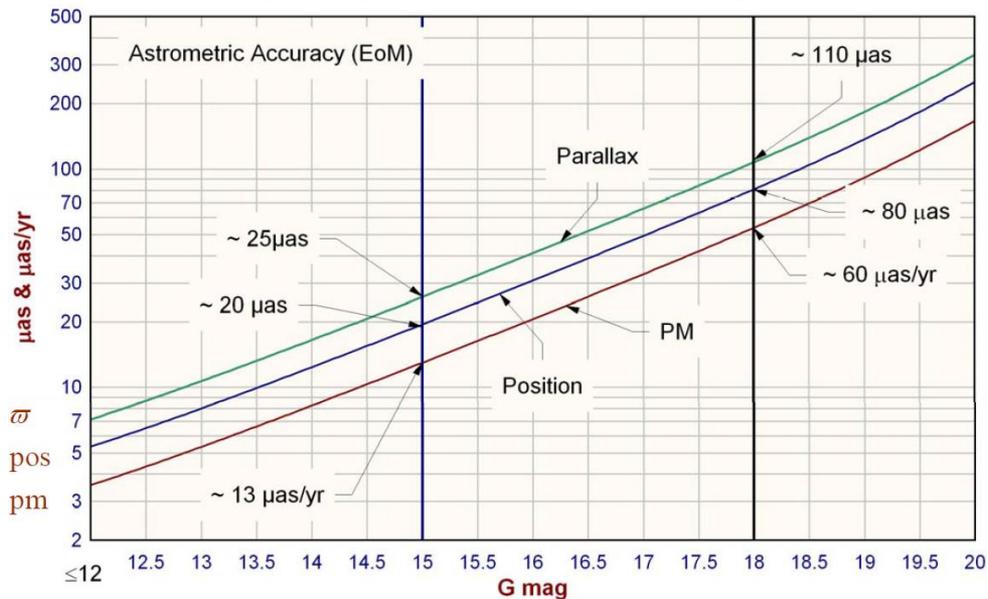
# ESA's Gaia optical Astrometry

- Method: extremely accurate centroid of 60 mas pixels. Compare to VLBI sub-mas beam.
- **Astrometry & photometric survey to  $V = 20.7^{\text{mag}}$** 
  - $\sim 10^9$  objects: stars, QSOs, solar system, galaxies.
- **Gaia Celestial Reference Frame (GCRF):**
  - Optically bright objects ( $V < 18\text{mag}$ ) give best precision
  - 1st release Gaia astrometric catalog DR1 Sep 2016,
  - DR2 Apr 2018.



Credit: F. Mignard (2013)

## Anticipated precision of Gaia catalogue



## Gaia release-1:

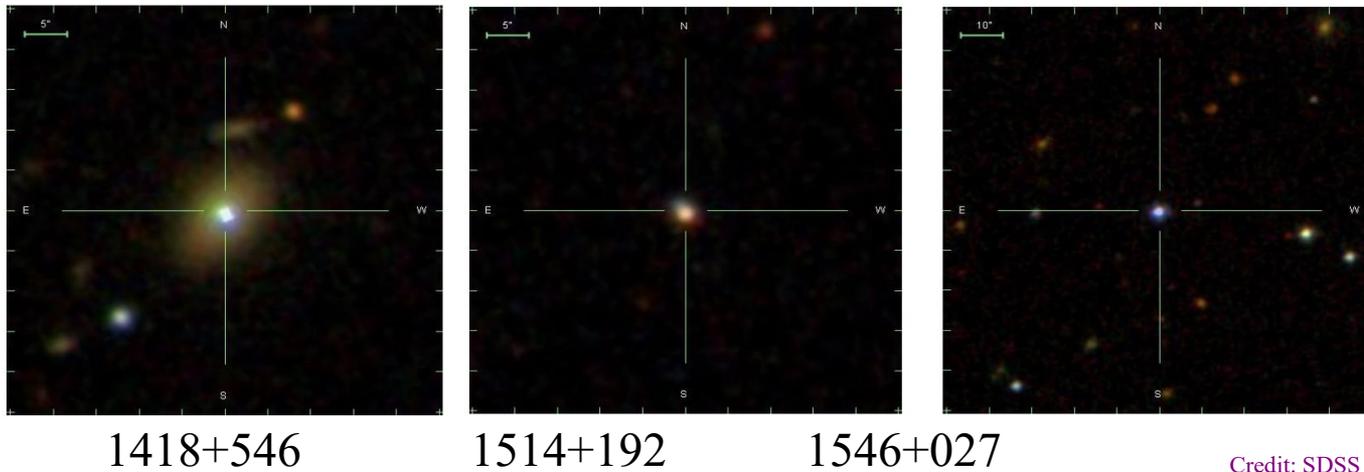
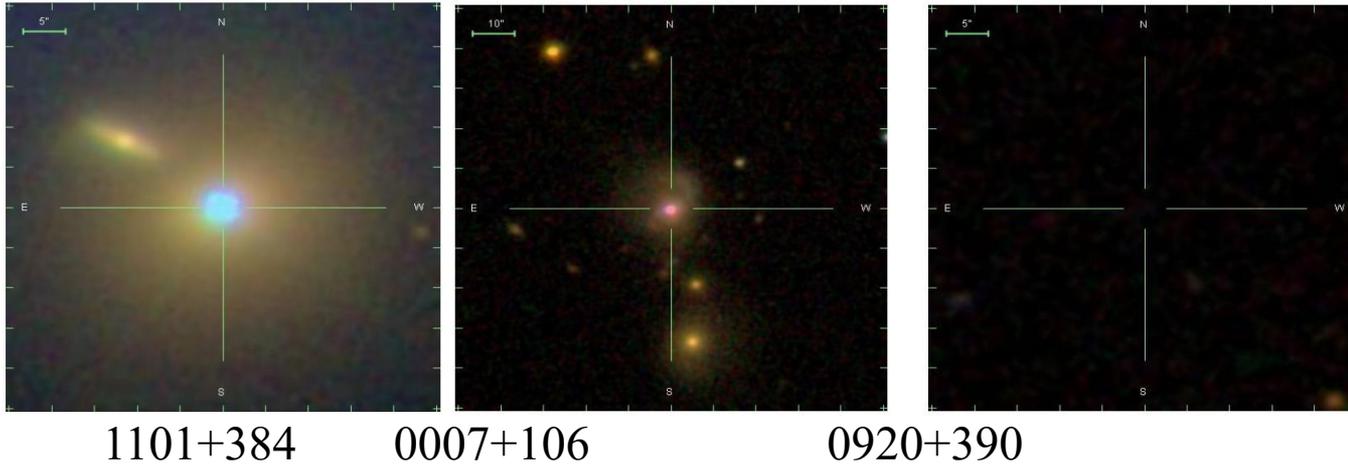
**$\sim 0.3$  mas in positions and parallaxes for 2 million brightest stars**

**$\sim 10$  mas for rest of the stars**



# Optical vs. Radio systematics offsets

## SDSS Optical images of quasars (scale 5-10 asec)



- Optical structure: The host galaxy may not be centered on the AGN or may be asymmetric.
- Optical systematics unknown, fraction of millarcsecond optical centroid offset?
- Optical imaging generally 10s of milliarcsecond. In general, no sub-mas optical imaging.

Celestial Frames  
using  
Radio Interferometry  
(VLBI)

# Radio Interferometry: Long distance phased arrays

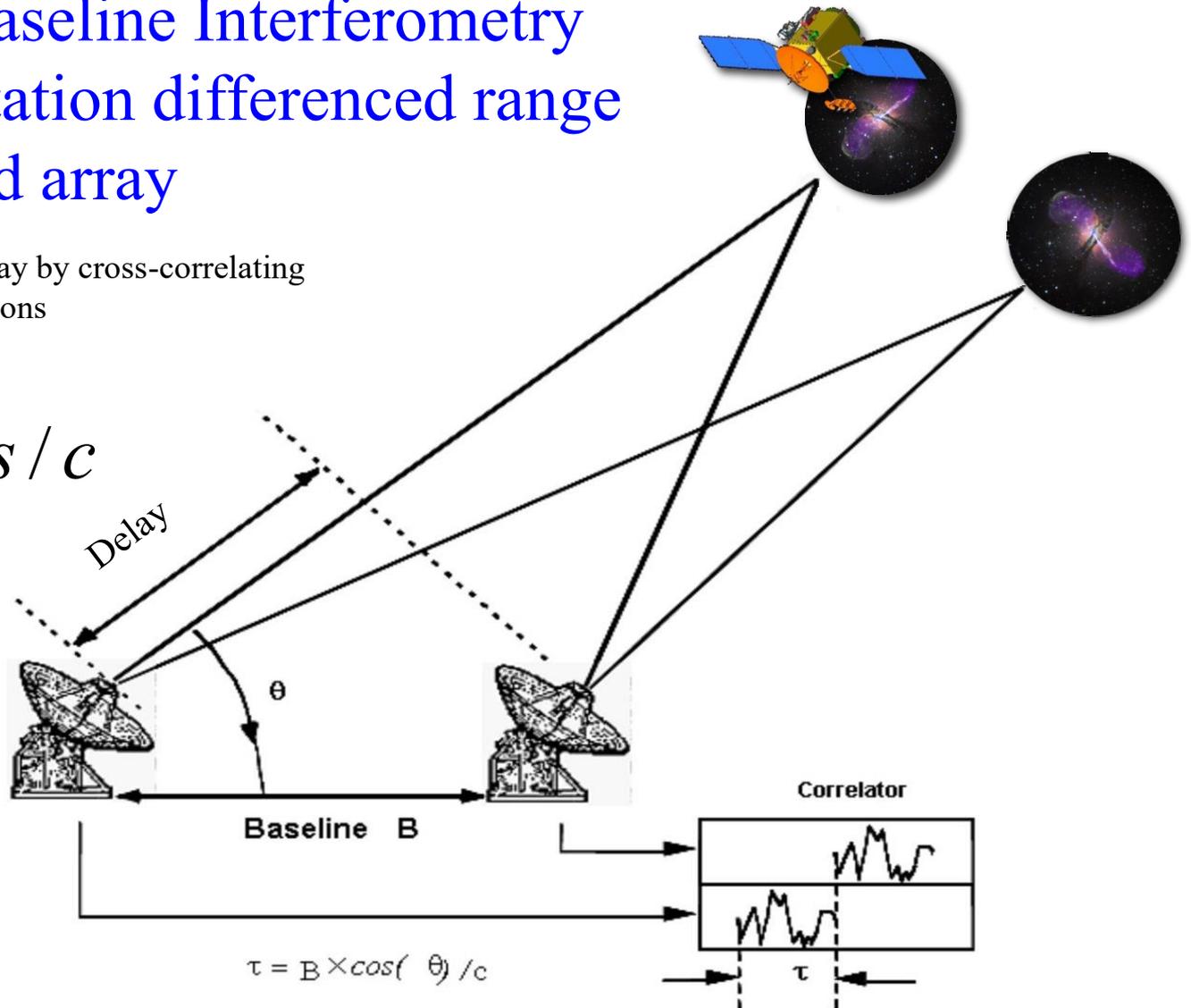
## Very Long Baseline Interferometry is a type of station differenced range from a phased array

- Measures geometric delay by cross-correlating signal from two (2) stations

$$t = B \cdot s / c$$

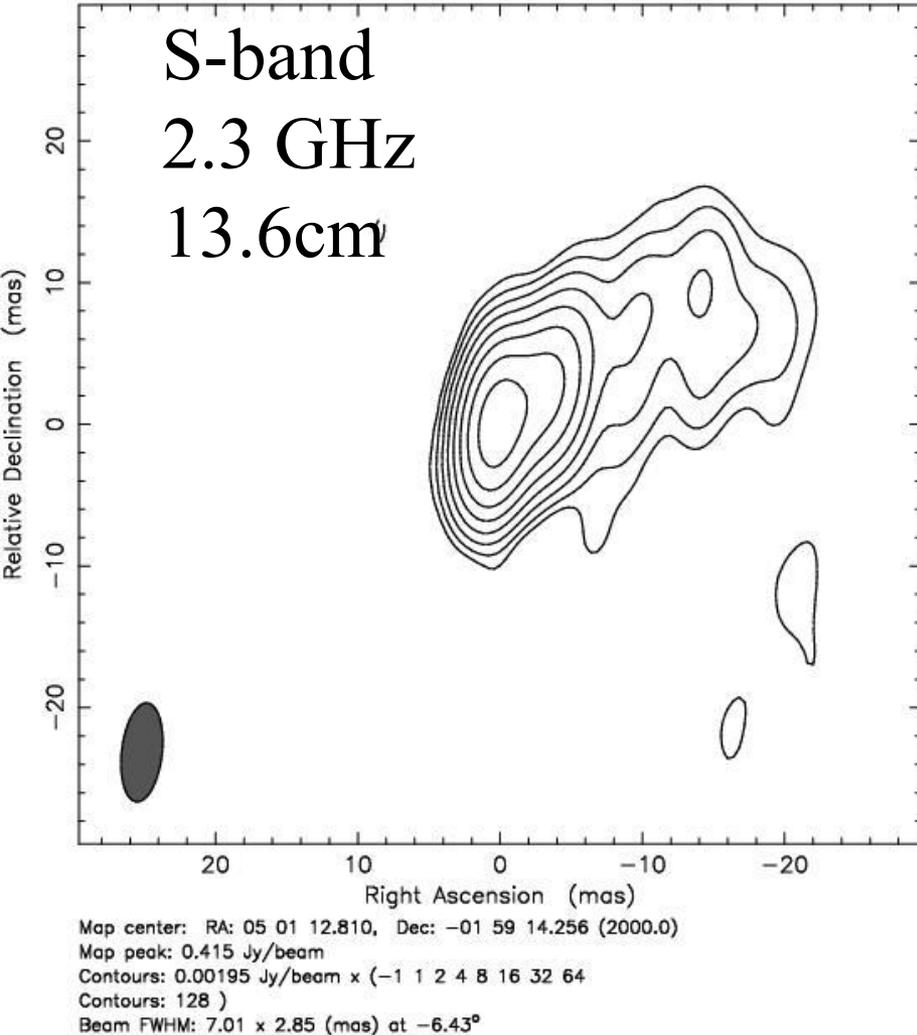
10,000 km baselines give resolution of  $\lambda/B \sim$  few nanoradian sub-mas beam !!

Resolves away all but galactic nucleus



# Radio Source Structure vs. Frequency

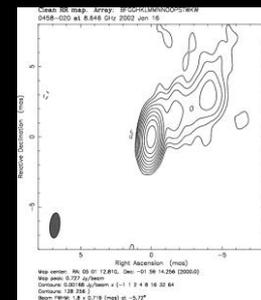
Clean RR map. Array: BFGGHLMMNNOOPSTWKW  
0458-020 at 2.302 GHz 2002 Jan 16



**X-band**  
8.6 GHz  
3.6cm

**K-band**  
24 GHz  
1.2cm

**Q-band**  
43 GHz  
0.7cm



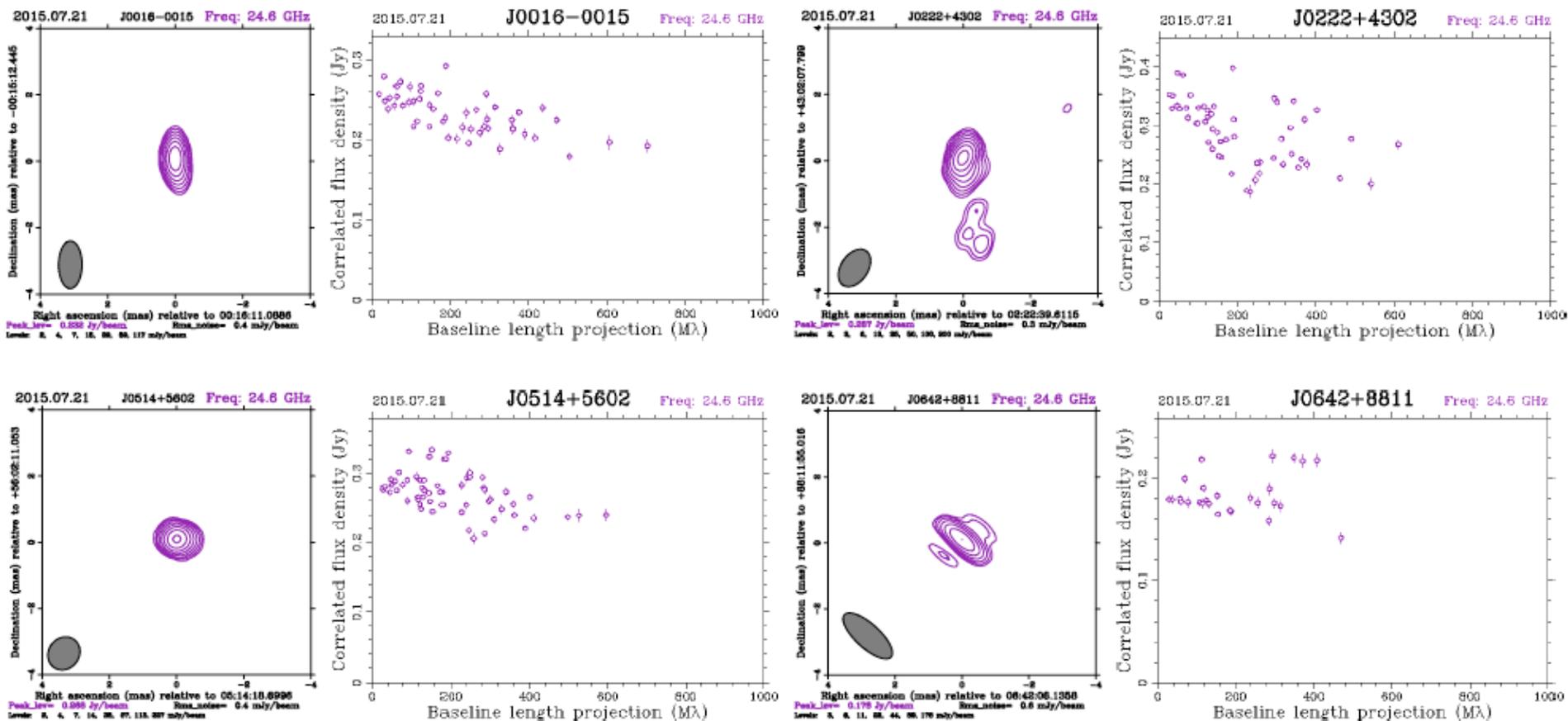
**The sources become better → Less structure**

**Ka-band**  
32 GHz  
0.9cm

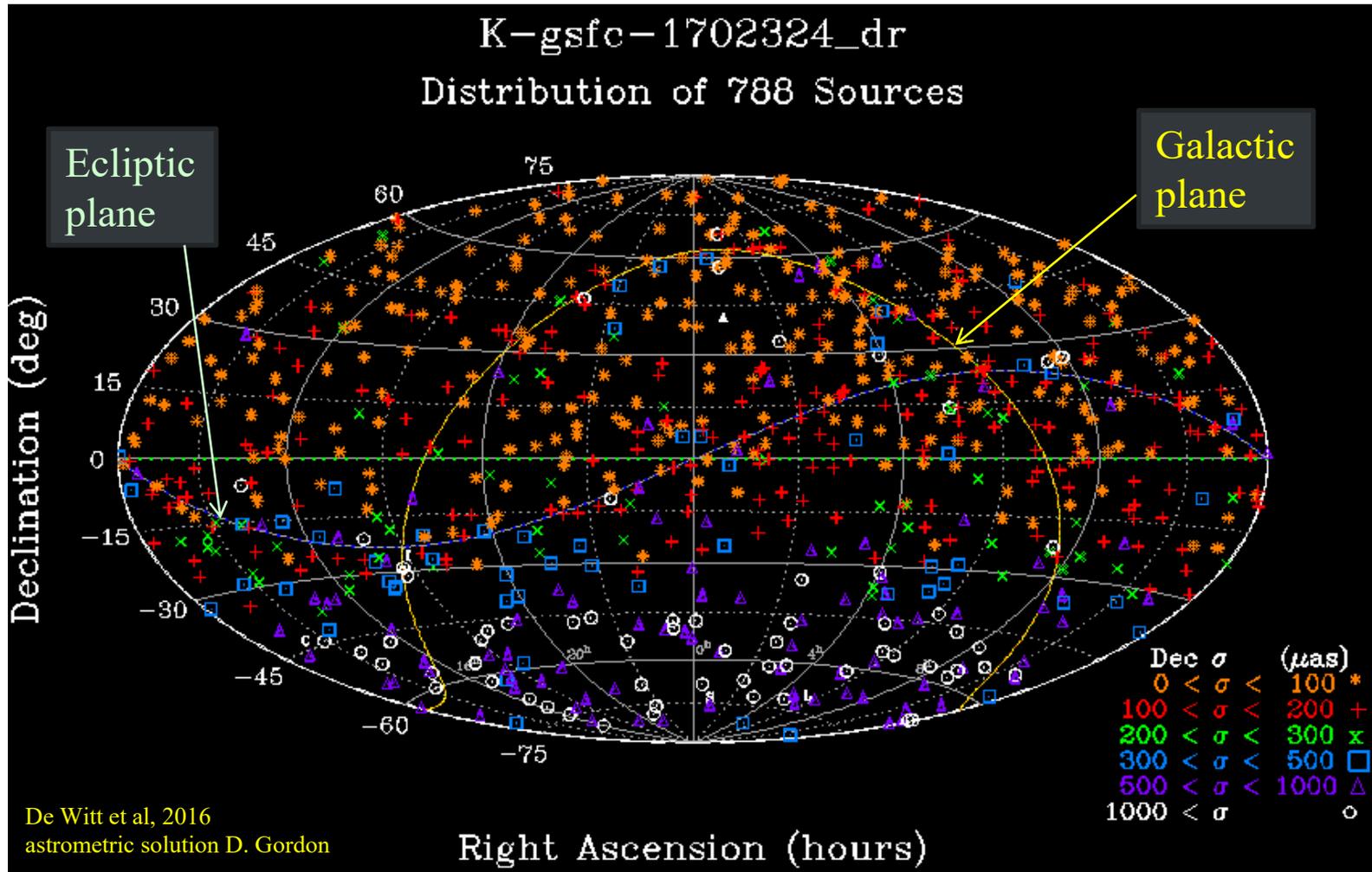
Images credit: Pushkarev & Kovalev *A&A*, 544, 2012 (SX);

Charlot et al, *AJ*, 139, 2010 (KQ)

# Imaging: VLBA at 24 GHz (1.2cm) (de Witt et al, 2016)

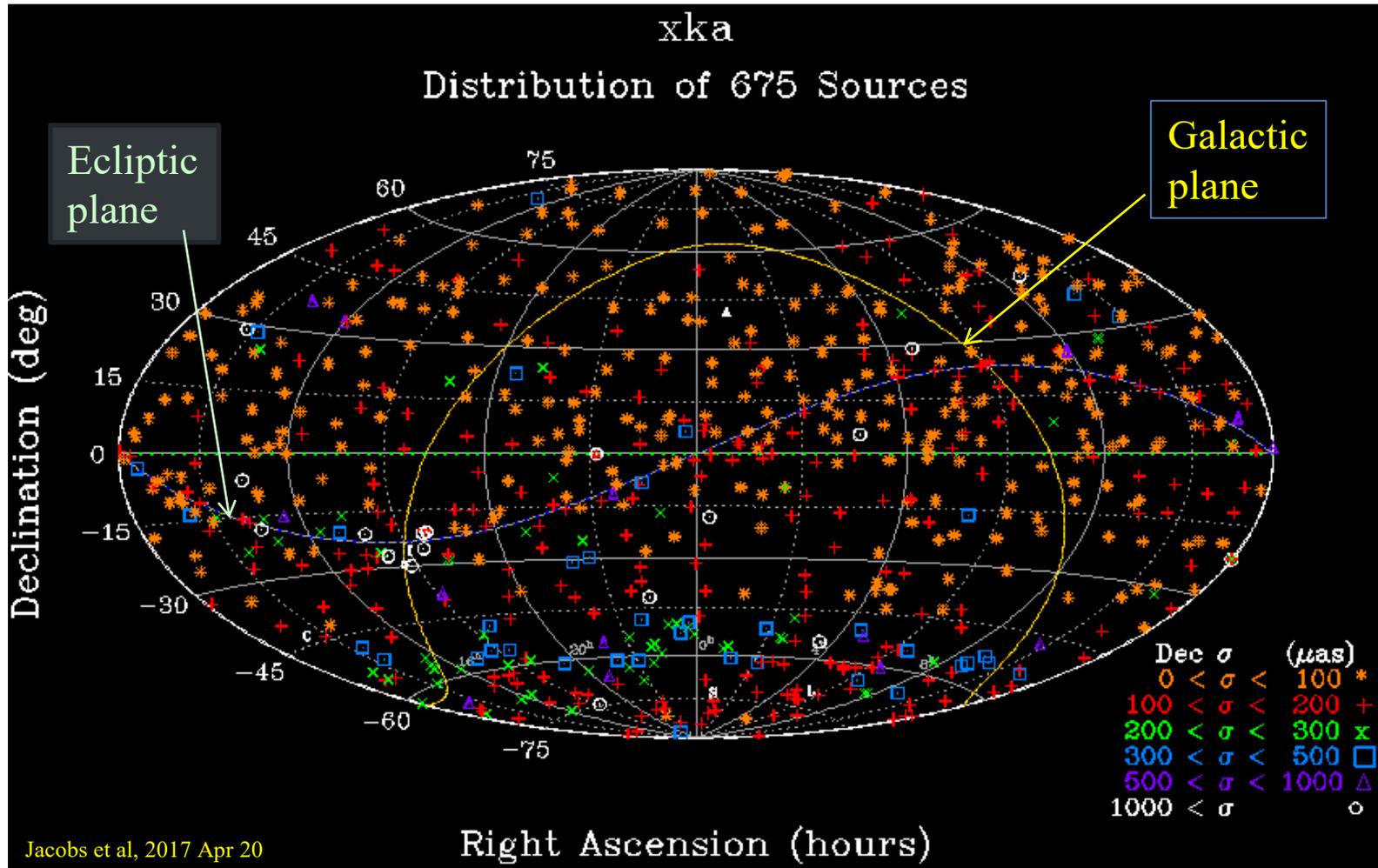


K-band (24 GHz) imaging shows VLBI sources are compact on millarcsec scales.  
Data for 500+ sources acquired. Processing limited by available analyst resources.  
Imaging will be prioritized as comparison outliers pinpoint sources of interest



- **Strengths:**
  - Uniform spatial density
  - Galactic plane sources (Petrov+ 2006)
  - less structure than S/X (3.6cm)
  - precision < 100  $\mu\text{as}$
  - needed ~ 0.25 million observations vs. SX's 12 million!

- **Weaknesses:**
  - Ionosphere only partially calibrated by GPS.
  - No solar plasma calibrations
  - South ( $\delta < -30$  deg) weak due to limited South Africa-Tasmania data



- **Strengths:**
  - Uniform spatial density
  - less structure than S/X (3.6cm)
  - precision  $< 100 \mu\text{as}$
  - needed only 60K observations vs. SX's 12 million!

- **Weaknesses:**
  - Poor near Galactic center due to inter-stellar media scattering
  - South weak due to limited time on ESA's Argentina station
  - Limited Argentina-California data makes vulnerable to  $\delta$  zonals
  - Limited Argentina-Australia weakens  $\delta$  from -45 to -60 deg



# Ka-band combined NASA/ESA Deep Space Net



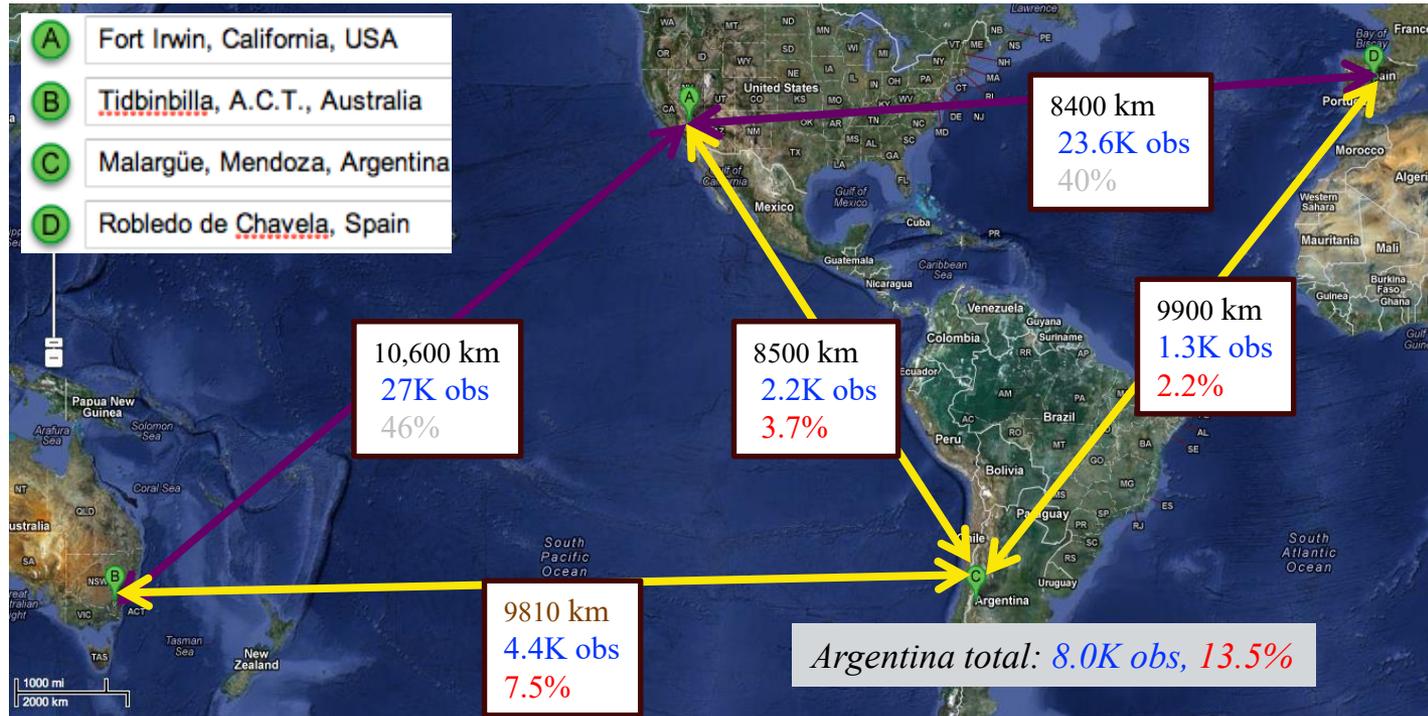
ESA Argentina to NASA-California under-observed by order of magnitude!

## Baseline percentages

- Argentina is part of 3/5 baselines or 60% but only 13% of obs
- Aust- Argentina 7.5%
- Spain-Argentina 2.2%
- Calif- Argentina 3.7%

This baseline is under-observed by a factor of ~ 12.

More time on ESA's Argentina station would have a huge, immediate impact!!



Maps credit: Google maps

ESA's Argentina 35-meter antenna adds 3 baselines to DSN's 2 baselines

- Full sky coverage by accessing south polar cap
- near perpendicular mid-latitude baselines: CA to Aust./Argentina



Three VLBI bands compare to better than 200  $\mu\text{s}$  RMS  
 Gaia DR-1 precision  $\sim 500 \mu\text{s}$ . DR-2 vs. VLBI may reveal zonals

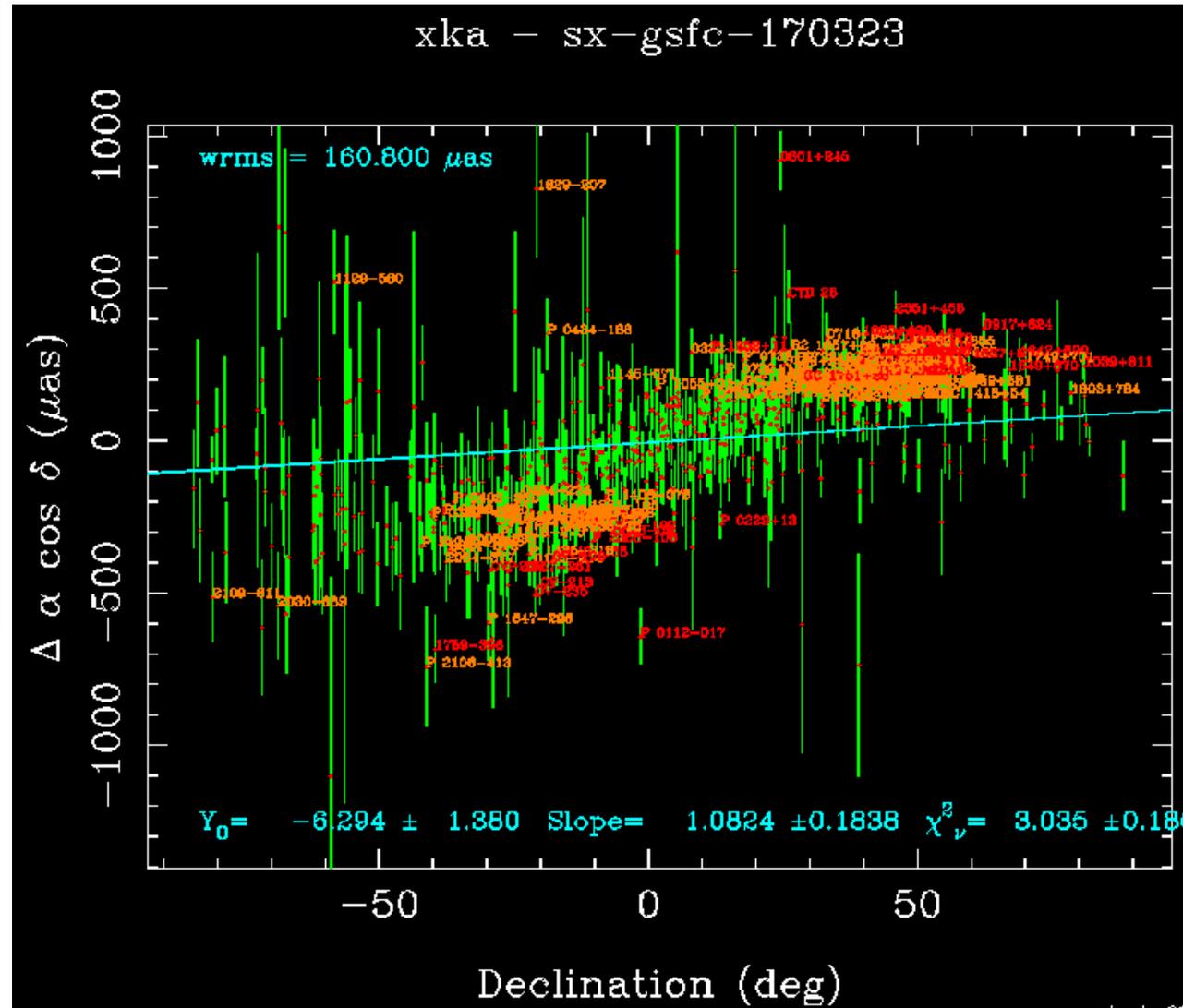


### Zonal Errors

- $\Delta\text{RA}$  vs. Dec:  
 $\sim 300 \mu\text{s}$  in south,  $200 \mu\text{s}$  in north
- Need 2 baselines to get 2 angles:  
 California-Canberra: 24K obs  
 California-Argentina: 2K obs
- > Need more California-Argentina data to overcome this 12 to 1 distortion in sampling geometry.  
 ESA's Malargüe is key.
- Usuda, Japan 54-m XKa (2019) would improve North-South sampling geometry and thus control declination zonal differences.



### XKa vs. SX: Zonal errors

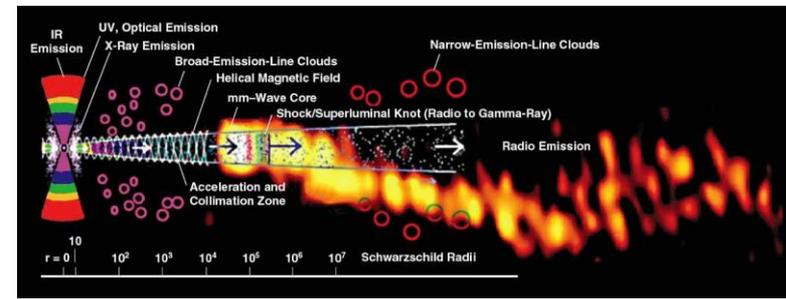


eslabobs-23

The goal:

Alignment of Optical and Radio  
into Common Frame

# Optical-Radio Frame Tie Geometry



Credit: Marscher+, Krichbaum+

Determine 3 small rotations ( $R_{1,2,3}$ ) and zonal differences i.e. spherical harmonics  $Y_{lm}$  between the individually rigid, non-rotating **radio** and **optical** frames to sub-part per billion level

Allows seamless integration into united frame.

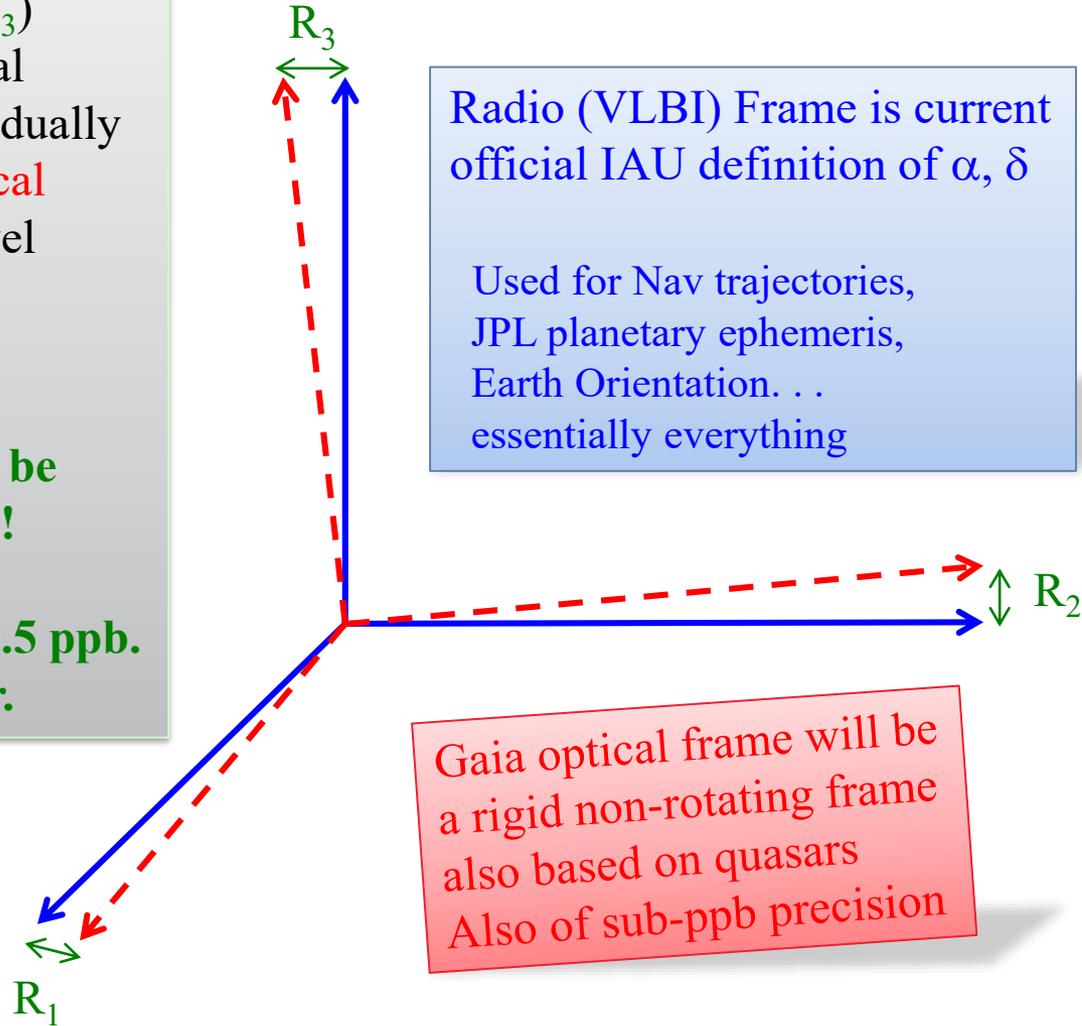
**More than 1 billion objects will be integrated into common frame!!**

**Object precision to  $< 100 \mu\text{as}$ , 0.5 ppb. want tie errors 10 times smaller.**

Radio (VLBI) Frame is current official IAU definition of  $\alpha, \delta$

Used for Nav trajectories, JPL planetary ephemeris, Earth Orientation. . . essentially everything

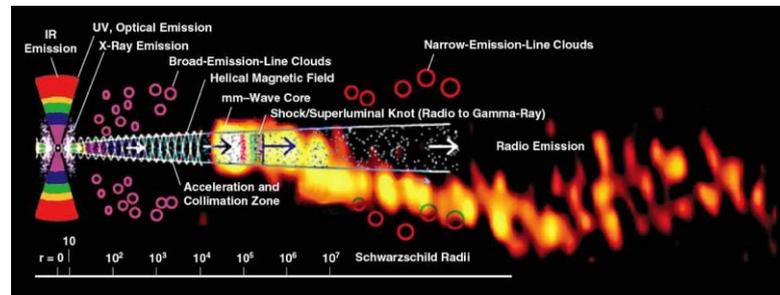
Gaia optical frame will be a rigid non-rotating frame also based on quasars Also of sub-ppb precision



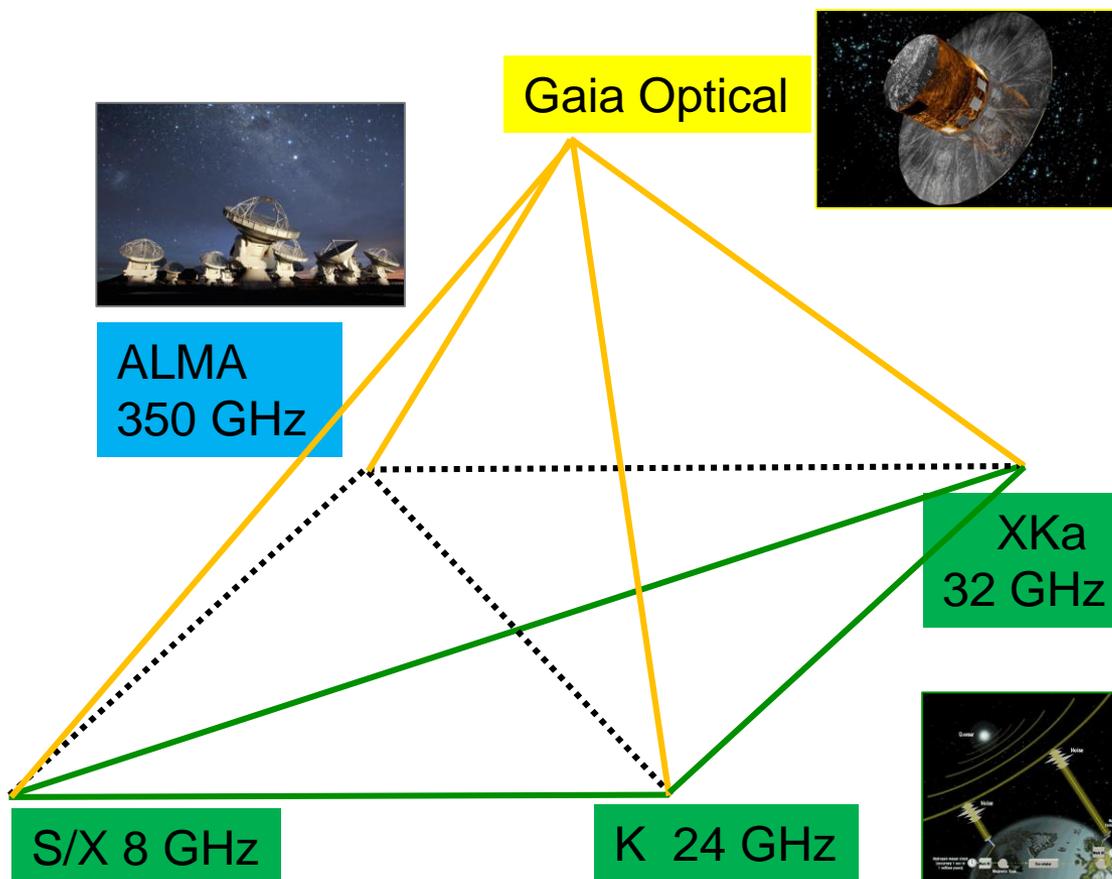
# Frame Tie Comparisons

## Tying Optical and Radio Celestial Frames

Systematics to be flushed out via  
Inter-comparison of multiple high  
precision frames.



Credit: Marscher+, Krichbaum+



### Systematics:

Gaia: 60 mas beam sees  
Host galaxy, foreground stars, etc.

ALMA: pilot obs bright end  $\sim 5^{\text{mag}}$   
Waiting on 10km+ configurations

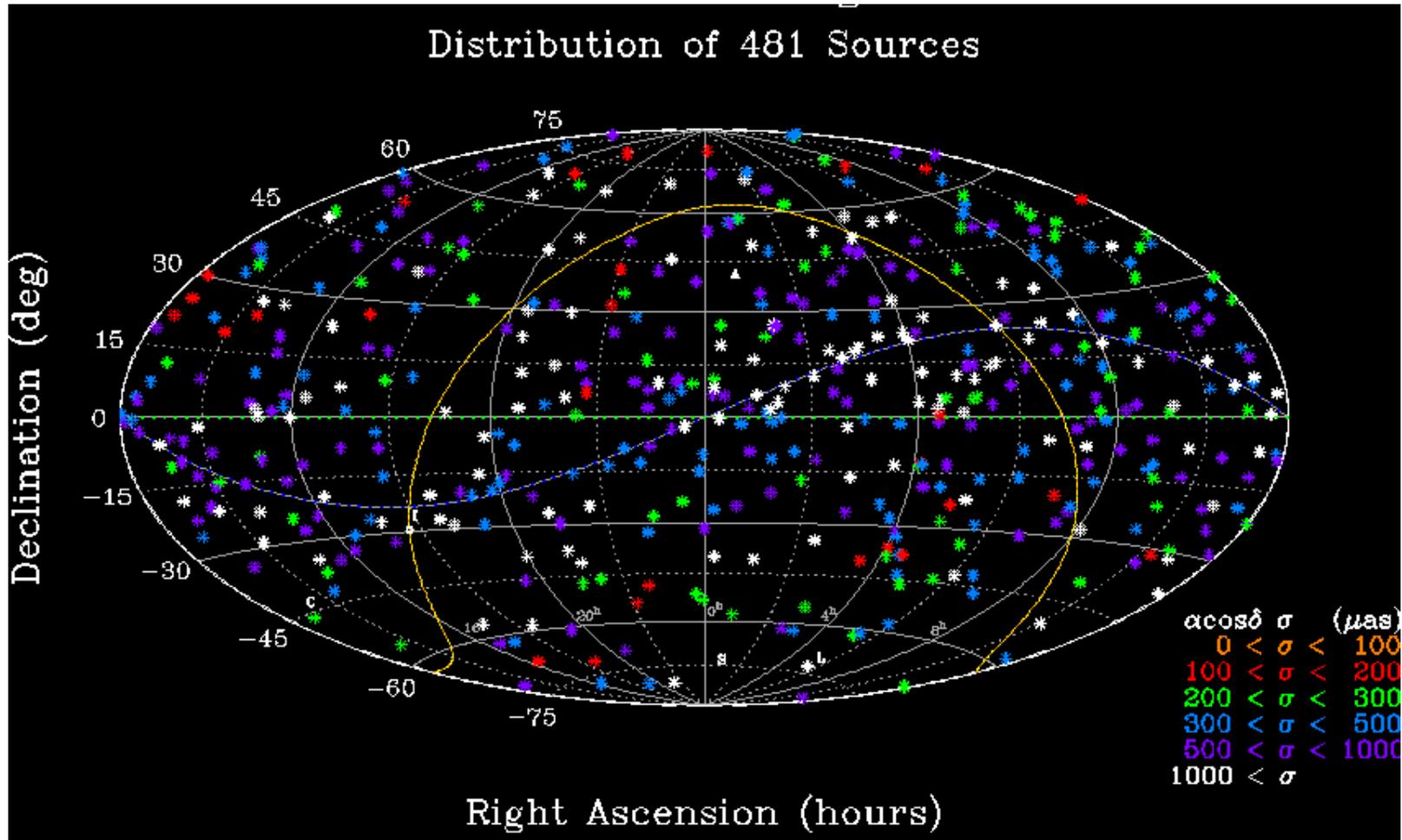
VLBI: All bands need more  
southern data

S/X: Source structure  
K: Ionosphere  
XKa: Argentina baselines  
under-observed

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. K VLBI



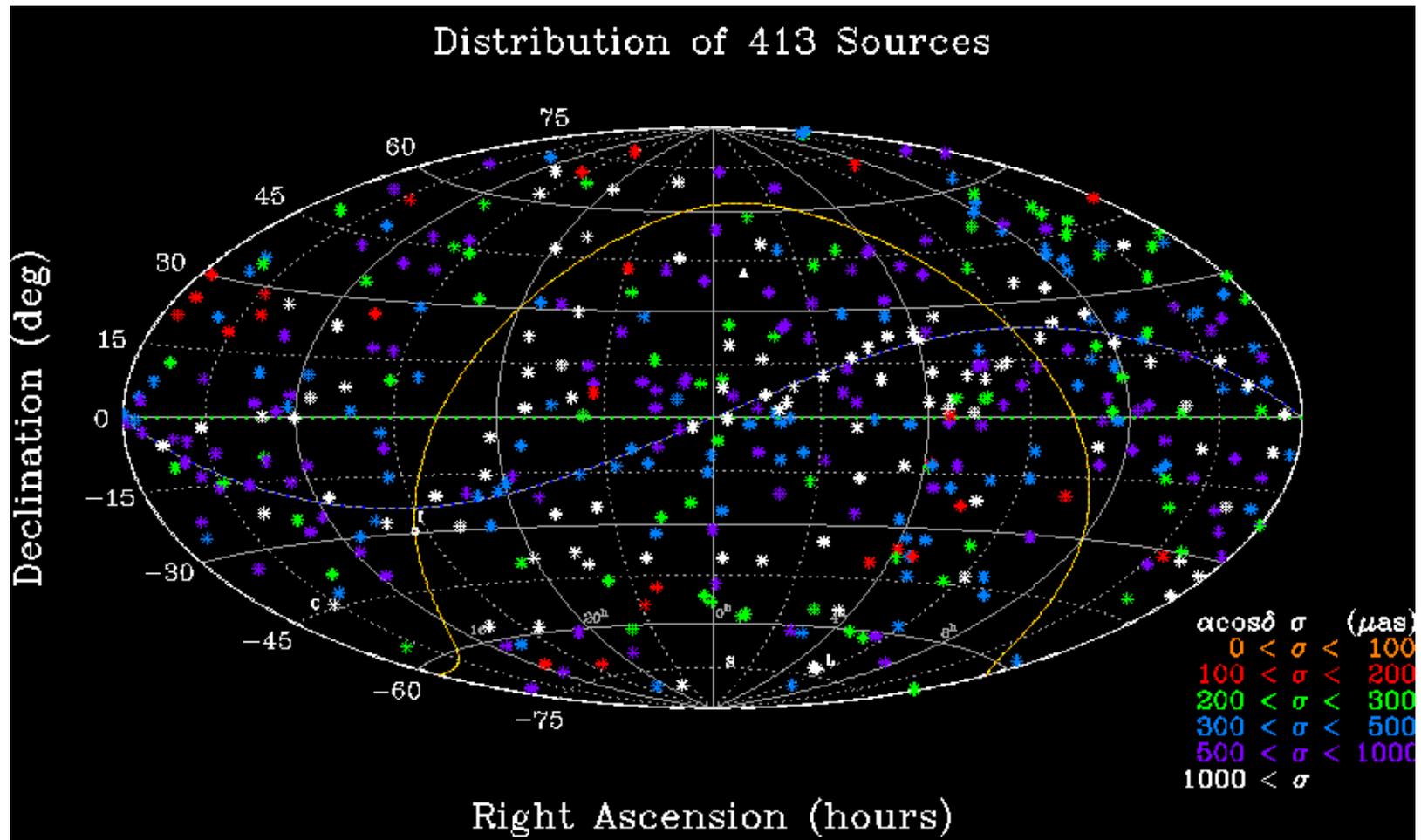
Fairly uniform distribution.

Color code shows Gaia formal sigmas.

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI

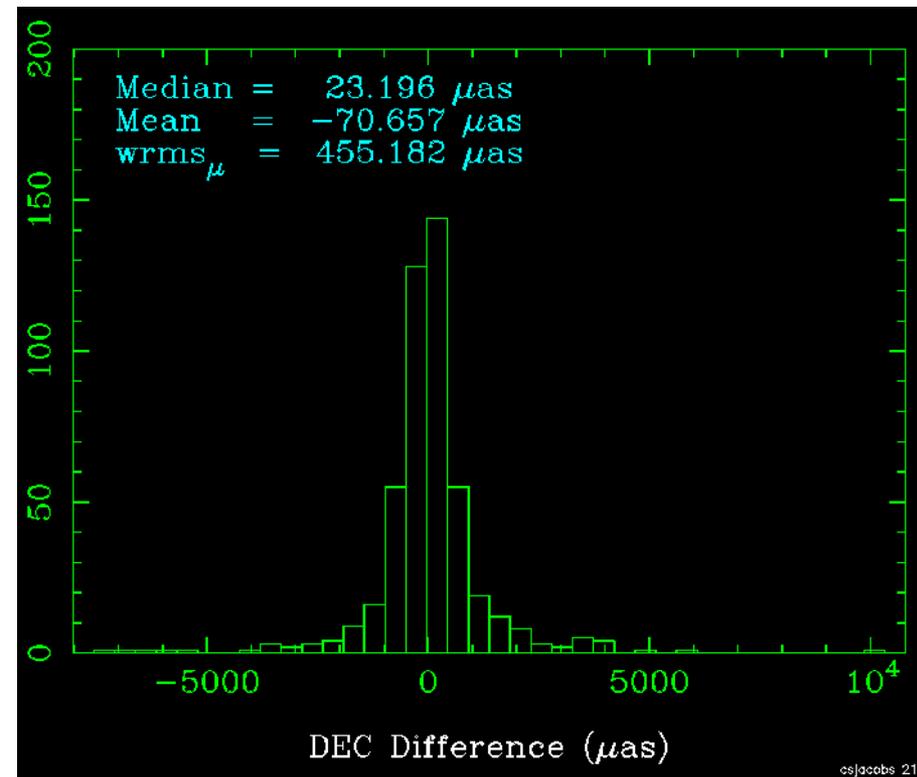
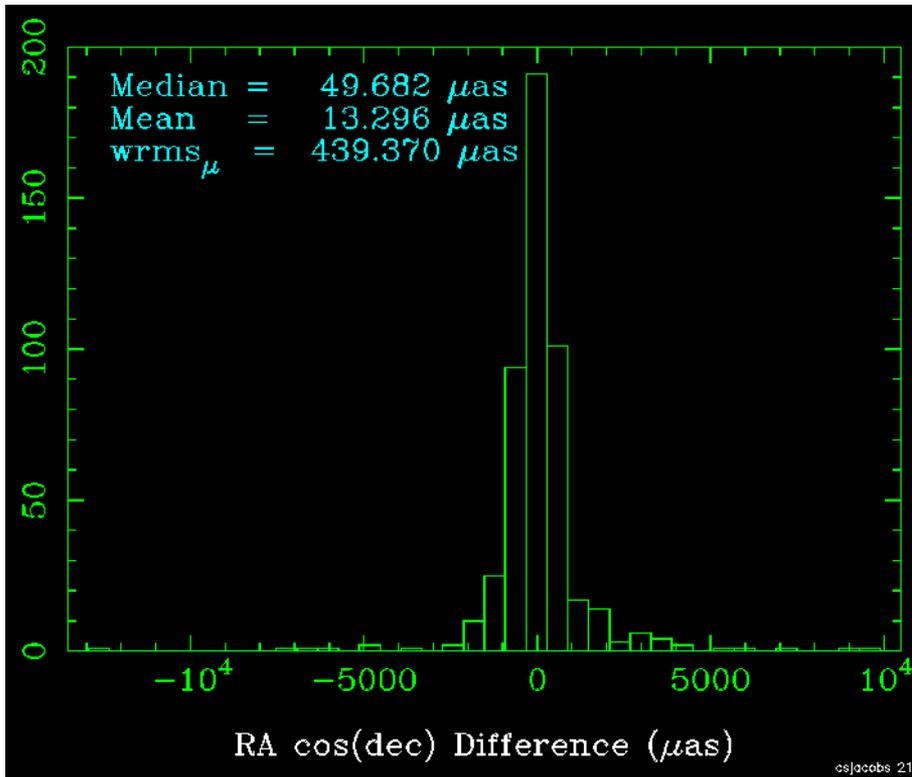


Fairly uniform distribution.

Color code shows Gaia formal sigmas.



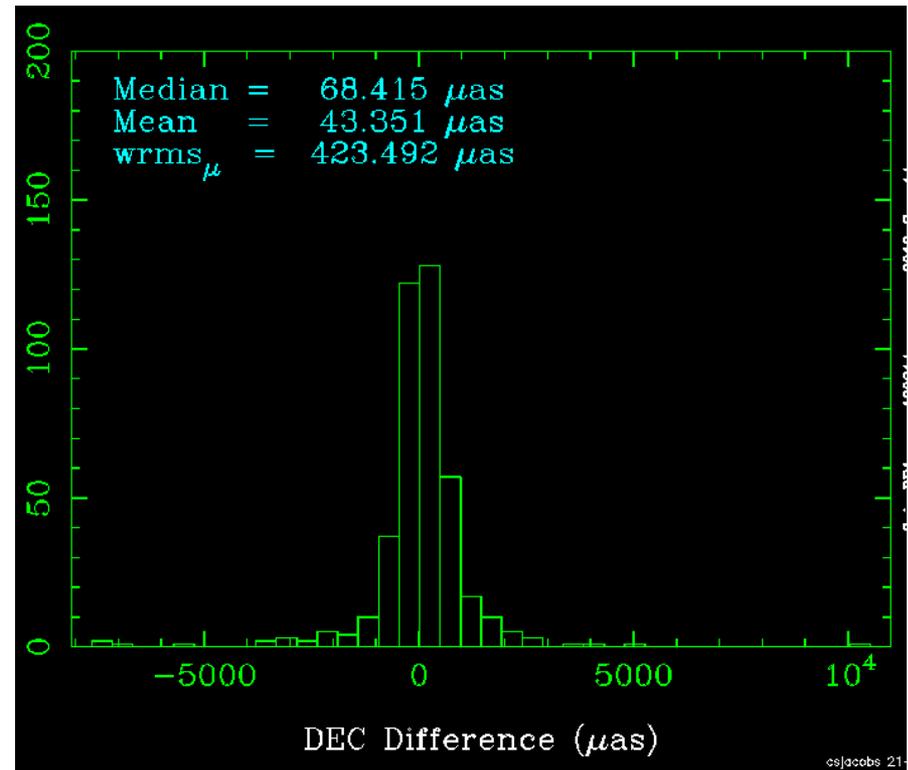
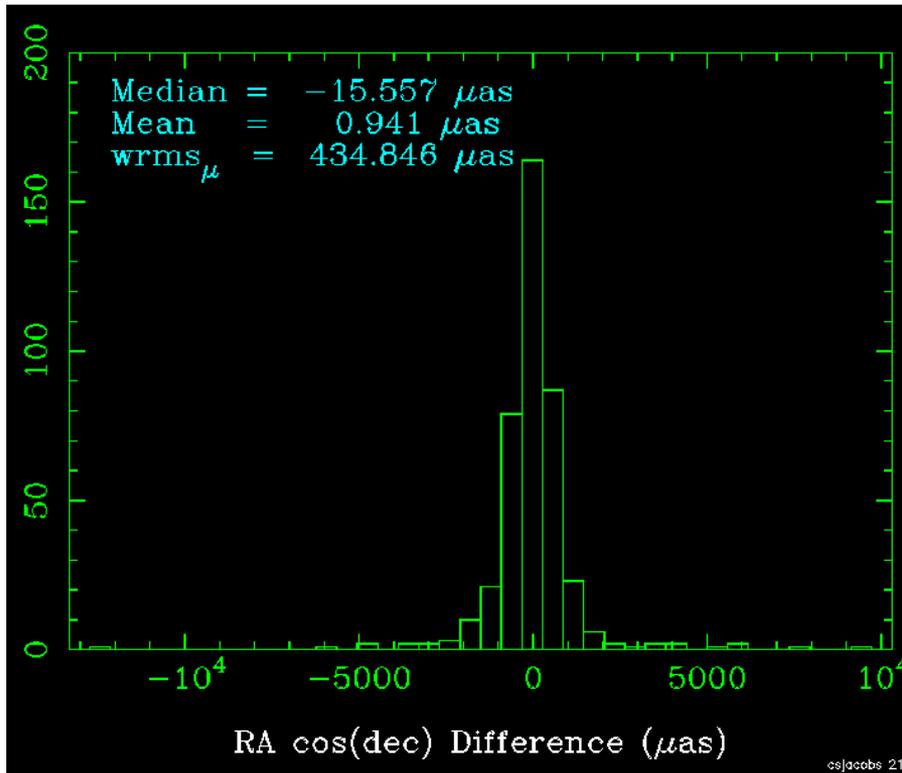
## Gaia DR1-aux vs. K VLBI



wRMS Ra and Dec differences about 440  $\mu\text{as}$  (2 nrad)  
Normalized differences are about 1.1 indicating realistic errors



## Gaia DR1-aux vs. Ka VLBI

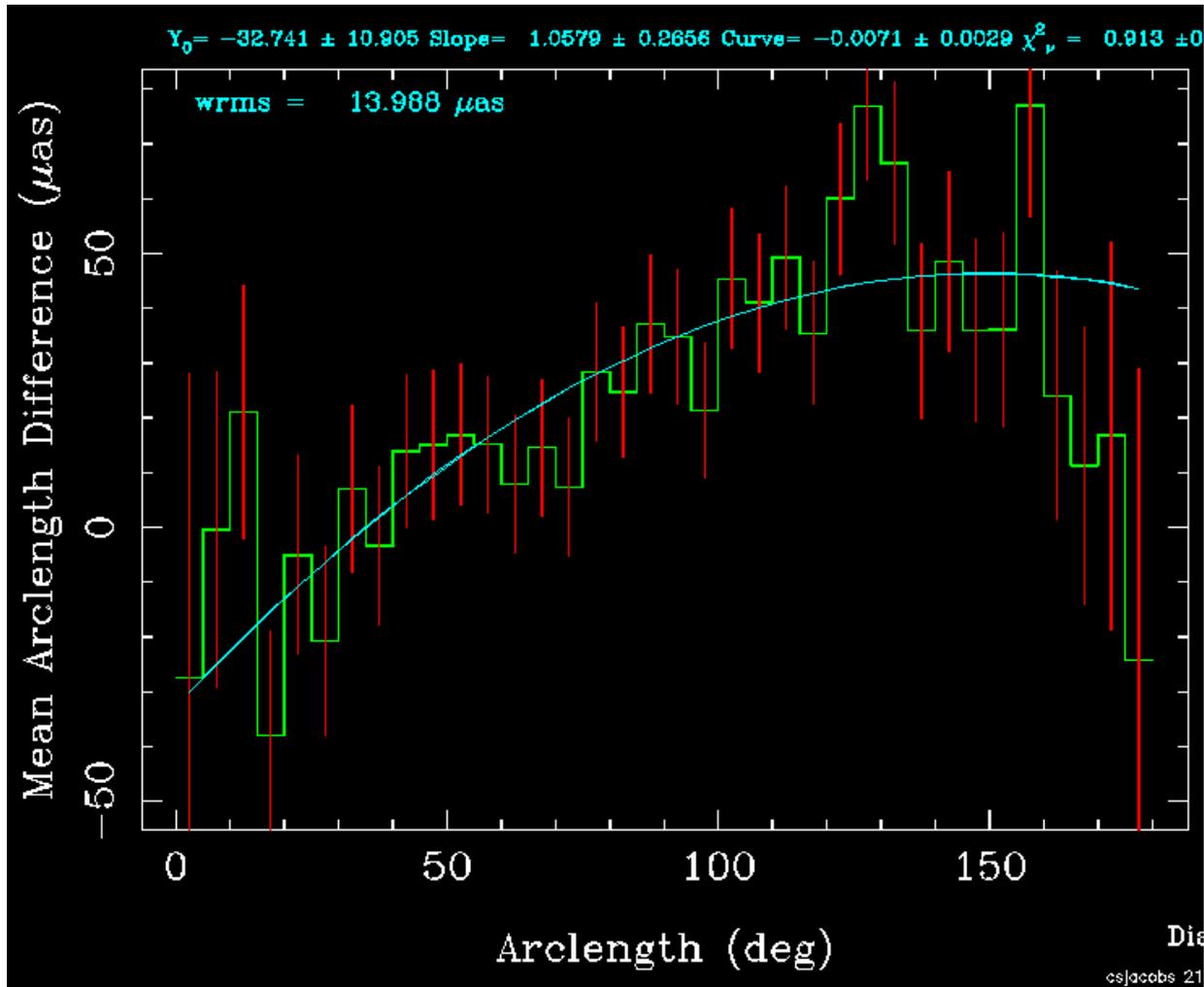


wRMS Ra and Dec differences about  $400 \mu\text{as}$  (2 nrad)  
Normalized differences are about 1.1 indicating realistic errors

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. K VLBI

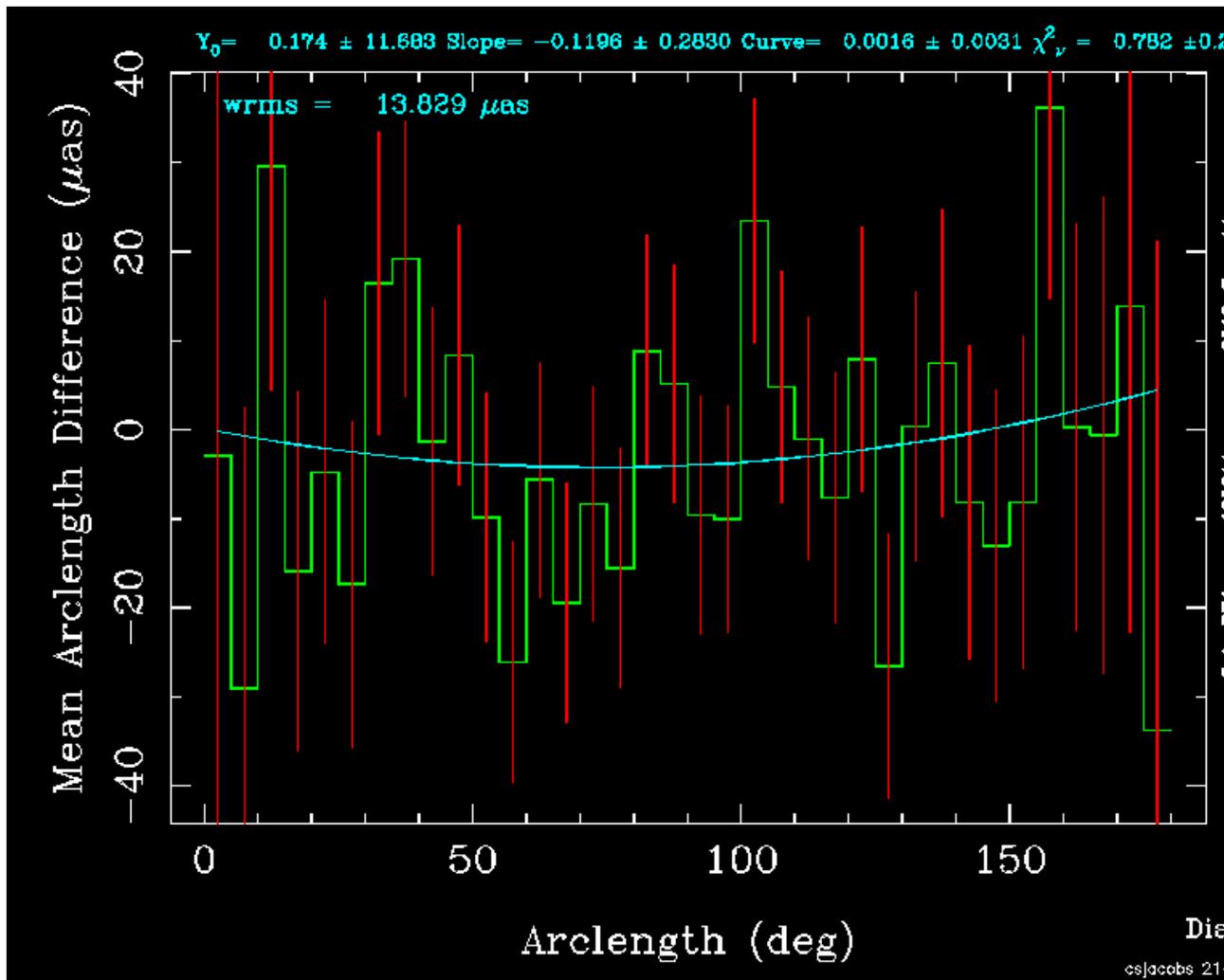


Arc differences vs. arclength bins show distortion at 50  $\mu\text{s}$  level

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI

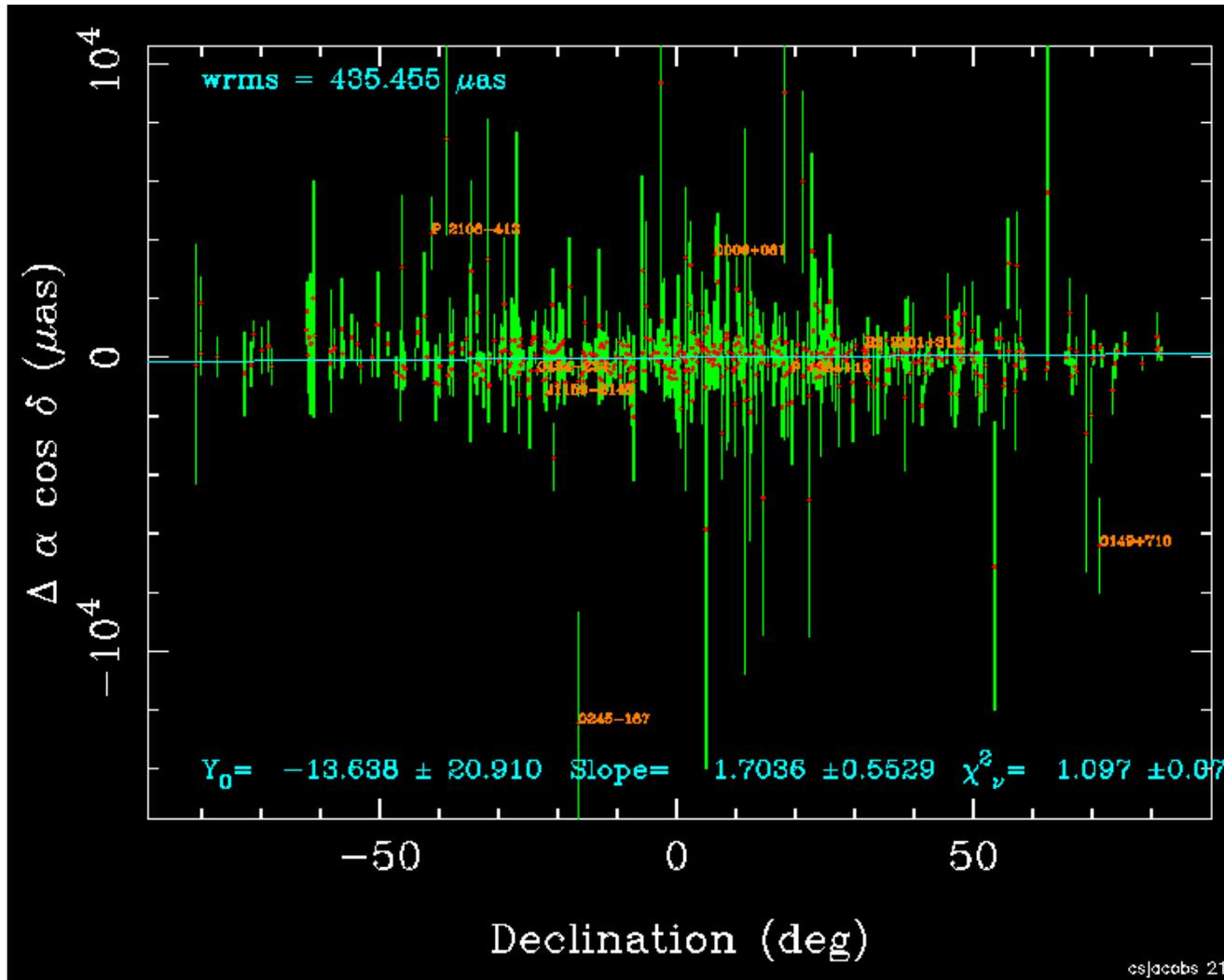


Arc differences steady vs. arclength bins at 15  $\mu\text{as}$  level

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. K VLBI

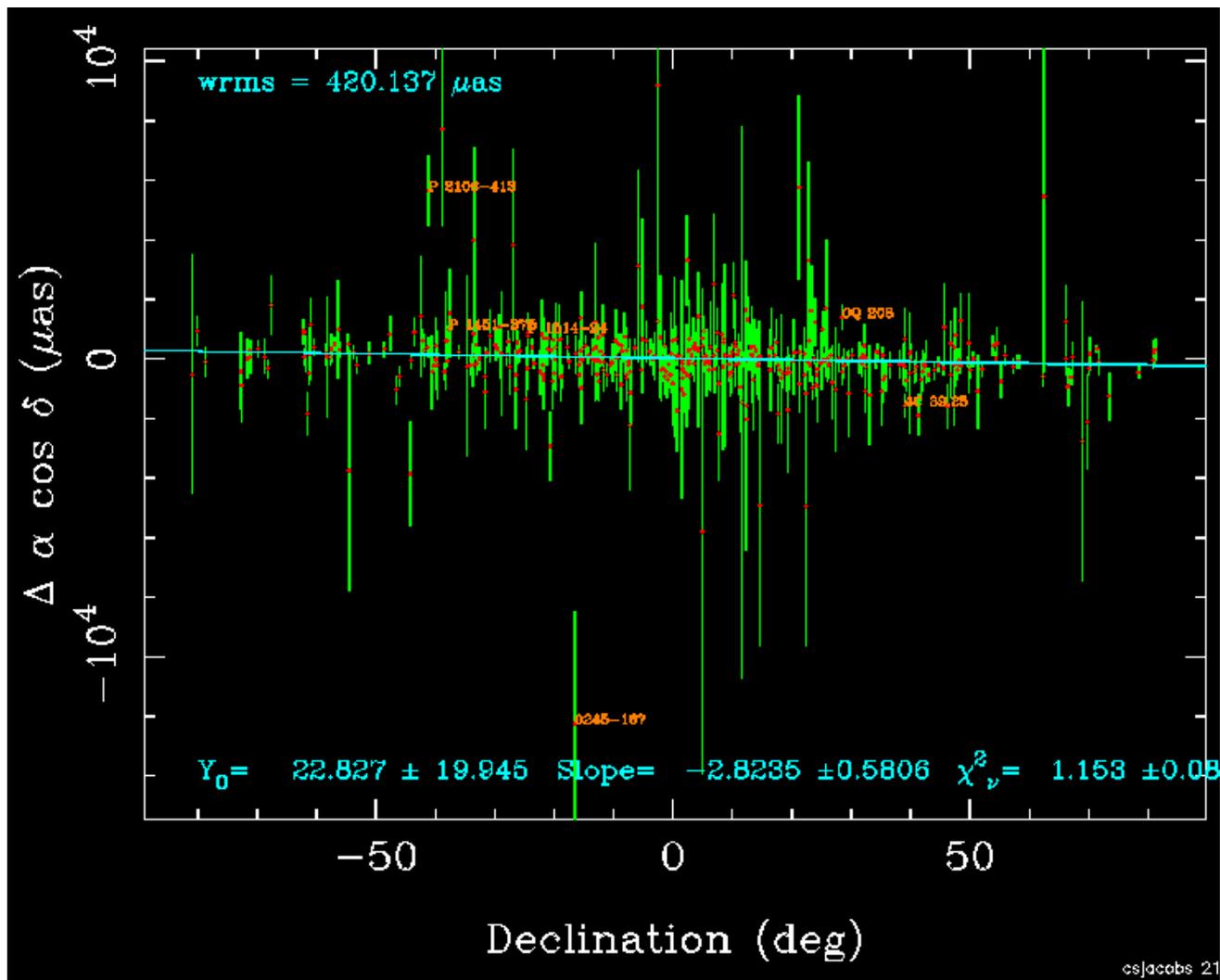


Systematic tilt:  $\Delta\alpha$  vs.  $\delta$  has 3 sigma slope of  $1.7 \pm 0.6 \mu as/deg$

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI



Systematic tilt:  $\Delta\alpha$  vs.  $\delta$  has 4.9 sigma slope of  $-2.8 \pm 0.6 \mu\text{as}/\text{deg}$

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. VLBI

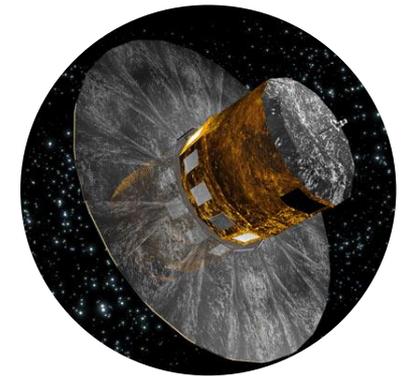
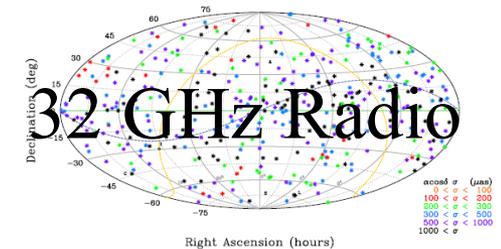
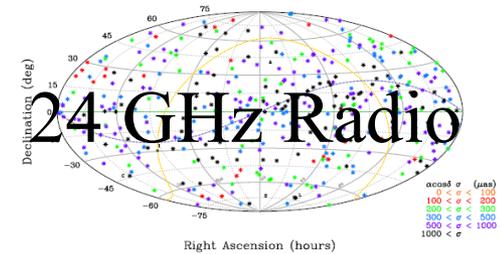
	SX-band 8 GHz 3.6cm	K-band 24 GHz 1.2 cm	XKa-band 32 GHz 0.9 cm
# sources	1984	481	413
# outliers $> 5\sigma$	106	13	7
% outliers	5.0 %	2.6 %	1.7 %
$\alpha$ wRMS	536 $\mu$ as	439 $\mu$ as	434 $\mu$ as
$\delta$ wRMS	544 $\mu$ as	455 $\mu$ as	423 $\mu$ as
$R_x$	32 +- 13	100 +- 24	56 +- 24
$R_y$	5 +- 11	-7 +- 21	32 +- 21
$R_z$	28 +-13	0 +- 23	15 +- 24

Hints that results improve by going to higher radio frequency  
However, the above results do not use exact same objects



# Summary: Tying Optical & Radio

- **Goal:** Tie of optical and radio celestial frames for deep space navigation and astronomical applications.
- **Roadmap:**
  - Preliminary optical & radio data are in-hand.
  - Increase number of sources in common between optical and radio
  - Expect to be limited by systematic calibration errors
  - Quantify and reducing systematics by
    - getting data in three radio bands (8, 24, 32 GHz)
    - Compare independent analysis chains
    - Image sources in radio to quantify non-pointlike structure
- **Preliminary results: Gaia DR1-aux vs. VLBI**
  - Excellent 3-D tie precision of  $\sim 20 \mu\text{as}$ .
  - Accuracy limited by systematic errors at 200 – 500  $\mu\text{as}$ .
  - Hints that 24 and 32 GHz VLBI are cleaner than 8 GHz
  - Lower percentage outliers, smaller scatter vs Gaia
  - Control of VLBI systematics will require increased southern observations.



**BACKUP**

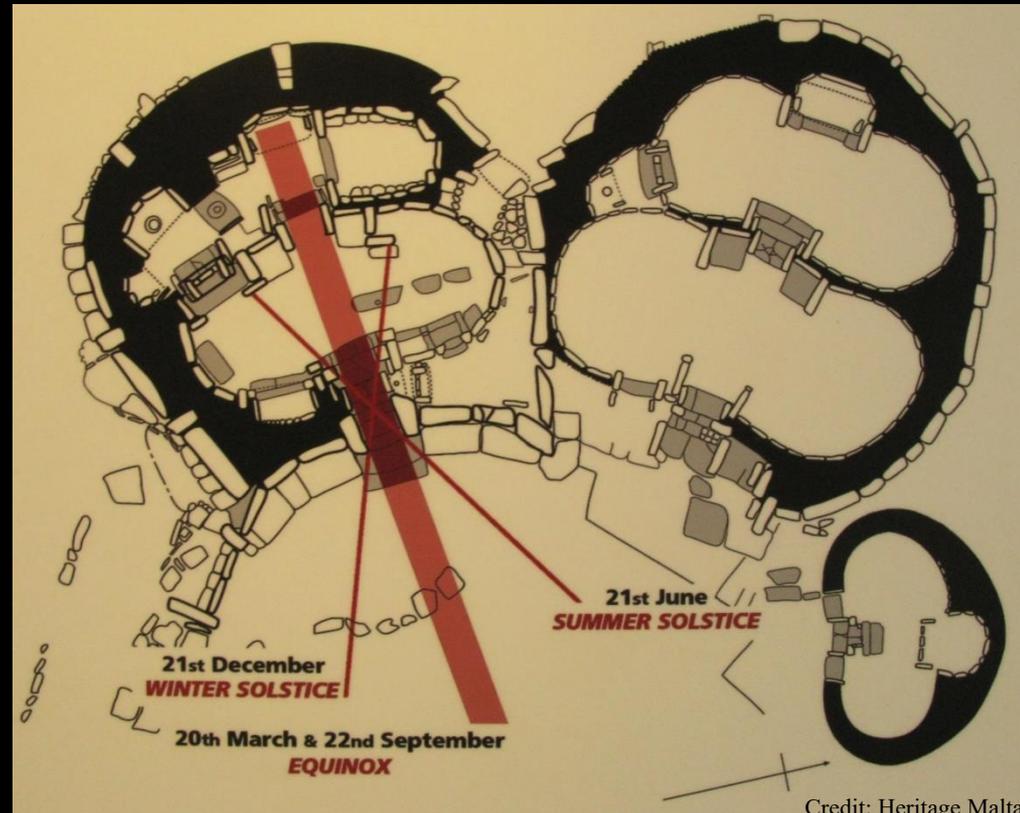
# Astrometry: measures positions in the sky, 5000+ years history!

Credit: Heritage Malta

Island of Malta  
Ggantija ~3500 B.C.  
Mnajdra ~3200 B.C.



Mnajdra solar alignments



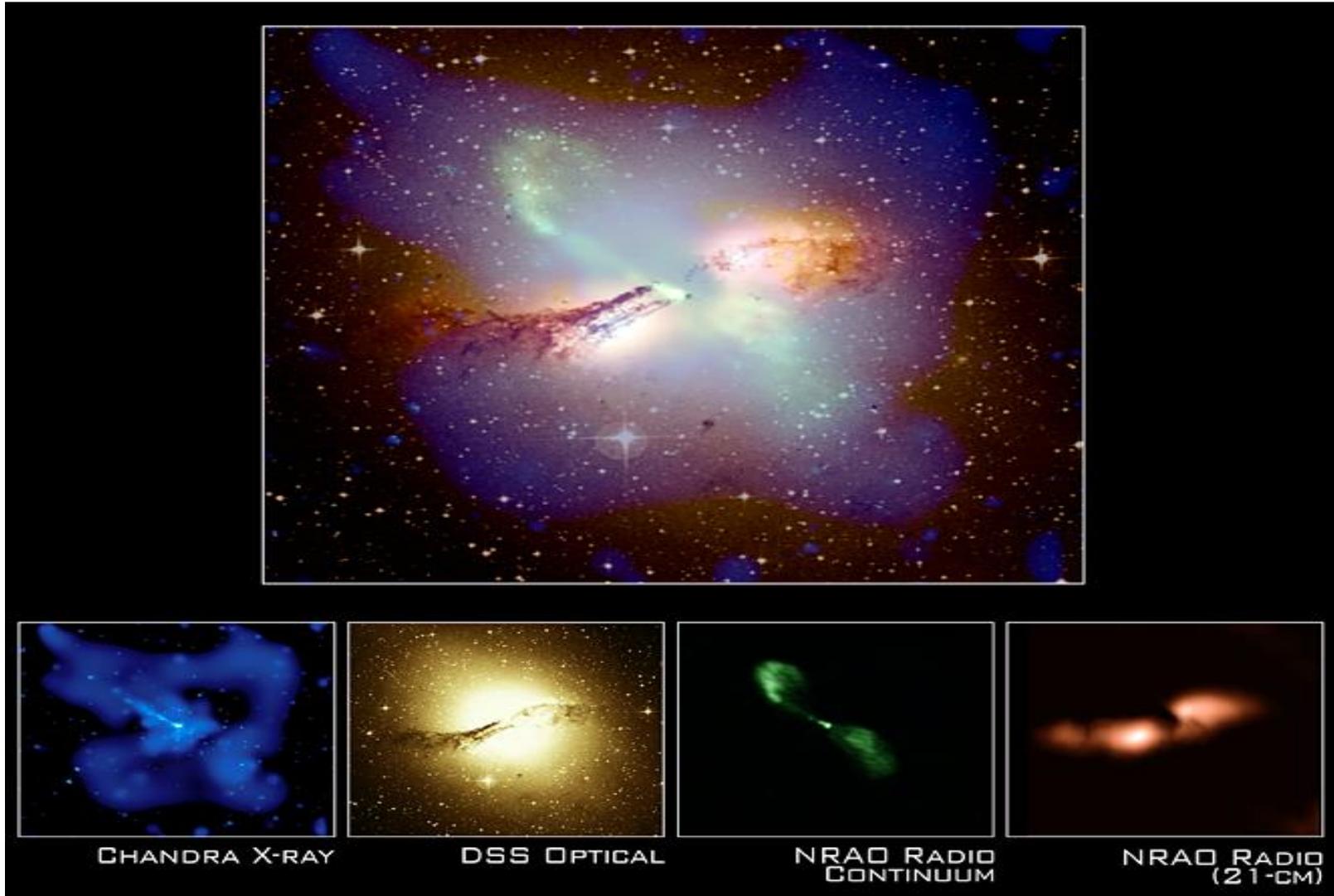
Credit: Heritage Malta

Mnajdra,  
Malta

©2011 C.S. Jacobs, used by permission

# The Source Objects

# Example Extragalactic Source: Centaurus-A in X-ray, Optical, Radio



Credits: X-ray (NASA/CXC/M. Karovska et al.); Radio 21-cm image (NRAO/VLA/Schiminovich, et al.),  
Radio continuum image (NRAO/VLA/J.Condon et al.); Optical (Digitized Sky Survey U.K. Schmidt Image/STScI)

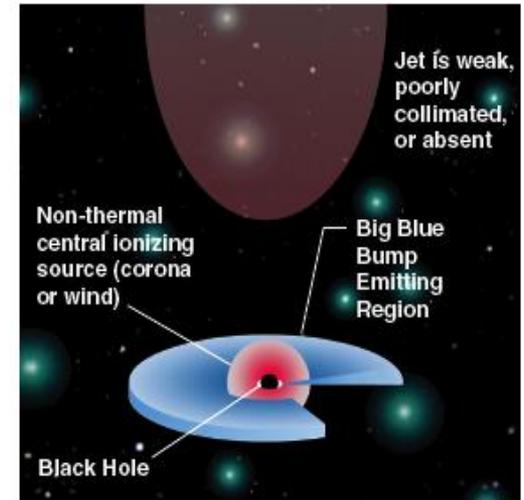


# Optical vs. Radio positions

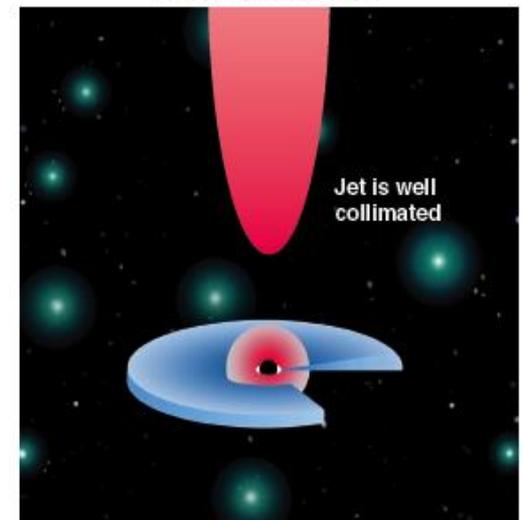
Positions differences from:

- Astrophysics of emission centroids
  - radio: synchrotron from jet
  - optical: synchrotron from jet?  
non-thermal ionization from corona?  
big blue bump from accretion disk?
- Instrumental errors both radio & optical
- Analysis errors

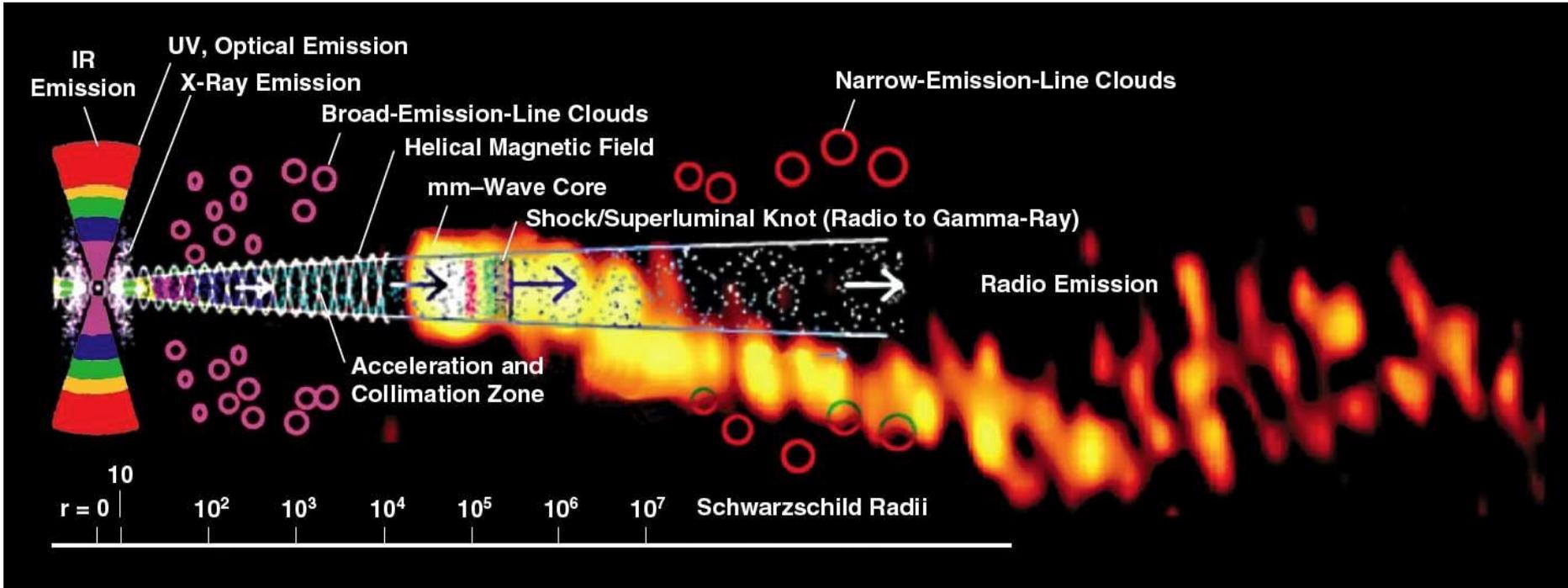
Radio-quiet Quasar



Radio-loud Quasar



# Active Galactic Nuclei (*Marscher*)



$R \sim 0.1-1 \mu\text{as}$

1mas

Features of AGN: *Note the Logarithmic length scale.*

“Shock waves are frequency stratified, with highest synchrotron frequencies emitted only close to the shock front where electrons are energized. The part of the jet interior to the mm-wave core is opaque at cm wavelengths. At this point, it is not clear whether substantial emission occurs between the base of the jet and the mm-wave core.”

*Credits: Alan Marscher, 'Relativistic Jets in Active Galactic Nuclei and their relationship to the Central Engine,' Proc. of Science, VI Microquasar Workshop: Microquasars & Beyond, Societa del Casino, Como, Italy, 18-22 Sep 2006. Overlay (not to scale): 3 mm radio image of the blazar 3C454.3 (Krichbaum et al. 1999)*