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# WFIRST Coronagraph Simulations and Performance Estimates

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# Outline



- I. Overview of the noise sources and their relation to planet yield
- II. Sample results on known RV planets
- III. Choosing a reference case for requirements
- IV. Initial look at sensitivities to key parameters



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# CALCULATING PLANET YIELD

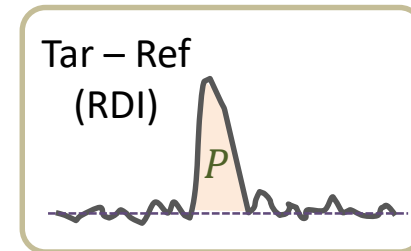
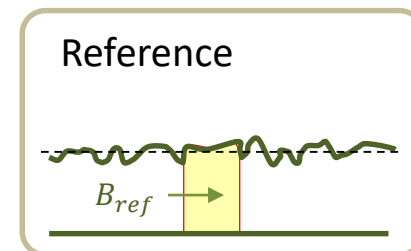
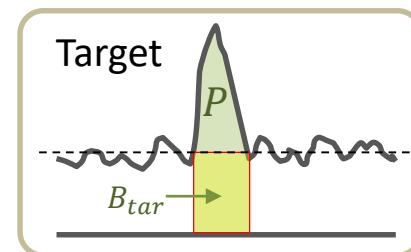
# A Simple Observing Scenario for Yield

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- We seek a simple analytical model of planet yield, via calculating the time to reach a desired SNR
- We need to be explicit about the observing assumptions
- We choose these assumptions:
  1. We are after a **photometric measurement**
    - Though note that in *detection*, we would not be doing photometry. The SNR is different in that case.
  2. We are doing **differential imaging**.
    - The SNR is the post-differential imaging SNR.
    - For simplicity we assume we are doing **Reference Differential Imaging (RDI)**.
  3. The reference star is brighter than the target star
    - If  $\Delta M > 3$  between target and reference then  $B_T > 16 B_R$
    - Shot noise of reference speckles is small compared with shot noise of target speckles
    - There is a normalization step also
  4. Exo-zodi is smooth and extended for both stars
    - Brightness distribution structures are  $\gg \lambda m/D$



$$\begin{aligned}
 Sig &= I_{tar} - I_{ref} \\
 &= (P + B_{tar}) - B_{ref} \\
 &= P + (B_{tar} - B_{ref})
 \end{aligned}$$

# Aside: Distinguishing types of SNR

Detection and spectroscopy are different statistical questions.

- For **spectrometry**, with the IFS, we are interested in the **photometric SNR**:

$$S_{phot} = \frac{\overset{\text{planet signal}}{P}}{\underset{\text{background}}{\sqrt{P + B}}}$$

- For planet **detection**, with the imager, we would be interested in **detection SNR**:

$$S_{detec} = \frac{P}{\sqrt{B}}$$

- The noise of interest in this case does *not* include the signal's shot noise
- We are instead interested in the background's false positive probability



# Analytical Expression for SNR

- Photometric SNR means we include planet shot noise
  - Keep in mind that we are considering the post speckle-subtraction SNR

$$SNR \equiv S = \frac{P}{\sigma_{tot}}$$

$$P = r_{pl} t \quad \text{planet signal}$$

- We write the total noise as:

$$\sigma_{tot}^2 = \sigma_r^2 + \sigma_s^2$$

random, uncorrelated, reduces with  $t$ 
Speckle subtraction error, excludes meas. noise

- The uncorrelated, random noise is given by:

$$\frac{\sigma_r^2}{t} = r_n = f_{SR} F^2 \left[ \underbrace{\Phi_* C_{pl} \tau_{pl} + \Phi_* C_{CG} I_{pk} m_{pix} \tau_{sp} + \left( \frac{d\Phi_Z}{d\Omega} \Delta\Omega_{PSF} \right) \tau_Z}_{\text{photonic (shot noise) terms}} \right] A_{PM} \eta + F^2 \left[ \underbrace{i_d m_{pix} + q_{CIC} \frac{m_{pix}}{t_{fr}} + \frac{m_{pix}}{t_{fr}} \left( \frac{\sigma_{rd}}{G_{EM}} \right)^2}_{\text{electronic terms}} \right]$$

planet      speckle      zodi
dark      clk. Ind. Chg.      read noise

$f_{SR} \equiv$  fraction of core light in region of interest for SNR

$F \equiv$  EMCCD excess noise factor  $\sim \sqrt{2}$

$\Phi_* = F_\lambda \cdot \Delta\lambda$

$\Phi_Z = F_\lambda^Z \cdot \Delta\lambda$

Note: This is the post-subtraction error, and should in principle reflect noise contributions for both the *target* and *reference* images. However, consistent with our assumption that the reference is significantly brighter than the target, we consider the error being dominated by the target star image only.

# Looking a little more closely at $\sigma_s$

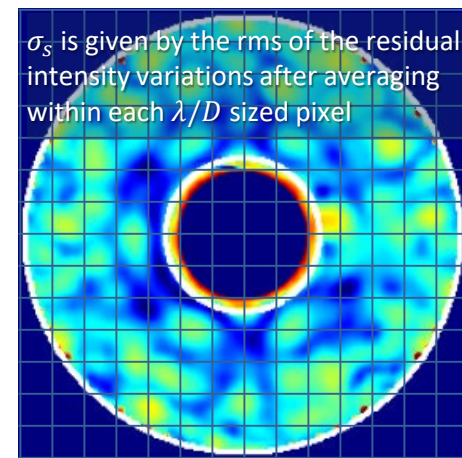
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- The speckle subtraction term  $\sigma_s$  contains **only** the speckle instability effects.
  - Excludes noise in the subtracted images, and corresponds to the post processing error
- For a given level of speckle instability, different post processing schemes (e.g. PCA, KLIP) will have different dependencies on prior data.
- But, in the context of a *single observation*, taking a total integration time  $t$ , this error *grows at the same rate as the signal*, i.e.,  $\sigma_s = k t$
- A useful version of this parameterization defines a post-processing improvement factor, which can depend on many variables unstated here, that is calculated from the residual speckle scene according to:

$$f_{pp} \equiv \frac{\sigma_s}{r_{sp} t}$$

$r_{sp} \equiv$  mean raw speckle rate

residual speckle, excluding shot noise;  
 $\lambda/D$  spaced grid superimposed on top



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- NB: The above definition shows how  $f_{pp}$  is measured, *not its dependencies!*
- From this definition, we have:  $\sigma_s = f_{pp} r_{sp} t$

# Putting it all together: time to reach SNR

Analytical expression for SNR:

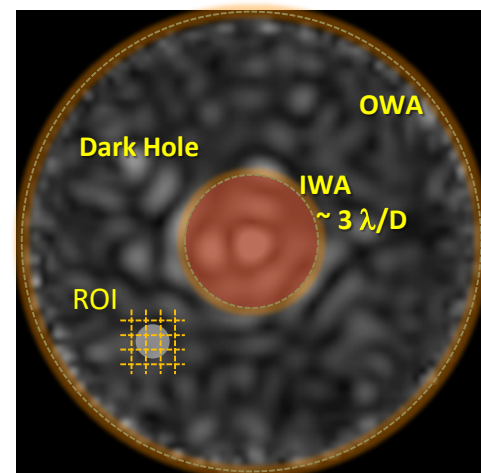
$$S = \frac{\overset{\text{planet rate}}{r_{pl} t}}{\underset{\text{noise rate}}{\sqrt{r_n t + \sigma_s^2}}}$$

Speckle Subtraction Error:

$$\sigma_s = \underset{\text{mean speckle rate}}{f_{pp} r_{sp} t}$$

Time to reach desired SNR:

$$t = \frac{S^2 r_n}{r_{pl}^2 - S^2 f_{pp}^2 r_{sp}^2}$$







# Estimated Integration Times, Imaging 2

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Imaging 2 in order of increasing integration time										
Rank	S/N	Planet		Vmag	WA		Hrs	Days	Cum Days	
1	1	beta Gem b	1	1.15	1	3.45	1	0.02	0.00	0.00
2	5	upsilon And d	5	4.1	5	3.81	5	0.75	0.03	0.03
3	9	47 UMa c	9	5.03	9	5.17	9	0.88	0.04	0.07
4	6	epsilon Eri b	6	3.72	6	9.30	6	1.28	0.05	0.12
5	7	47 UMa b	7	5.03	7	3.04	7	1.57	0.07	0.19
6	2	gamma Cep b	2	3.21	2	2.85	2	1.61	0.07	0.26
7	13	Gliese 777 b	13	5.73	13	5.09	13	3.41	0.14	0.40
8	11	HD 114613 b	11	4.85	11	5.23	11	4.18	0.17	0.57
9	14	mu Ara e	14	5.12	14	7.00	14	4.20	0.17	0.75
10	33	psi Dra B b	33	5.81	33	4.09	33	6.49	0.27	1.02
11	15	14 Her b	15	6.61	15	3.40	15	14.08	0.59	1.60
12	19	HD 217107 c	19	6.17	19	5.46	19	19.84	0.83	2.43
13	4	HD 192310 c	4	5.73	4	2.70	4	20.62	0.86	3.29
14	20	HD 154345 b	20	6.76	20	4.61	20	25.58	1.07	4.35
15	22	HD 134987 c	22	6.47	22	4.52	22	60.91	2.54	6.89
16	31	HD 142 c	31	5.7	31	6.71	31	63.40	2.64	9.53
17	17	55 Cnc d	17	5.96	17	9.02	17	74.83	3.12	12.65
18	10	HD 39091 b	10	5.65	10	3.72	10	76.97	3.21	15.86
19	23	HD 87883 b	23	7.57	23	4.00	23	411.15	17.13	32.99
20	29	GJ 832 b	29	8.66	29	9.30	29	4019.91	167.50	200.49

565 nm, 10% BW

SCENARIO PARAMETER SELECTIONS	
Observation Mode	Img 2comp
SNR Target	5
Detector Type	PC EMCCD
Coronagraph Type	HLC
RV System	2
Frame Time	30
Post-proc Factor	3.3%
Planet phase angle	65
Exo-Zodi Set	1
Contrast Floor	2E-09



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# OPTIMIZING PLANET YIELD



# The Goal In Optimization

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- We could frame the discussion as:
  - A. Want to maximize planet yield**
  - B. Want to minimize planet equivalent contrast**
- Option A:
  1. Set a maximum total time, then add up all the easiest planets until the time is exhausted. Report the number of planets.
  2. Proxy: minimize the time-to-SNR for the dimmest viable planets (total time is dominated by the dimmest planet)
- Option B:
  - Used in the error budget (a.k.a. contrast sensitivity budget):
  - Define a nominal case, e.g. dimmest viable planet; report smallest planet flux ratio that can be observed in given time  $t_0$

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# Noise Equivalent Contrast (NEC): $\xi_{eq}$

- What is the minimum planet contrast that can be seen with  $SNR \geq 5$  under our observing scenario?
- Equivalent Contrast Definition:
  - The planet that will be detected with SNR of  $S$  after integrating for time  $t$  is one which has a planet-contrast equal to the  $S$ - $\sigma$  equivalent contrast, after post processing:

Planet signal in the core region after  $t$  seconds

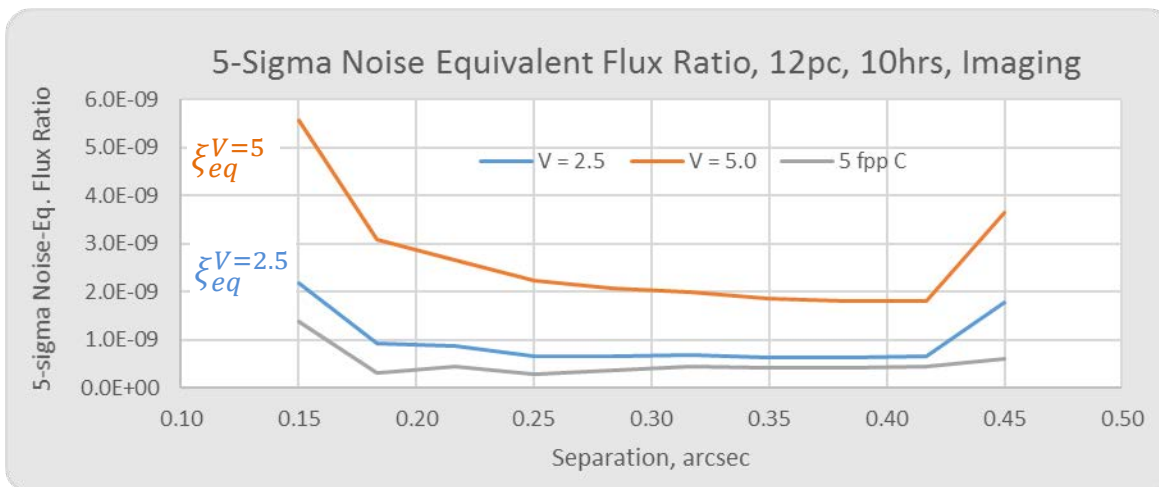
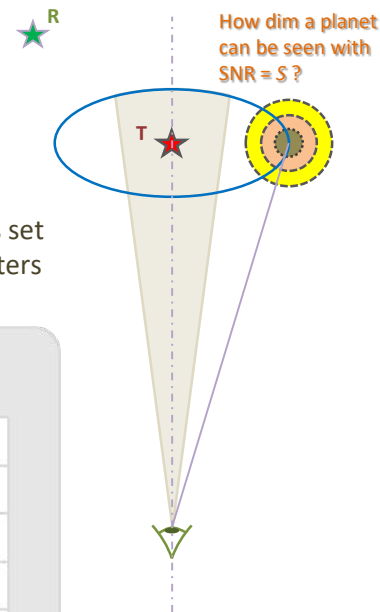
$$f_{SR} \cdot \Phi_* \xi_{eq} A \tau_{pl} \eta t = S \cdot \sigma_{tot}$$

signal fraction      area      QE  
flux      thruput time

$$\xi_{eq} = \kappa \cdot \sigma_{tot}$$

$$\kappa \equiv \frac{S}{f_{SR} \Phi_* A \tau_{pl} \eta t}$$

This conversion factor is set by the scenario parameters



# Asymptotic Behavior of $\xi_{eq}$

- How does the NEC depend on post processing and integration time?
- For imaging,  $f_{SR} = 1$ , so for simplicity we drop this factor, and we have:

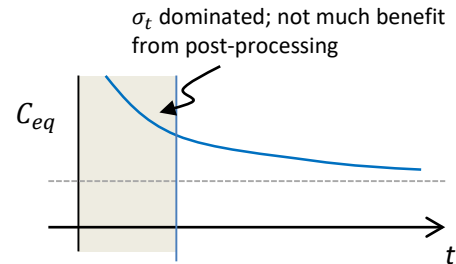
Our definitions of NEC:

$$\Phi_* \xi_{eq} A \tau_{pl} \eta t = S \underbrace{\sqrt{r_n t + f_{pp}^2 r_{sp}^2 t^2}}_{\sigma_{tot}}$$

$$\xi_{eq} = S \sqrt{\frac{r_n}{\Phi_*^2 A^2 \tau_{pl}^2 \eta^2 t} + f_{pp}^2 \frac{C_{CG}^2 I_{pk}^2 m_{pix}^2}{\tau_{core}^2}}$$



- For very short times the first term dominates and there is no benefit from post-processing



- At large times, the first term under the radical drops out, so that we arrive at:

$$\xi_{eq} \xrightarrow{t \rightarrow \infty} S f_{pp}(t) \frac{C_{CG} I_{pk} m_{pix}}{\tau_{core}}$$

# Which System to Evaluate On?

- The sensitivity is most important on the hardest viable target
- Consider a realistic IFS case, and compare integration time
- Comparison suggests
  - HD 190360 b
  - aka **Gliese 777 b** (easier to remember?)

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Observation Mode	IFS 1comp		
SNR Target	15		
Detector Type	PC EMCCD		
Coronagraph Type	SPC	mag	Star
RV System	1	1.15	HD62509
Frame Time	30	s	single frame
Post-proc Factor	7.0%	f_pp	resid. speckle str.
Planet phase angle	45	deg	not used
Exo-Zodi Set	1	1 or 0	multiplies exoZodi
Contrast Floor	2E-09	5E-09	knowledge errors

IFS 1 in order of increasing integration time							
Rank	No.	Planet	Vmag	WA	Hrs	Days	Cum Days
		Gliese 7	30	30	30	30	0.00
1	1	beta Gem b	1.15	2.95	1.58	0.07	0.07
2	9	47 UMa c	5.03	4.42	29.00	1.21	1.27
3	5	upsilon And d	4.1	3.26	138.34	5.76	7.04
4	13	Gliese 777 b	5.73	4.36	126.29	5.26	12.30
5	33	psi Dra B b	5.81	3.50	660.63	27.53	39.83
6	11	HD 114613 b	4.85	4.47	707.62	29.48	69.31
7	20	HD 154345 b	6.76	3.95	1382.64	57.61	126.92
8	19	HD 217107 c	6.17	4.68	1625.24	67.72	194.64

Detector and IFS Design Settings			
<b>Detector Architecture</b>			
Item	Value	Units	Comments
Dark current	3E-05	e/pix/s	Leon Harding, 10/6/2016
Clock Ind. Charge	2E-03	e/pix/fr	Leon Harding, 10/6/2016
Read noise	0	e	eff. Read noise below
EMgain	1000	X	0
Quantum Eff.	74%	QE	Includes Ph. Ctg. Eff. Loss
Pixel Size	13	μm	
f SR	0.111		frac. Of core light in SNR ROI
Desired mpix	16.0		pixels in SNR ROI
Excess Noise Fac.	1.00	ENF	
Frame Rate	0.0333	Hz	Wes used 300s
<b>Focal Plane Architecture</b>			
Imager Critical λ	450	nm	Nyquist sampled
Imager Sampling	0.341	(λ/D) / pix	
IFS Critical λ	660	nm	Nyquist sampled
IFS Lensl per PSF	2	lenslets	across PSF core
IFS Spatial Samp	2	rows	pixels in spatial dir.
IFS Spectral Samp	2	cols	pixels / spect. Elem.
IFS sampling on sky	0.029	arcsec	/ lenslet @ crit. λ
		10.5mas	
<b>Rates of signal and background into the SNR region of interest</b>			
<b>Stellar Flux</b>			
Item	Value	Units	Comments
Local Zodi	22	mag/as^2	brightness density
Exo Zodi	23	mag/as^2	brightness density



# What are the dominant errors for Gliese 777 b?

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SCENARIO PARAMETER SELECTIONS			
Observation Mode	IFS 1comp		
SNR Target	15		
Detector Type	PC EMCCD		
Coronagraph Type	SPC	mag Star	
RV System	13	5.73	HD190360
Frame Time	30	s	single frame
Post-proc Factor	7.0%	f_pp	resid. speckle str.
Planet phase angle	45	deg	not used
Exo-Zodi Set	1	1 or 0	multiplies exoZodi
Raw Contrast Floor	2E-09	5E-09	knowledge errors

### Scene Signal and Background (per Frame)

Core electrons per frame			
Item	Value	Units	Comments
Planet Electrons	0.057	e-/fr	PSF core (photon)
Speckle Electrons	0.022	e-/fr	PSF core
Zodi Electrons	0.058	e-/fr	PSF core
Pixel electrons per frame			
Planet Electrons	0.0036	e-/fr	per pixel (in core)
Speckle Electrons	0.00	e-/fr	per pixel
Zodi Electrons	0.0	e-/fr	per pixel
Core electrons per frame			
Planet in Core	0.06	e-/fr	PSF core (elec.)
Speckle in Core	0.02	e-/fr	PSF core
Zodi in Core	0.1	e-/fr	PSF core

### Scene Rates (per second)

Core photons per second			
Item	Value	Units	Comments
Planet Phot Rate	2.57E-03	phot/s	PSF core (photon)
Speckle Phot Rate	1.0E-03	phot/s	PSF core

### Scenario Summary

Science Instrument	IFS		
Center lambda	6.60E-07	m	V-band ctr.
Bandwidth	18%	--	V-band is 16.18%
Spec Resolution	50	R	
Filter			
Item	Value	Units	Comments
WL Beginning	6.01E-07	m	Wavelength min
WL Ending	7.19E-07	m	Wavelength max
$\Delta\lambda$	1.00E-09	m	For calc. integral

### SNR

Time to SNR			
Item	Value	Units	Comments
Time Required to Reach SNR	4.55E+05	sec	This is integration time only
	126.290	hrs	
	5.262	days	

### Final SNR

Item	Value	Units	Comments
SNR Check	15.00	SNR	
Signal	868.9	e	Total Signal
Noise	57.9	e	Total Noise
Frames Needed	15,154.8	frames	for SNR target

### Final Noise Contributions

Item	Value	Units	Comments
Shot	29.477	e	signal shot noise
Speckle	18.442	e	<sp> shot noise
Zodi	29.608	e	zodi shot
Dark Current	14.773	e	
CIC	22.022	e	
Read	0.000	e	
Speckle Structure	23.808	e	residual Speckle

# Which Parameters to Investigate?

- Initial Set:

- $\tau_{core}$
- $C_{CG}$
- $\Delta\Omega_{PSF}$
- $q_{CIC}$
- $t_{fr}$
- $f_{pp}$

Final Noise Contributions			
Item	Value	Units	Comments
Shot	37.860	e	signal shot noise
Speckle	23.686	e	<sp> shot noise
Zodi	56.372	e	zodi shot
Dark Current	27.386	e	
CIC	40.824	e	
Read	0.000	e	
Speckle Structure	39.273	e	residual Speckle

Set to IFS1 Comp and planet = 13 (Gliese 777 b)						
	tau Core	C_CG	dOmega	qCIC	t_fr	fpp
nominal	3.64E-02	2.31E-09	5.23E-03	2.00E-03	3.00E+01	7.00E-02
nom + 10%	4.01E-02	2.54E-09	5.75E-03	2.20E-03	3.30E+01	7.70E-02
tNom	126.29	126.29	126.29	126.29	126.29	126.29
tDelta	103.96	133.70	130.30	128.50	124.30	131.90
delta tSNR	22.3	7.4	4.0	2.2	2.0	5.6
Sensitivity	177%	59%	32%	18%	16%	44%

Sensitivity is defined here as the ratio of fractional increase in tSNR over fractional change in the given parameter

NB: Another important attribute to consider is the inner working angle.

A study of inner working angle has to be done somewhat differently, since there we are looking for the number of additional planets available as IWA becomes smaller.







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# BACKUP



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# Detector Pixels in the IFS Configuration

For the IFS, the SNR region of interest (ROI) comprises the collection of pixels that altogether are involved in the photometry of a *single spectral element*

The system is constant-dispersion, therefore the sampling in the spectral dimension is set, and not wavelength dependent. However, the spatial sampling does depend on wavelength.

$$m_{pix} = \left( N_{lens} \frac{\lambda_i}{\lambda_{min}} \right)^2 \cdot 2_{spec} \cdot N_{spat} \left( \frac{\lambda_i}{\lambda_{min}} \right)$$

neglect for realistic Wavefront errors

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