

# Insights into Vesta and Ceres internal structures from their topography

AGU 2017 meeting  
New Orleans, Louisiana,  
12 December 2017.

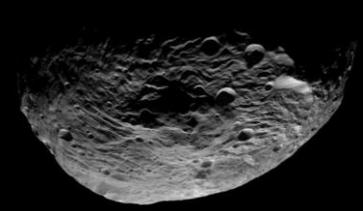
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C. T. Russell<sup>3</sup>, R. R. Fu<sup>4</sup>

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<sup>3</sup>University of California Los Angeles

<sup>4</sup>Department of Earth and Planetary Sciences, Harvard University.



## Goal of the talk:



- Explain how the internal structures of **Vesta** and **Ceres** diverged by looking at the present-day topography (and gravity) measured by **Dawn**



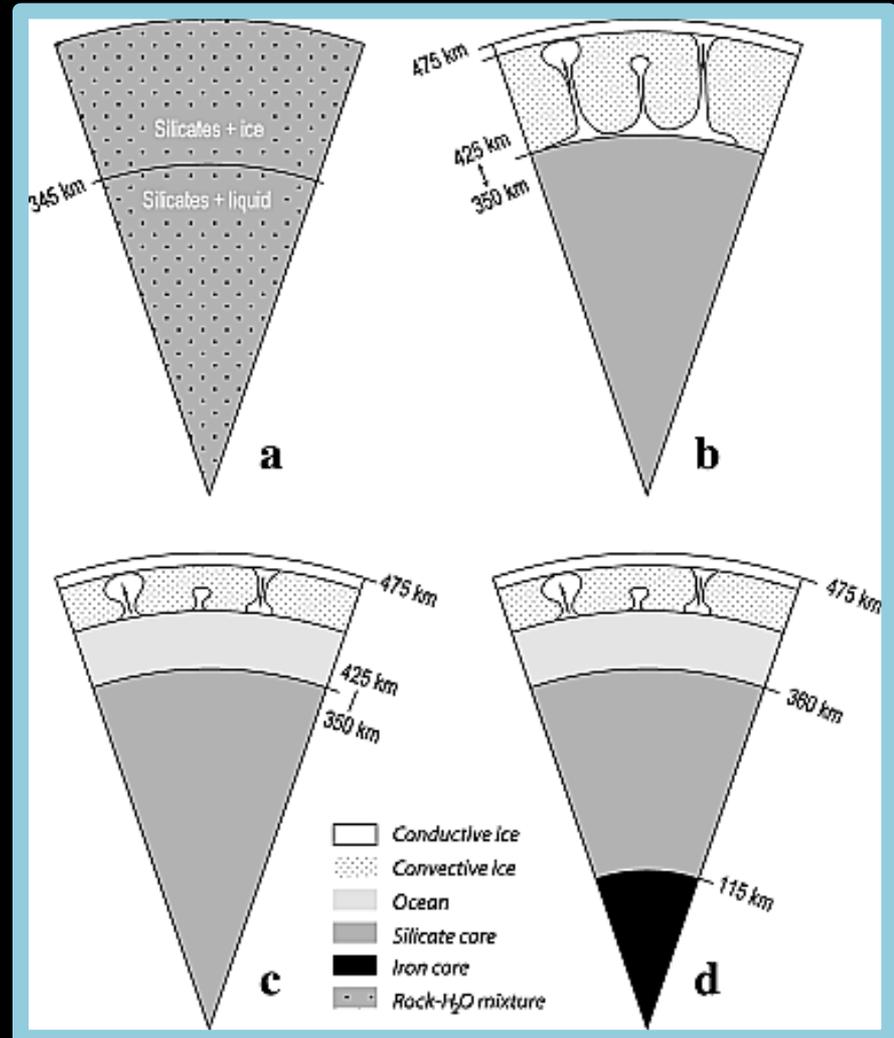
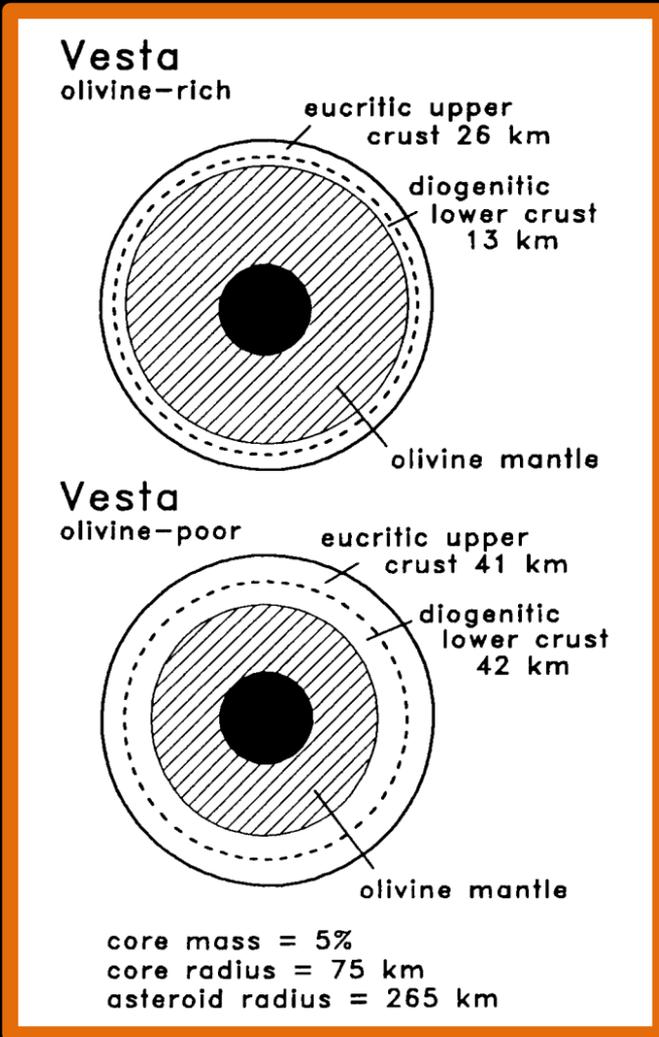
# How we use shape data to study interiors?

- **Hydrostatic equilibrium**
- **Isostatic compensation**
- **Viscous relaxation**

# What did we know before Dawn?

## Vesta

## Ceres



Ruzicka et al., 1997

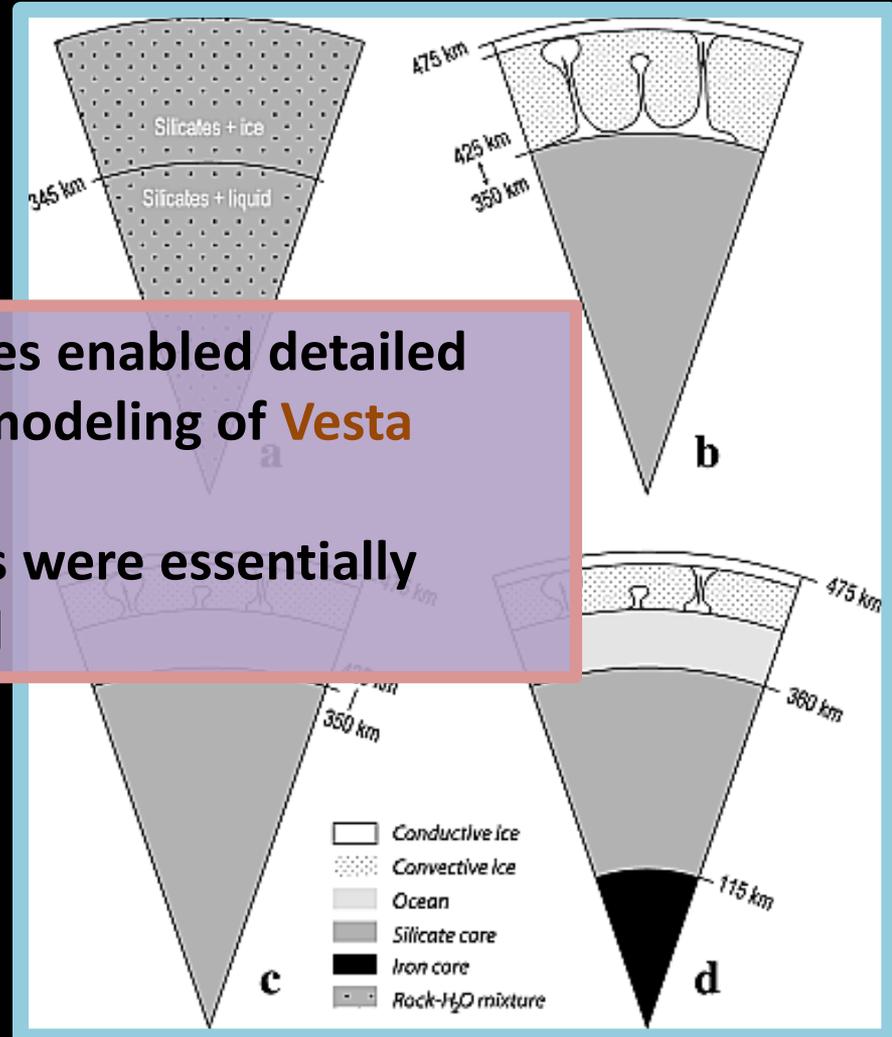
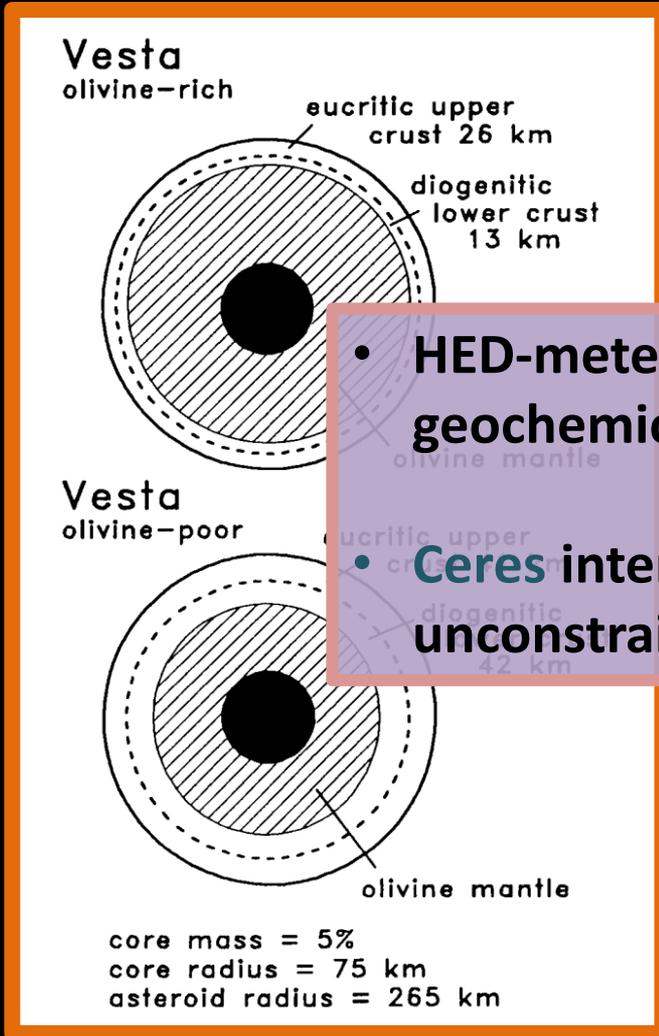
McCord and Sotin, 2005

Ermakov et al., Vesta and Ceres topography, AGU 2017.

# What did we know before Dawn?

## Vesta

## Ceres



- HED-meteorites enabled detailed geochemical modeling of **Vesta**
- **Ceres** interiors were essentially unconstrained

Ruzicka et al., 1997

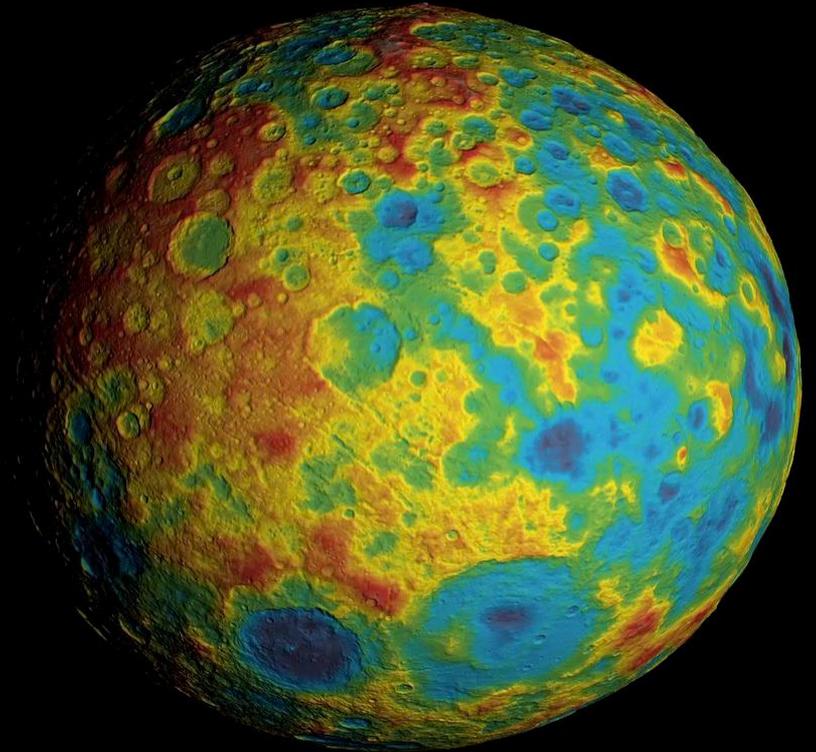
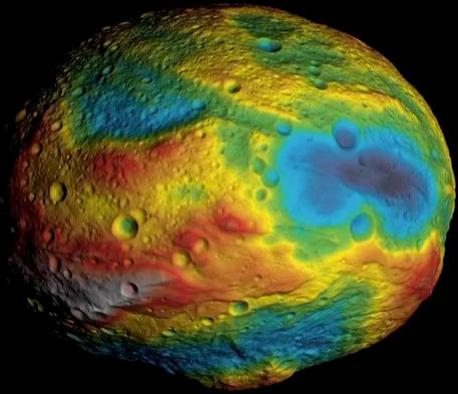
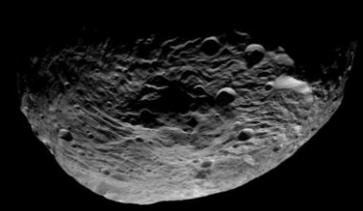
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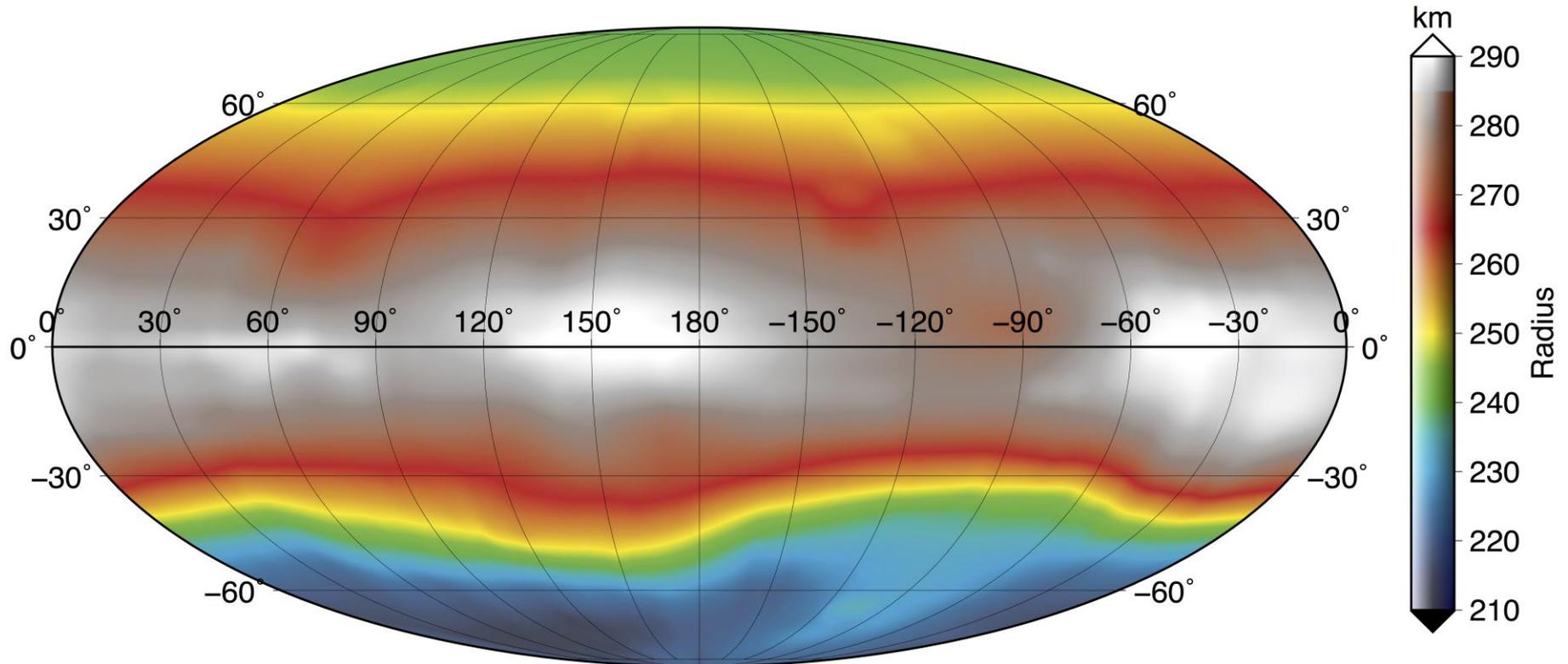
# Input for our modeling

- **Shape model**
  - **Stereophotogrammetry (SPG)**
  - **Stereophotoclinometry (SPC)**
  - **Mutually consistent with the accuracy much better than the spatial resolution of gravity field**
- **Gravity field**
  - **Accurate up to  $n = 18$  ( $\lambda=93$  km) for **Vesta** (Konopliv et al., 2014)**
  - **Accurate up to  $n = 17$  ( $\lambda=174$  km) for **Ceres** (Konopliv et al., 2017)**
- **Assumptions we have to make:**
  - **Multilayer model with uniform density layers**
  - **Range of core densities for **Vesta****
  - **Range of crustal densities from HEDs for **Vesta****
  - **Can't really assume anything for **Ceres****

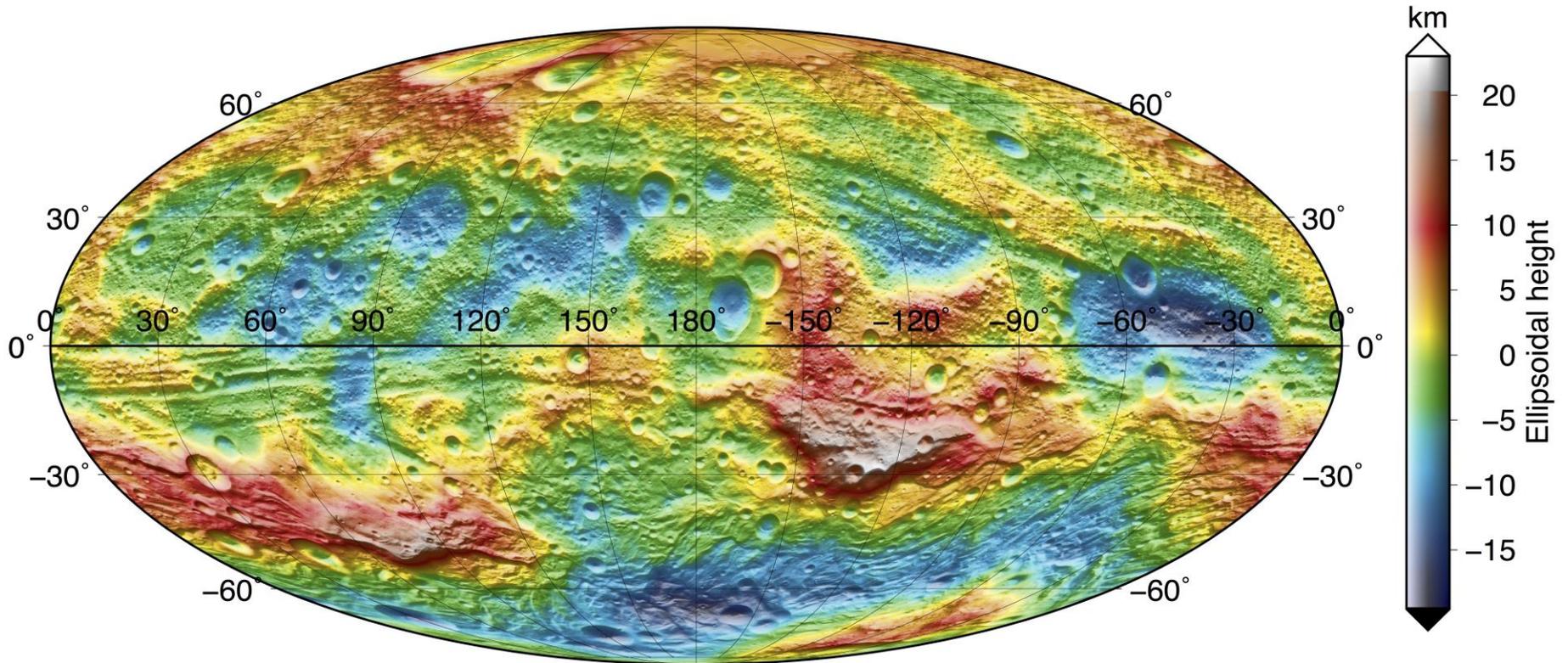
# Vesta and Ceres



# Vesta (Thomas et al, 1997)



# Vesta SPC

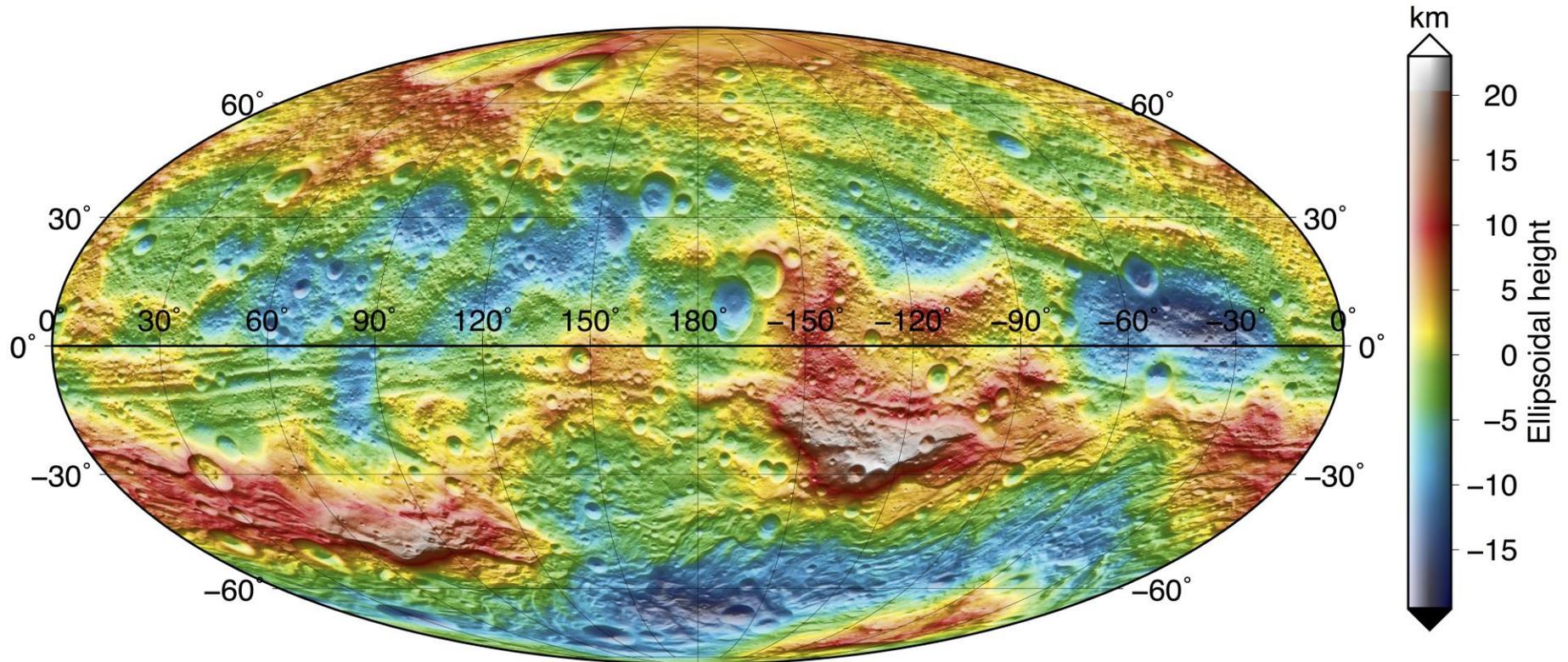


Reference ellipsoid:

$a = 280.9$  km

$c = 226.2$  km

# Vesta SPG

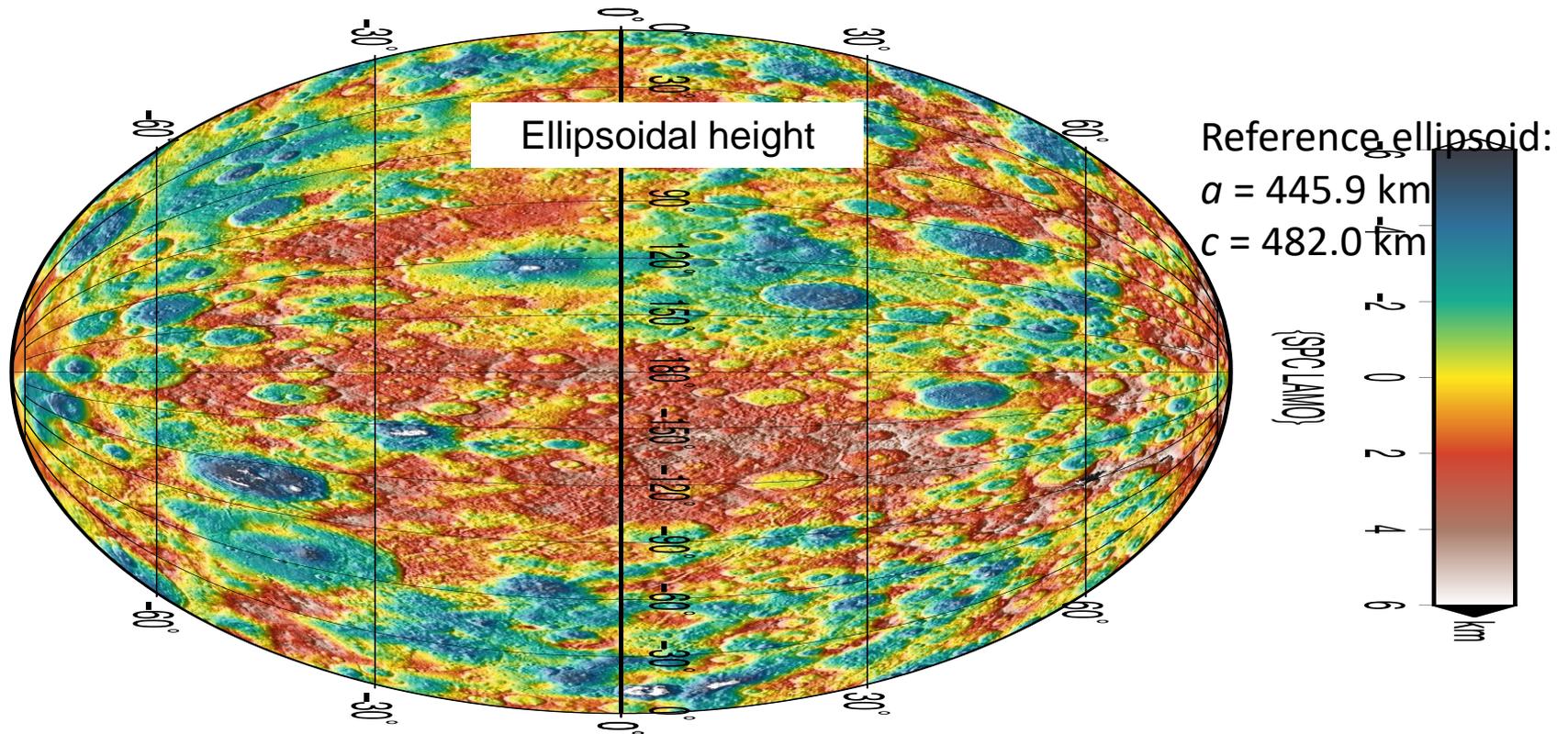


Reference ellipsoid:

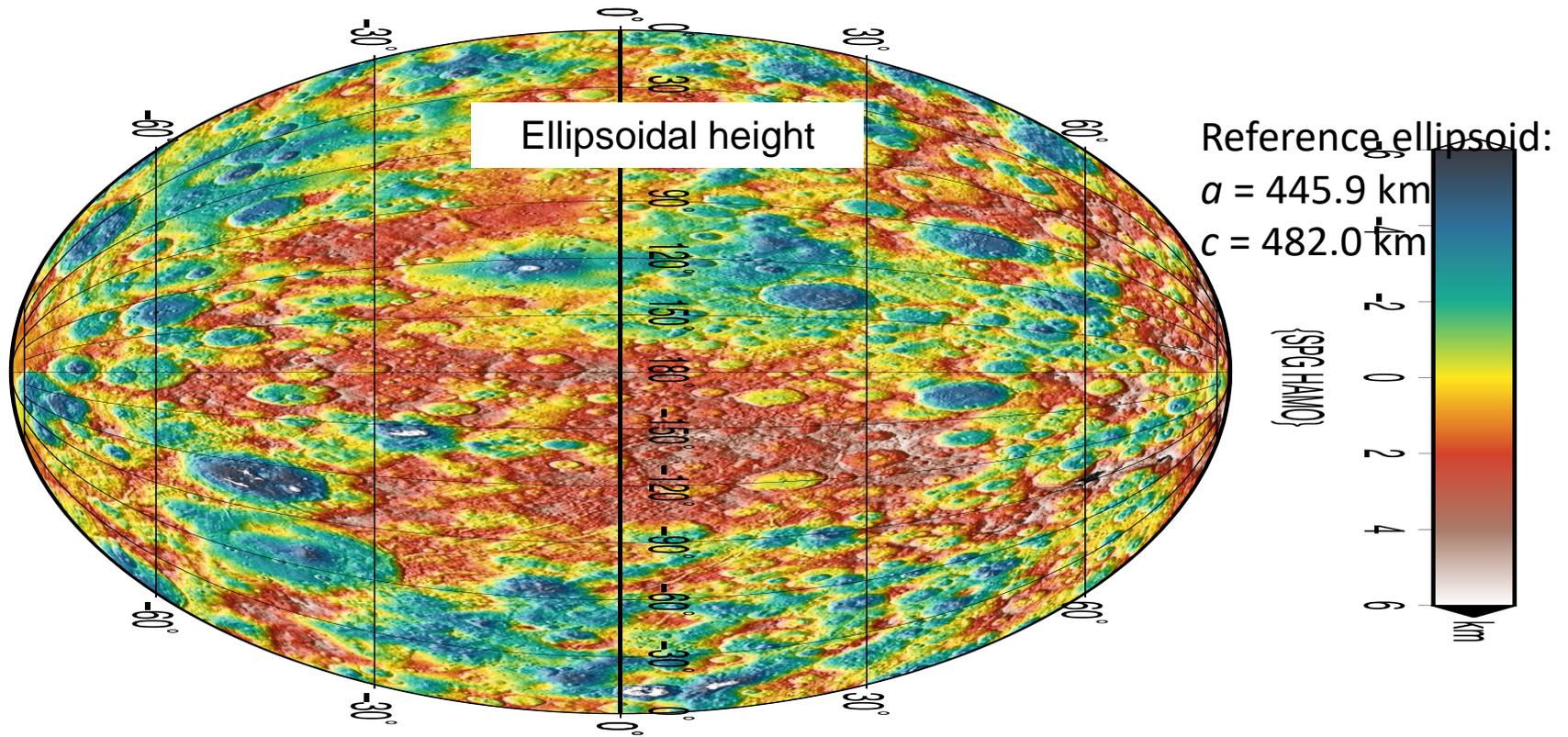
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# Ceres SPC



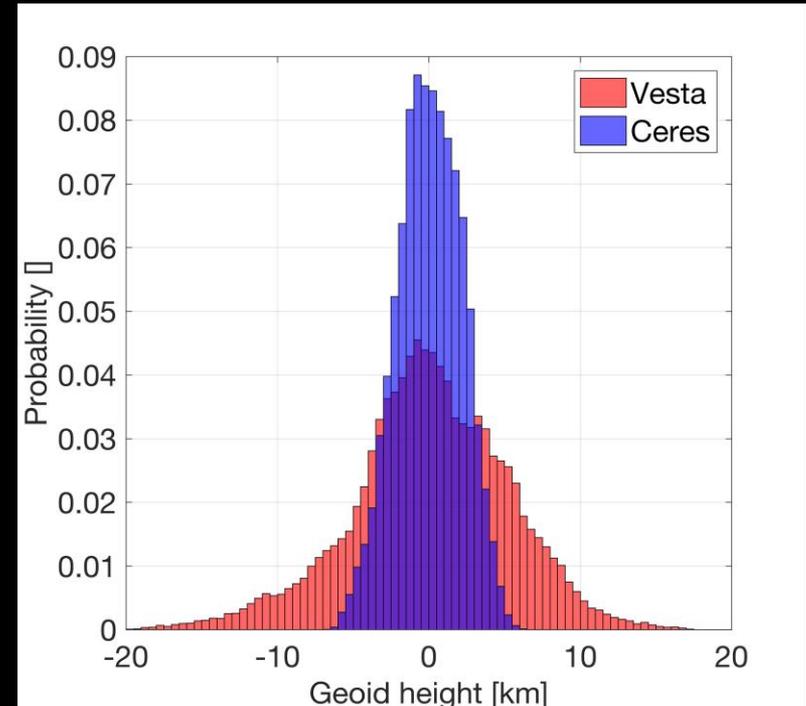
# Ceres SPG



# Broad characteristics of Vesta and Ceres topography

Parameter	Vesta	Ceres
Radius range (km)	80.1	44.5
Polar flattening	0.2038	0.0770
Equatorial flattening	0.0262	0.0043
Geoid height range (km)	37.9	13.2
Geoid height range RMS (km)	5.2	2.1

## Hypsograms of Vesta and Ceres

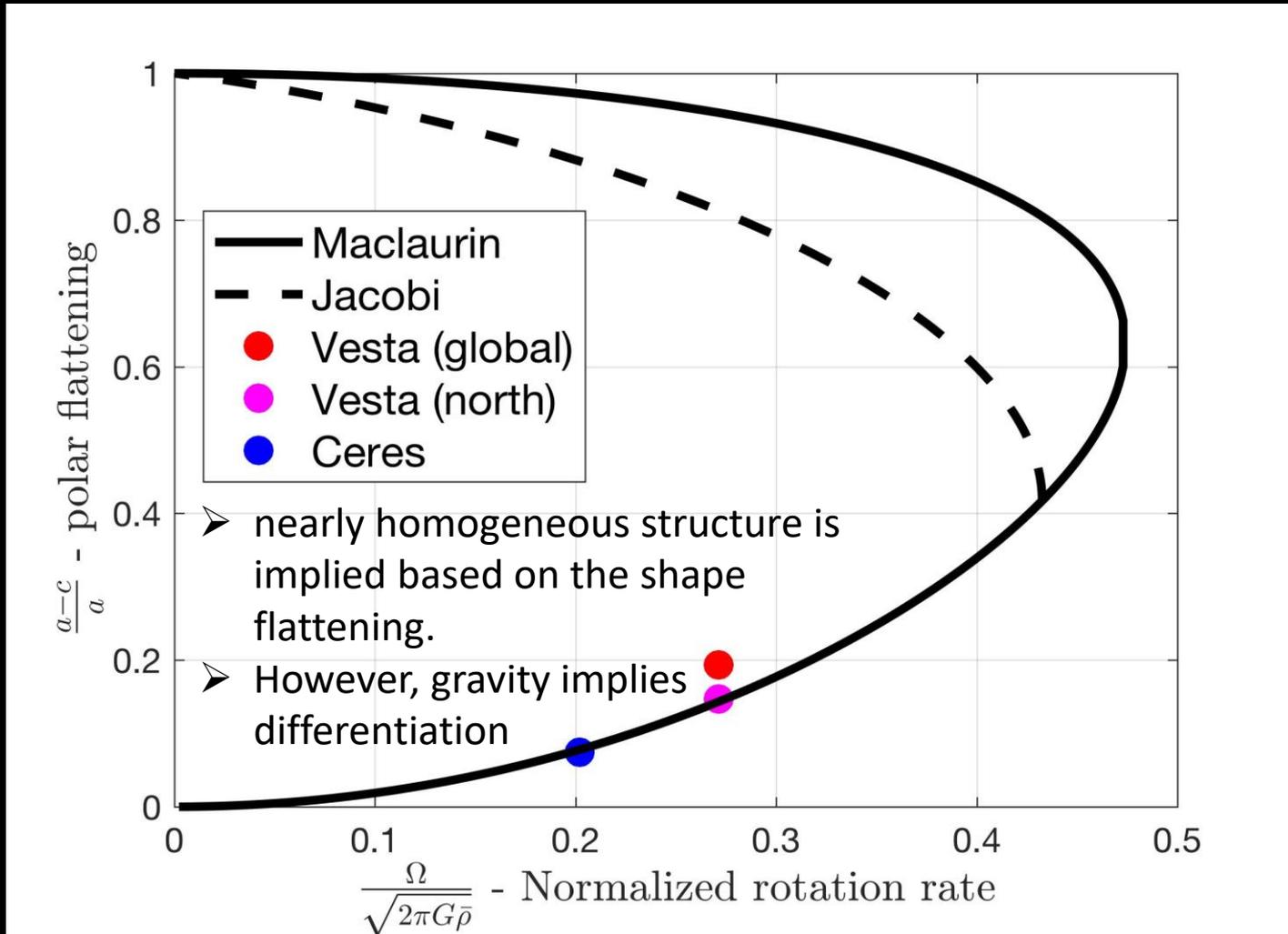




# How we use shape data?

- **Hydrostatic equilibrium**
- **Isostatic compensation**
- **Viscous relaxation**

# Hydrostatic equilibrium



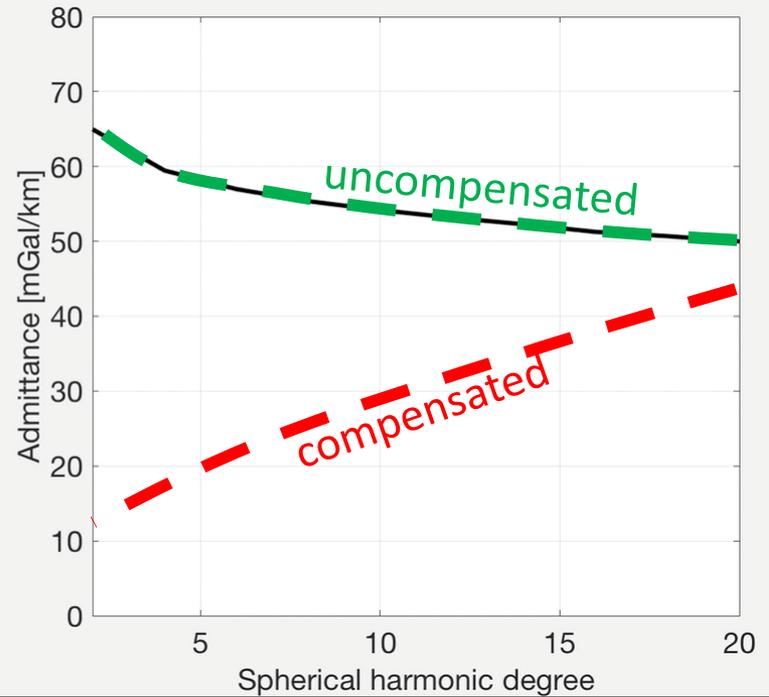
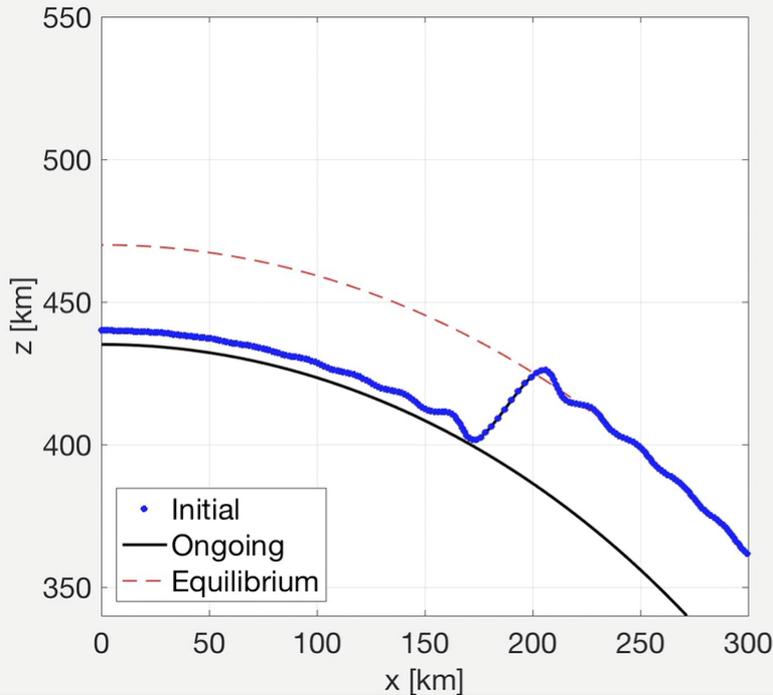


# How we use shape data?

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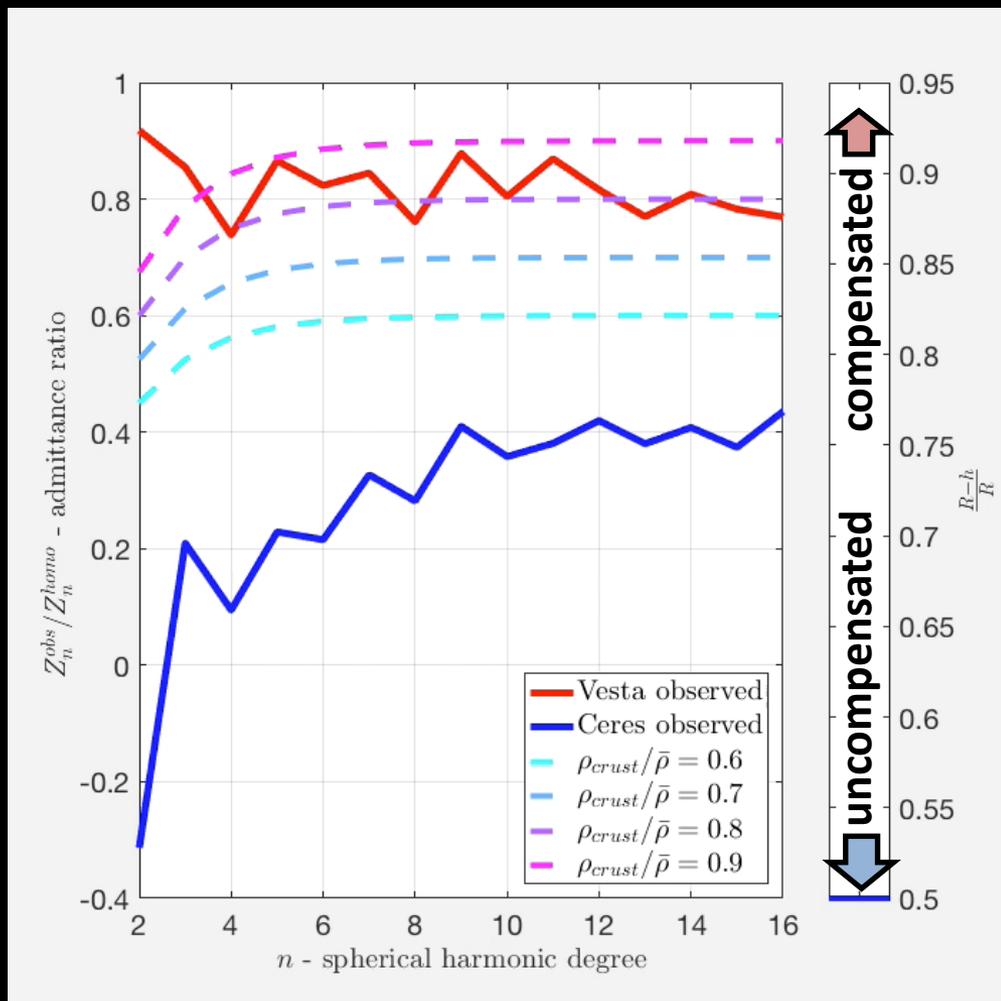
# Isostatic compensation

## Example: viscous spherical cap relaxation



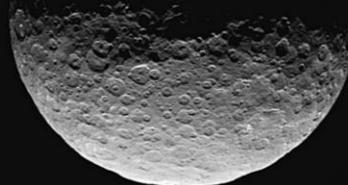
# Isostatic compensation

- Admittance ( $Z$ ) is a ratio of gravity to topography.
- Compensated and uncompensated topography have difference admittances.
- Modeling of isostasy allows constraining the density and thickness of the compensated layer as well as the density contrast.

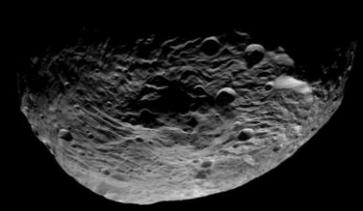




# Compensation for **Vesta** and **Ceres**



- **Vesta** topography is uncompensated
- **Vesta** acquired most of its topography when the crust was already cool and not-relaxing
- **Ceres** topography is compensated
- Lower viscosities (compared to Vesta) enabled relaxation of topography to isostatic state



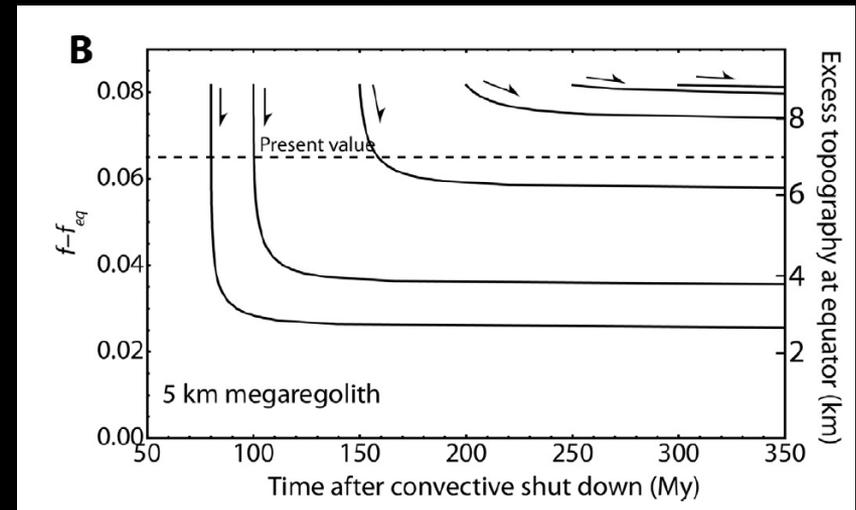
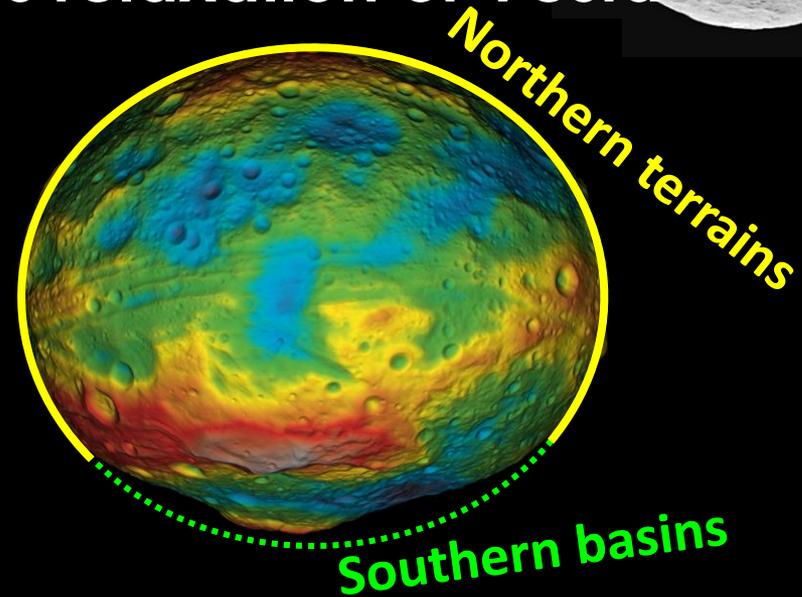
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# Early efficient viscous relaxation of Vesta

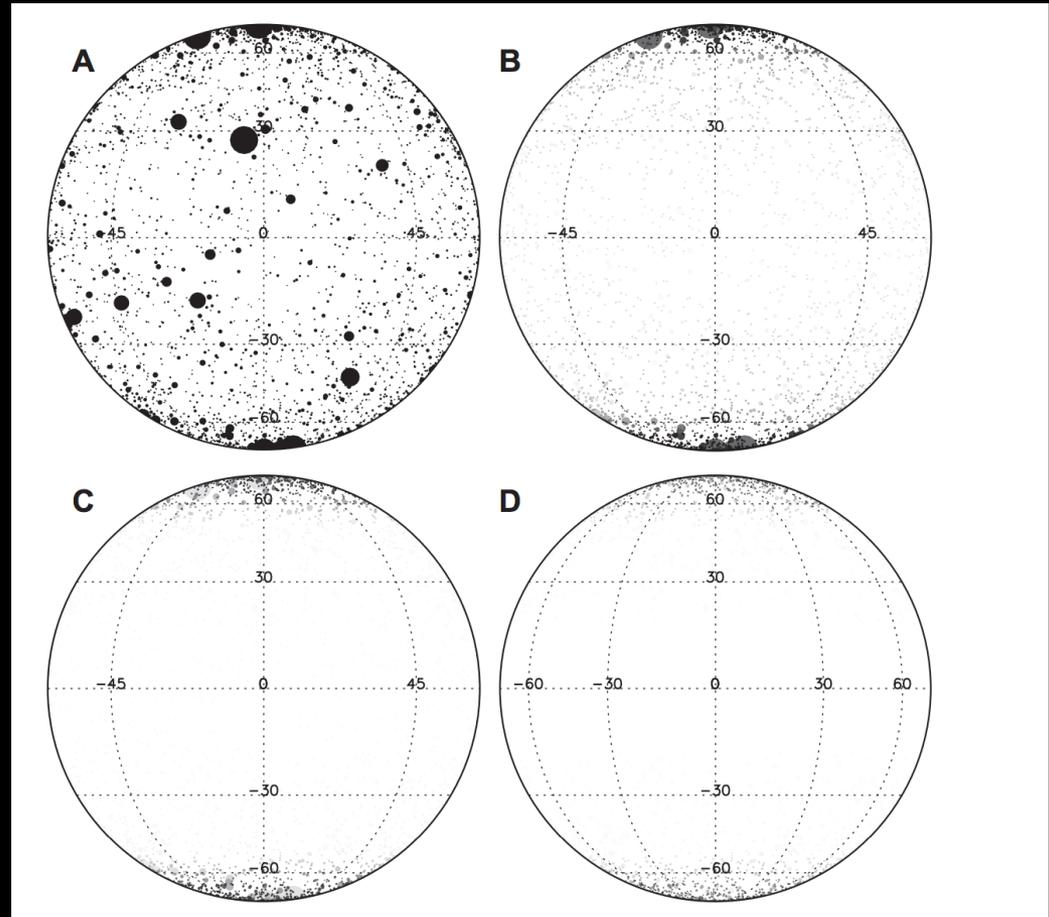
- Vesta was likely close to hydrostatic equilibrium in its early history (Fu et al., 2014)
- Vesta's northern terrains likely reflect its pre-impact equilibrium shape.
- Major impact occurred when Vesta was effectively non-relaxing leading to uncompensated Rheasilvia and Veneneia basins.



(Fu et al., 2014)

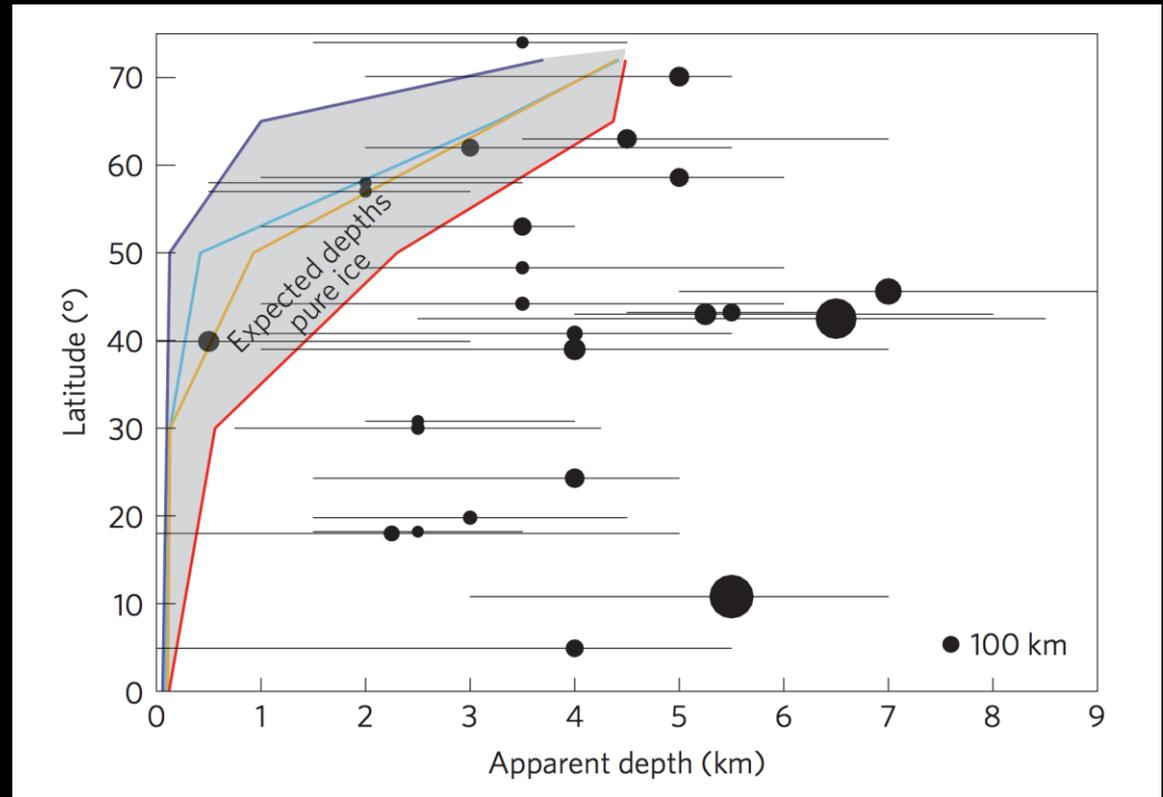
# Viscous relaxation on Ceres (expectation)

- **Bland et al., 2013**  
predicted that craters on Ceres would quickly relax in an ice-dominated shell
  - **Equatorial warmer craters would relax faster than colder polar craters**



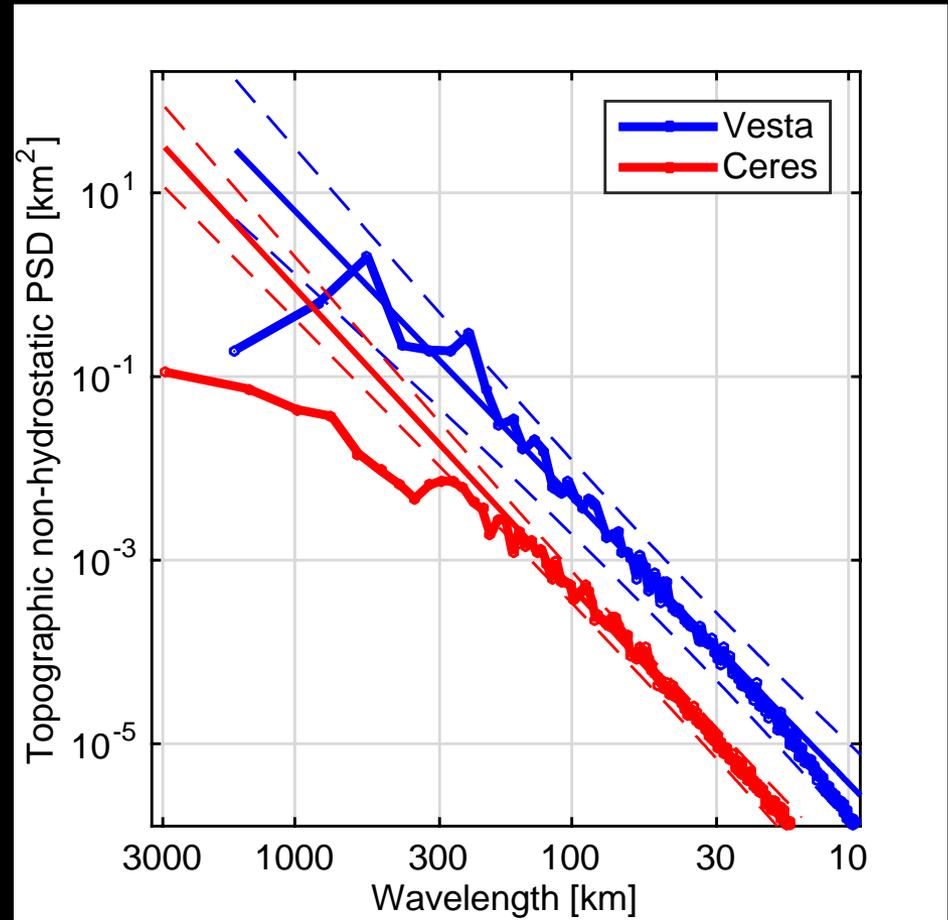
# Viscous relaxation on Ceres (observation)

- **Bland et al., 2016** did not find that evidence for such relaxation pattern
  - **No latitude dependence of crater depth**



# Evidence for viscous relaxation

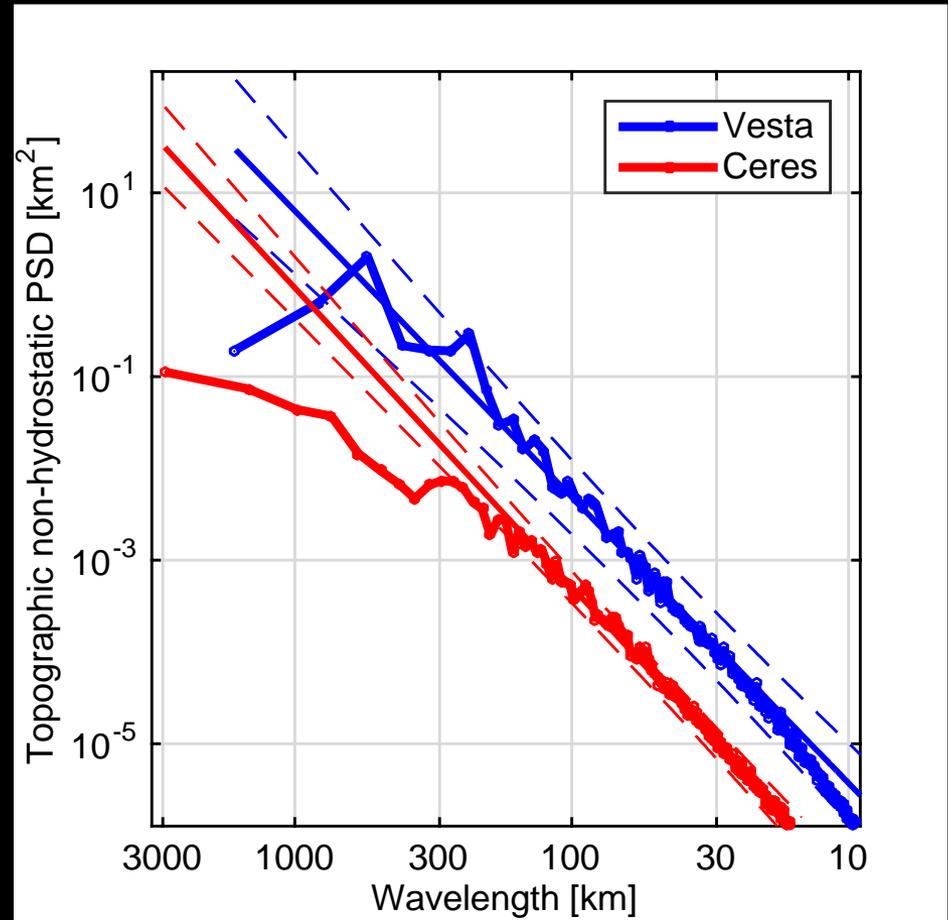
- **More general approach: study topography power spectrum**
- **Power spectra for Vesta closely fits with the power law to the lowest degrees ( $\lambda < 750$  km)**
- **Ceres power spectrum deviates from the power law at  $\lambda > 270$  km**



Ermakov et al., in prep

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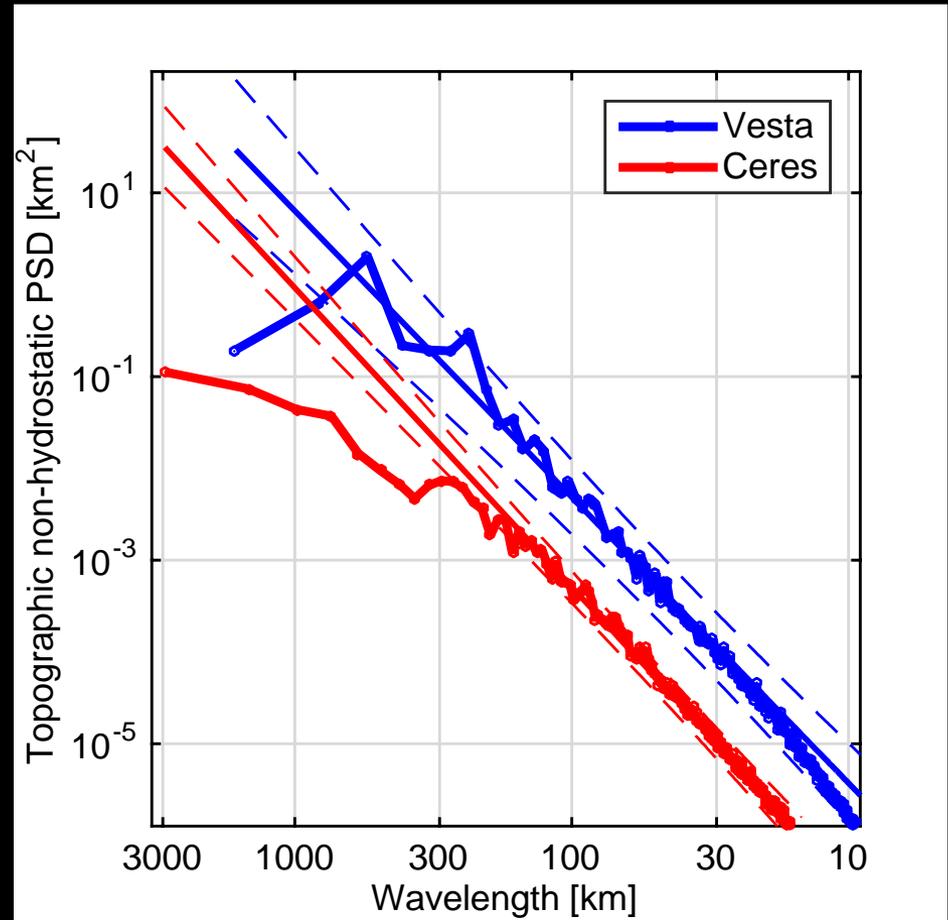
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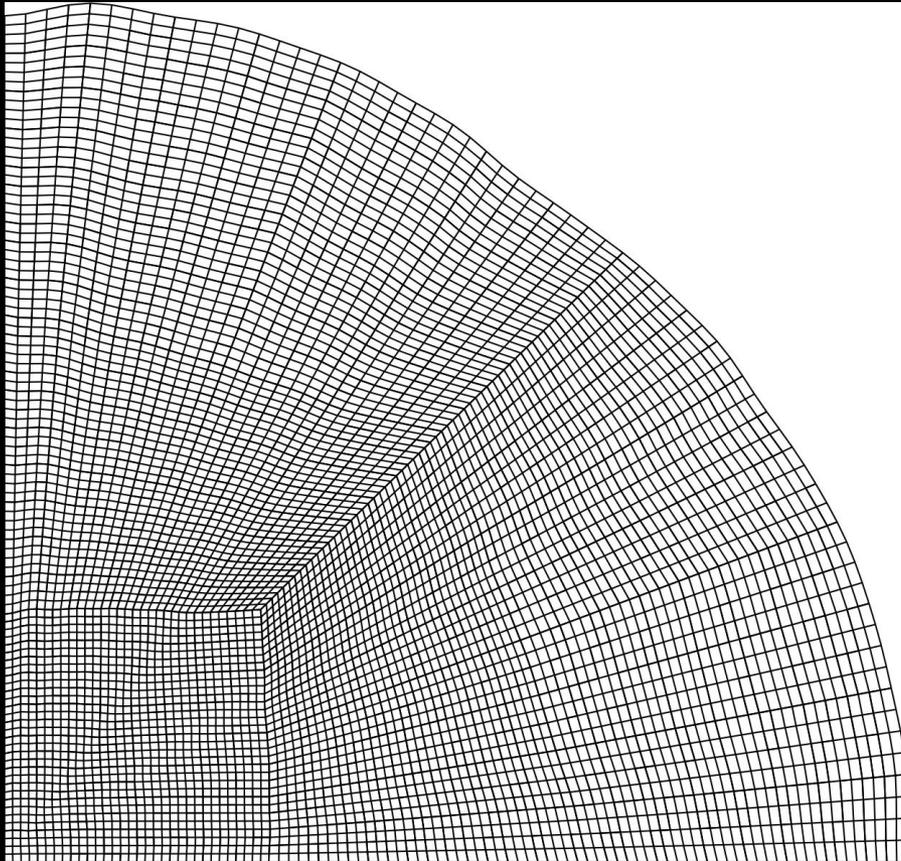
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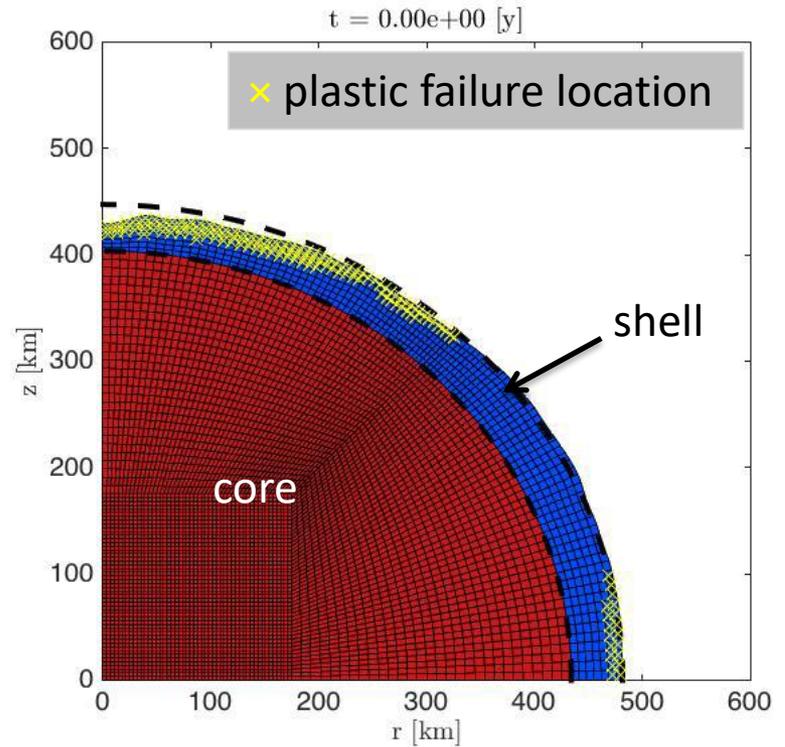
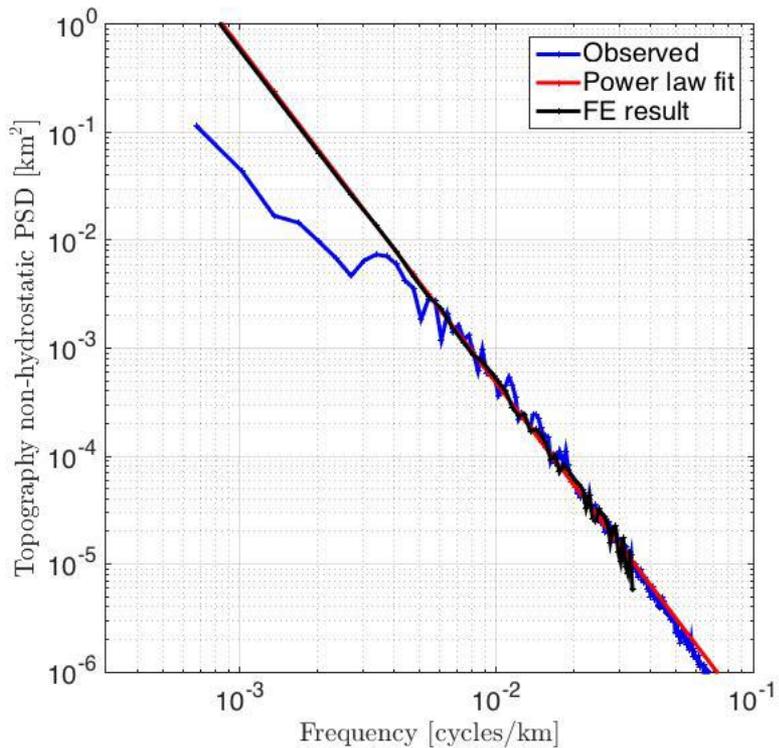
# Finite element model



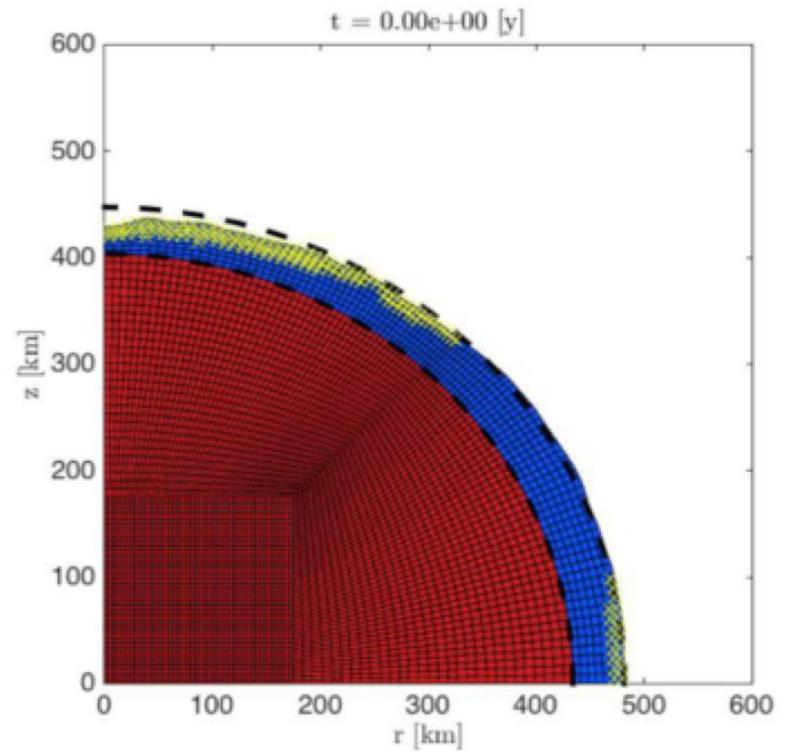
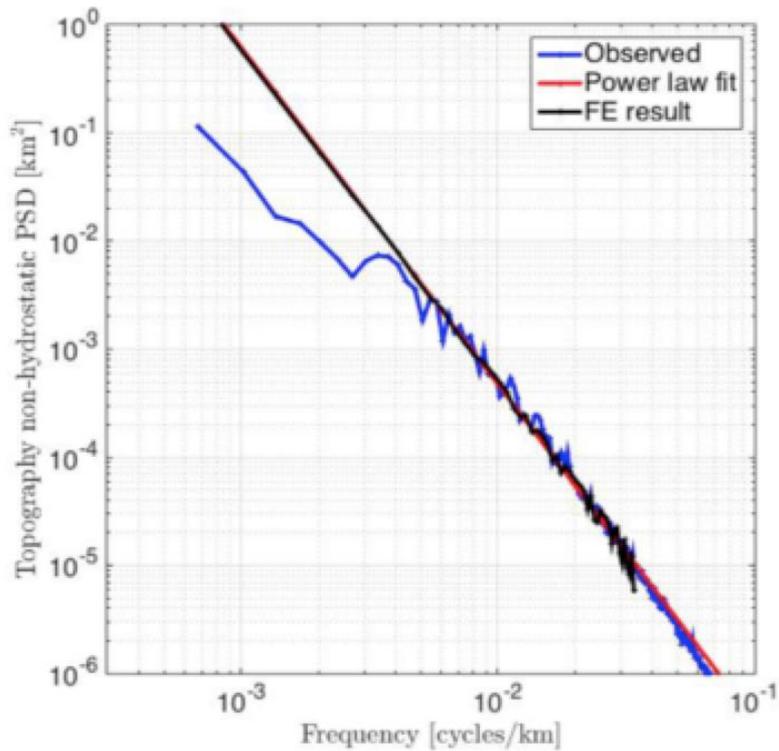
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- Solve Stokes equation for an incompressible flow using deal.ii library
- Compute the evolution of the outer surface power spectrum

Fu et al., 2014; Fu et al,  
submitted to EPSL

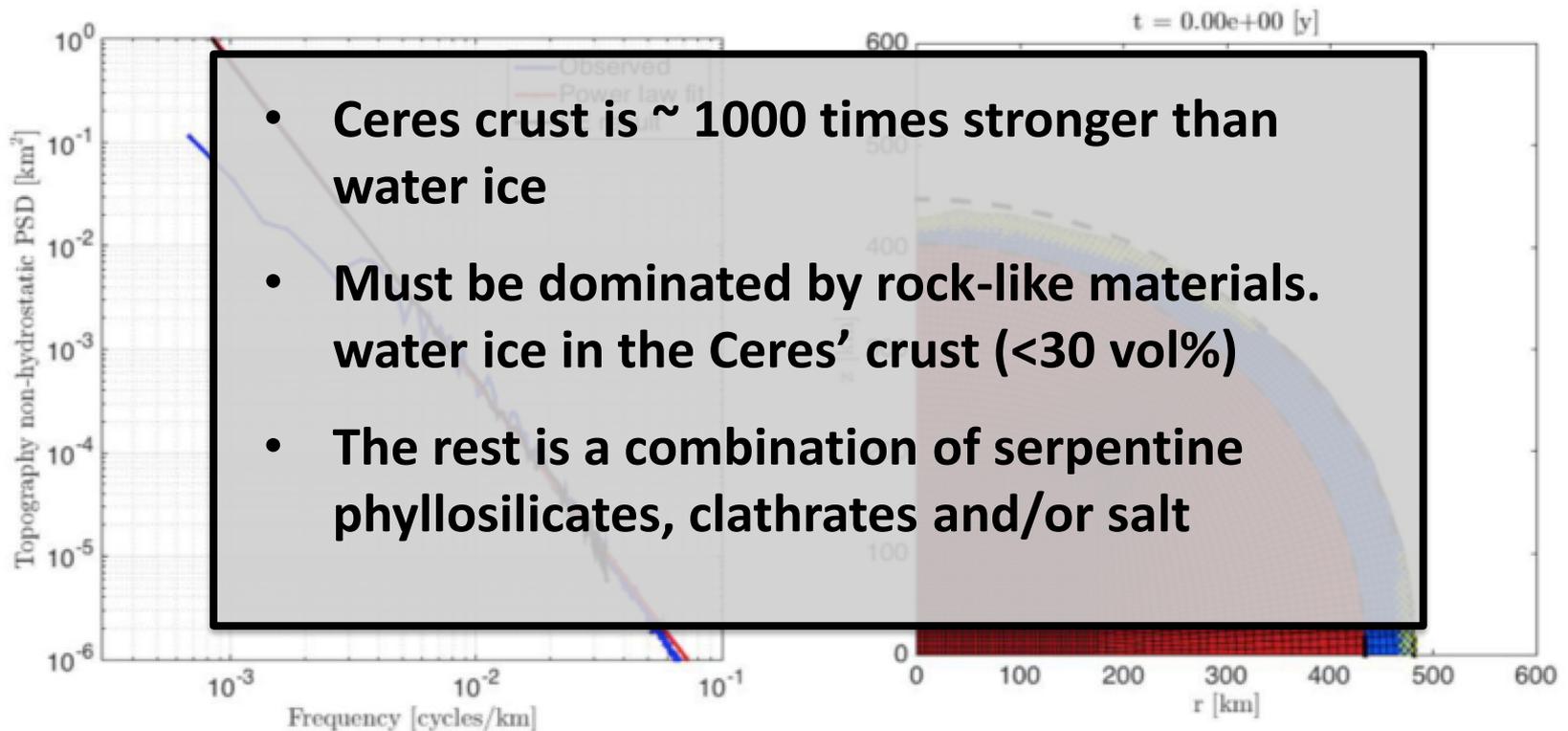
# Example of a FE modeling run



# Finite element modeling results

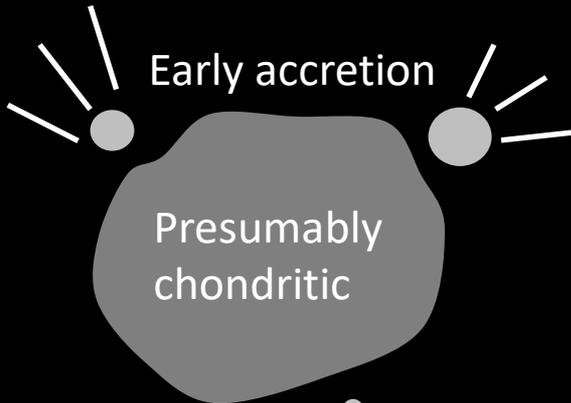


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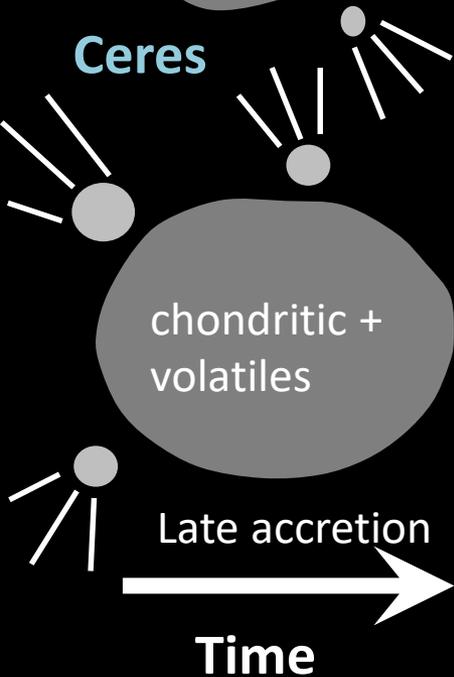


# Vesta and Ceres comparative evolution

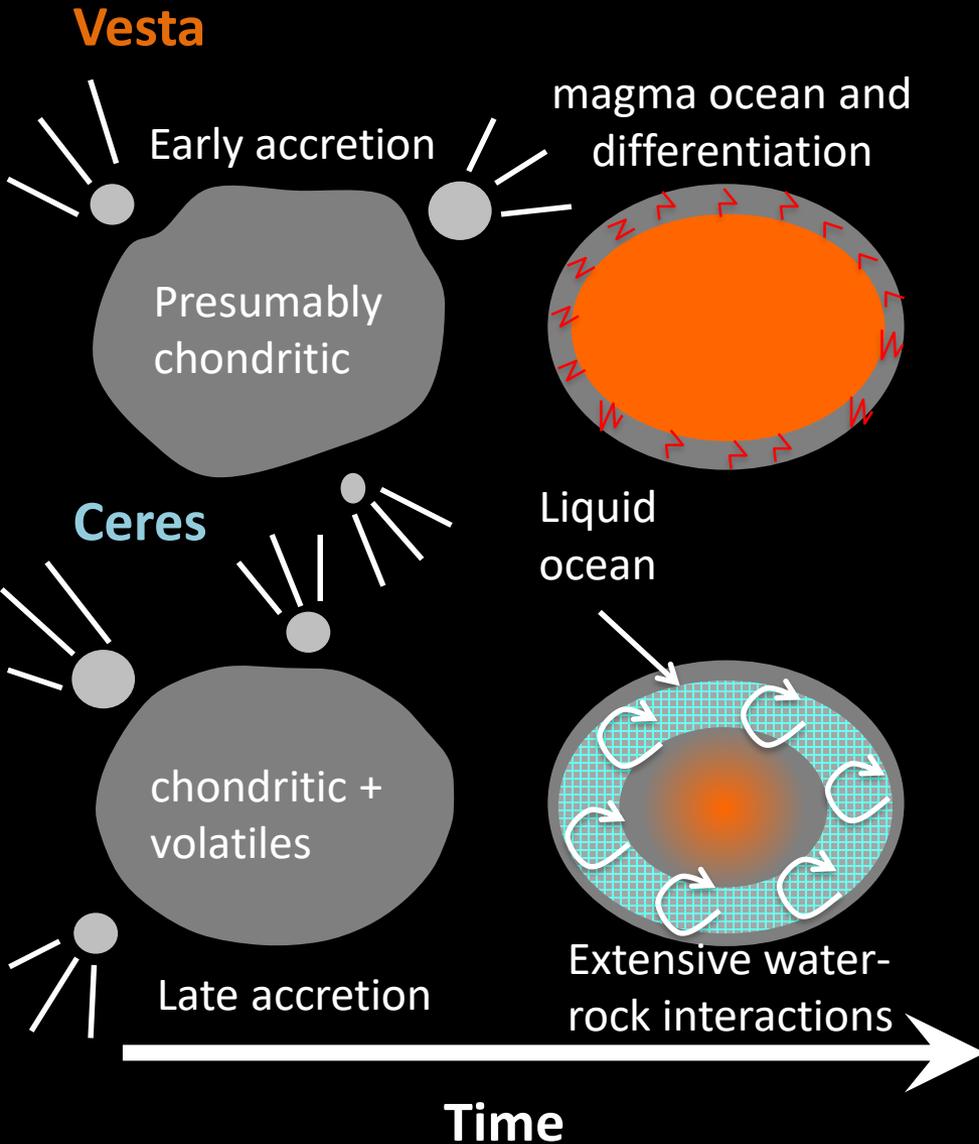
Vesta



Ceres

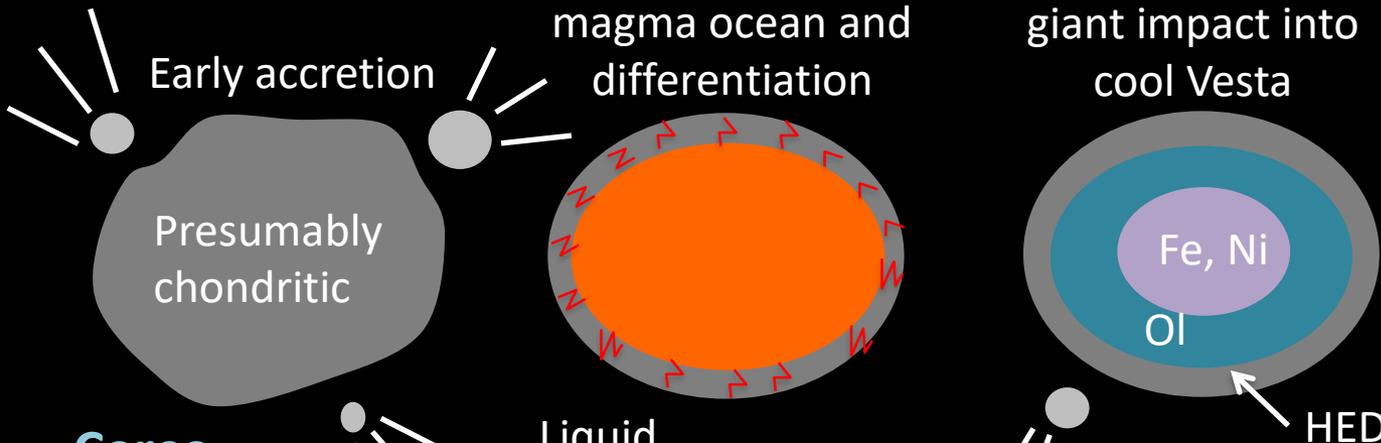


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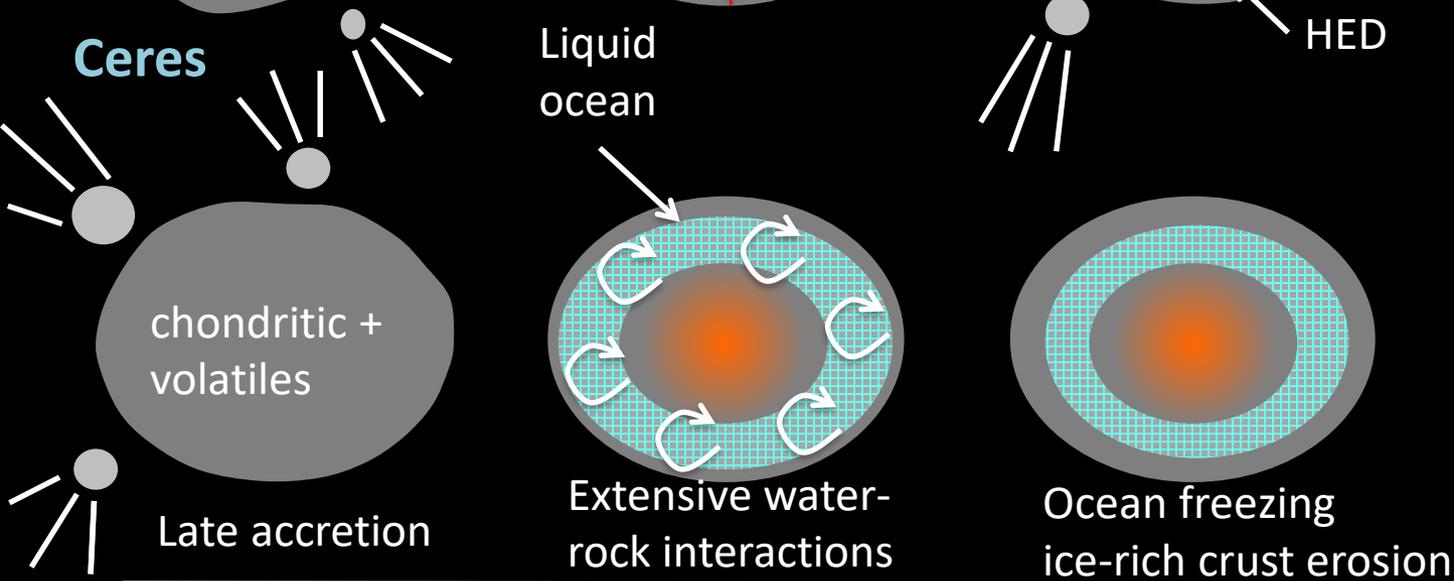


# Vesta and Ceres comparative evolution

## Vesta

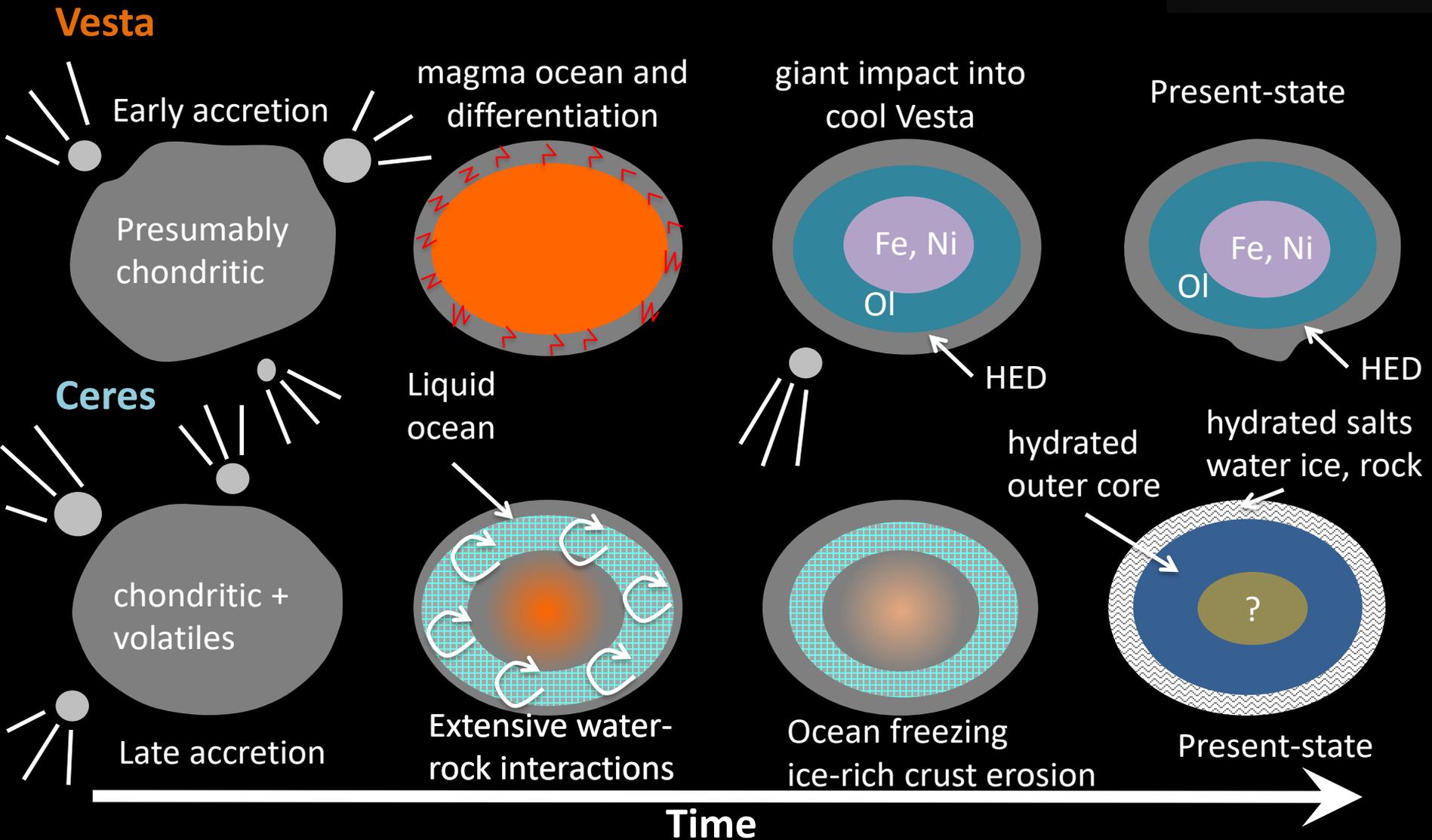


## Ceres

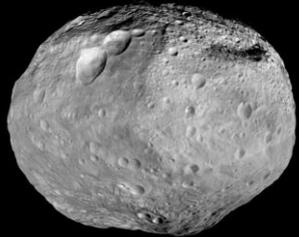


Time

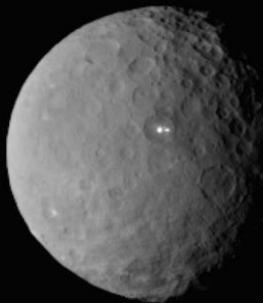
# Vesta and Ceres comparative evolution



# Summary



- Formed early (< 5 My after CAI)
- Once hot and hydrostatic, **Vesta** is no longer either
- Differentiated interior
- Most of topography acquired when **Vesta** was already cool => uncompensated topography
- Combination of gravity/topography data with meteoritic geochemistry data provides constraints on the internal structure

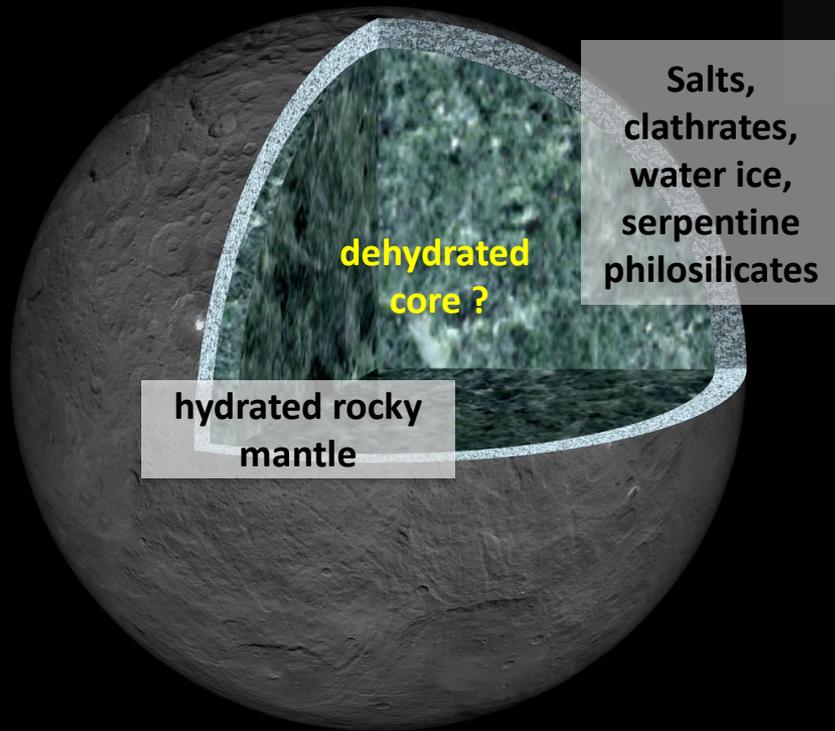


- Cooler history
  - late formation
  - and/or heat transfer due to hydrothermal circulation
- Partially differentiated interior
- Experienced viscous relaxation
- Much lower surface viscosities (compared to Vesta) allowed compensated topography
- **Ceres'** crust is light (based on admittance analysis) and strong (based on FE relaxation modeling)
- Not much water ice in **Ceres** crust (<30 vol%) now

# Internal structures of Vesta and Ceres

## Ceres →

- Crust is light (1.1-1.4 g/cc) and mechanically rock-like w
- Mantle density ~2.4 g/cc and unlithified at least to a depth of 100 km
- Possible dehydrated rocky core remains unconstrained



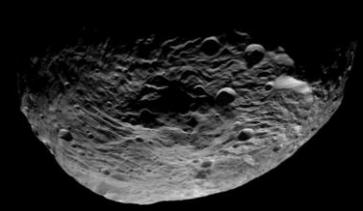
HED-dominated crust



## ← Vesta

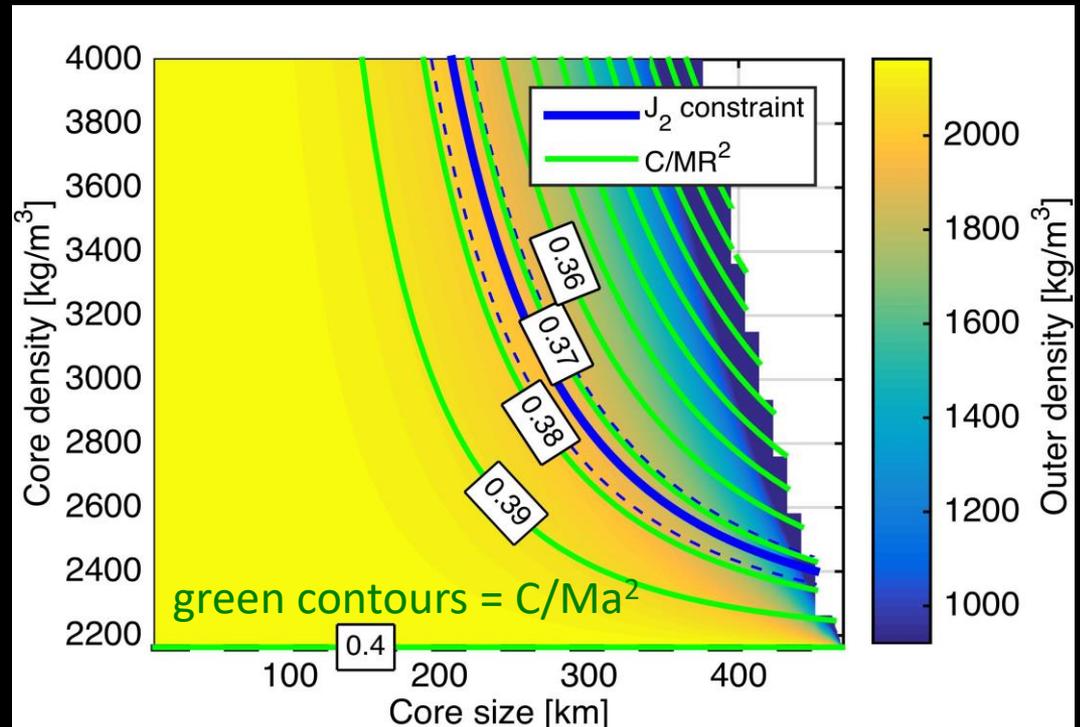
- Crustal density constrained by HEDs and admittance (2.8 g/cc)
- Assuming density of iron meteorites (5-8 g/cc), the core radius is 110 – 155 km

# Backup slides



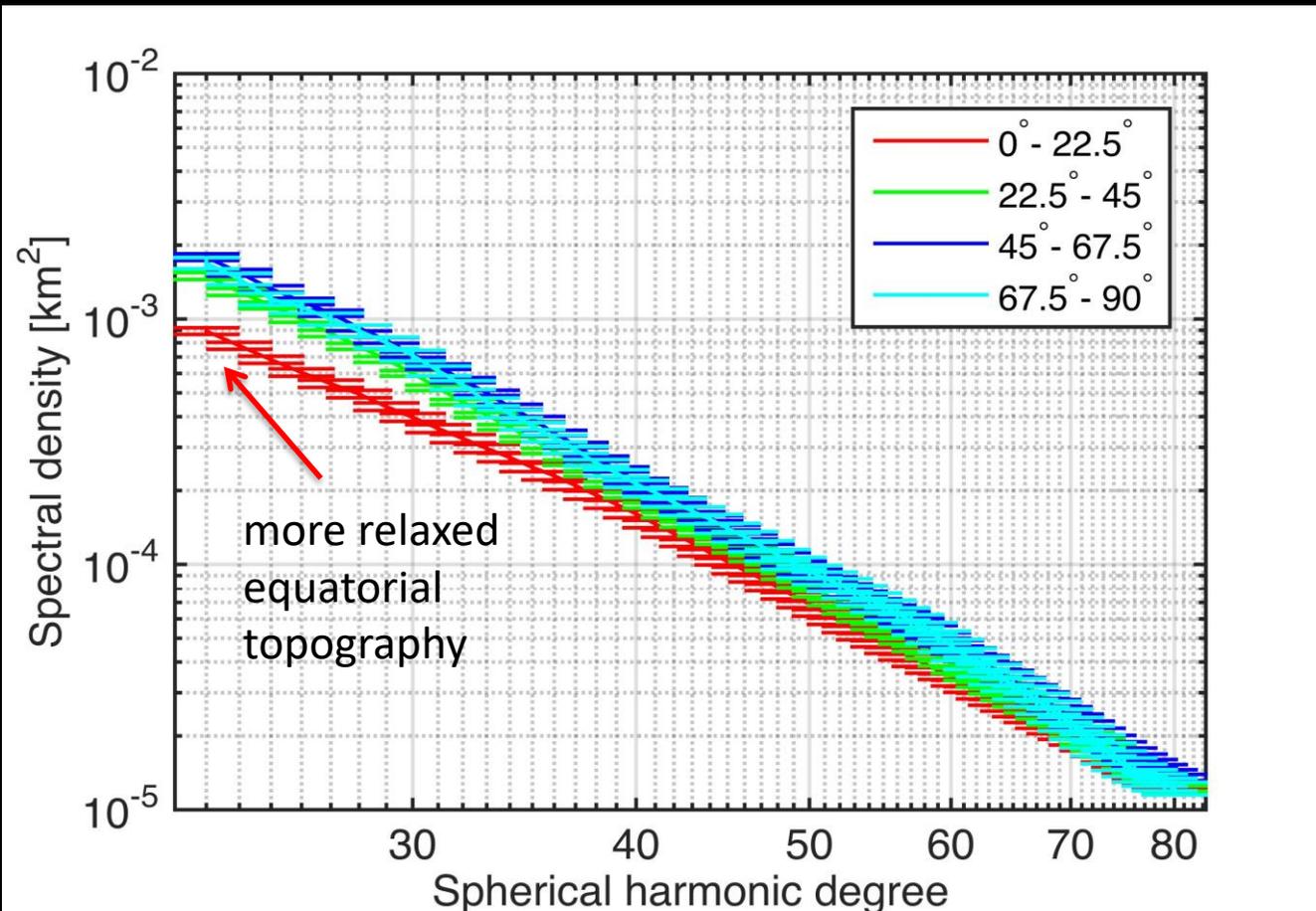
# Two-layer model

- Simplest model to interpret the gravity-topography data
- Only 5 parameters: two densities, two radii and rotation rate
- Yields  $C/Ma^2 = 0.373$   
 $C/M(R_{vol})^2 = 0.392$



Using Tricarico 2014 for computing hydrostatic equilibrium

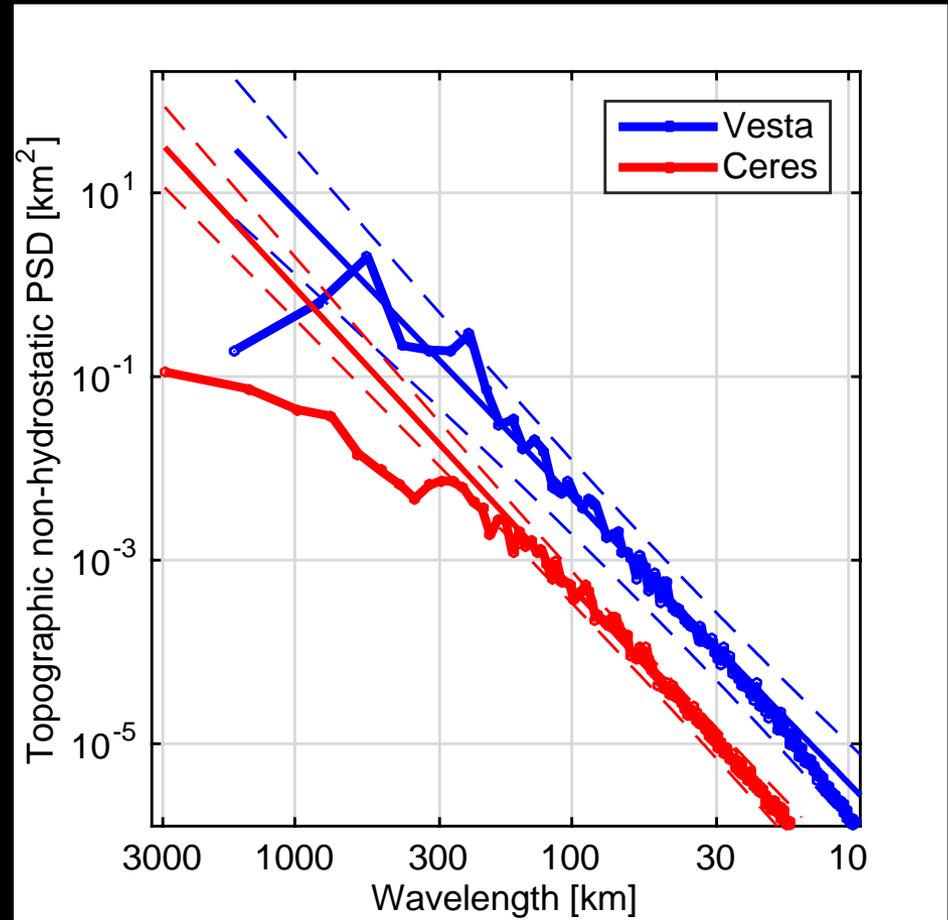
# Latitude dependence of relaxation



Ermakov et al., in prep

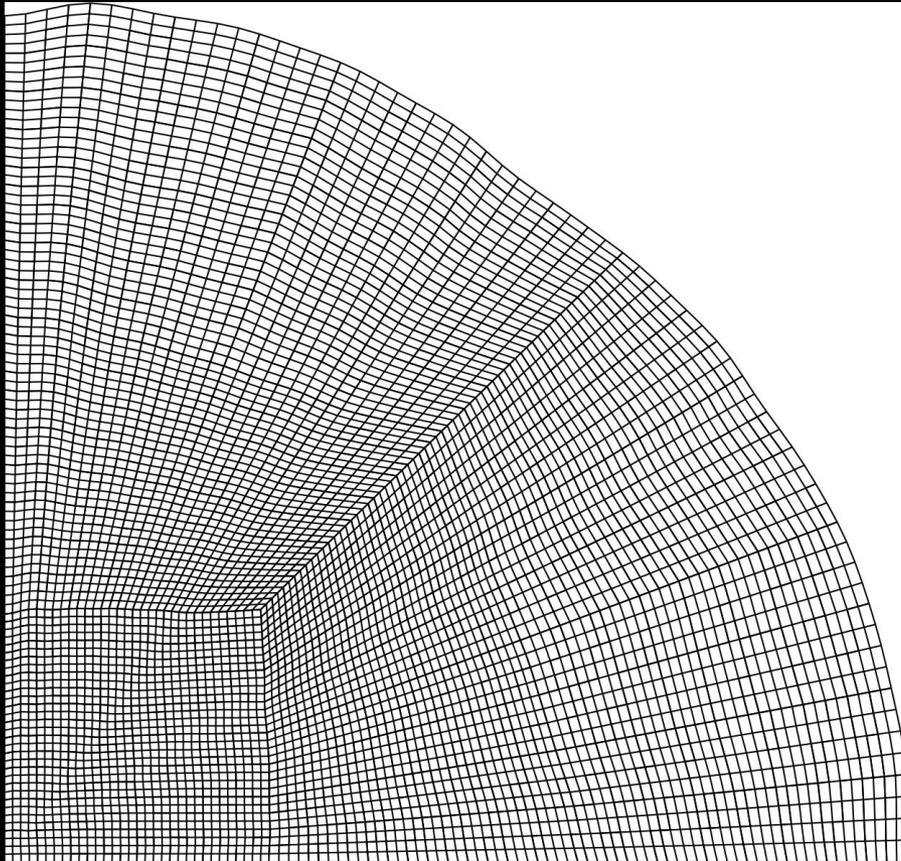
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# Finite element model



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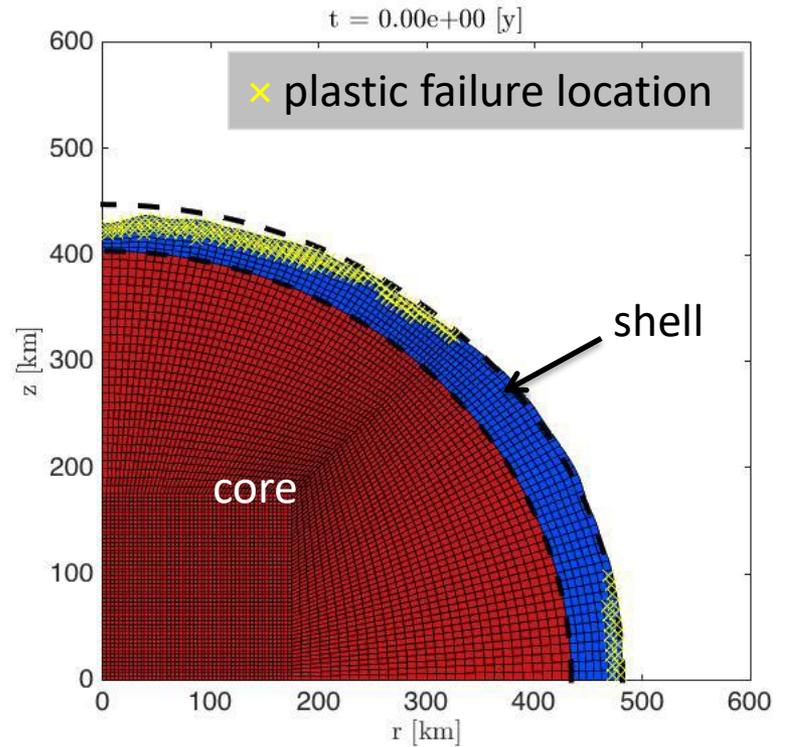
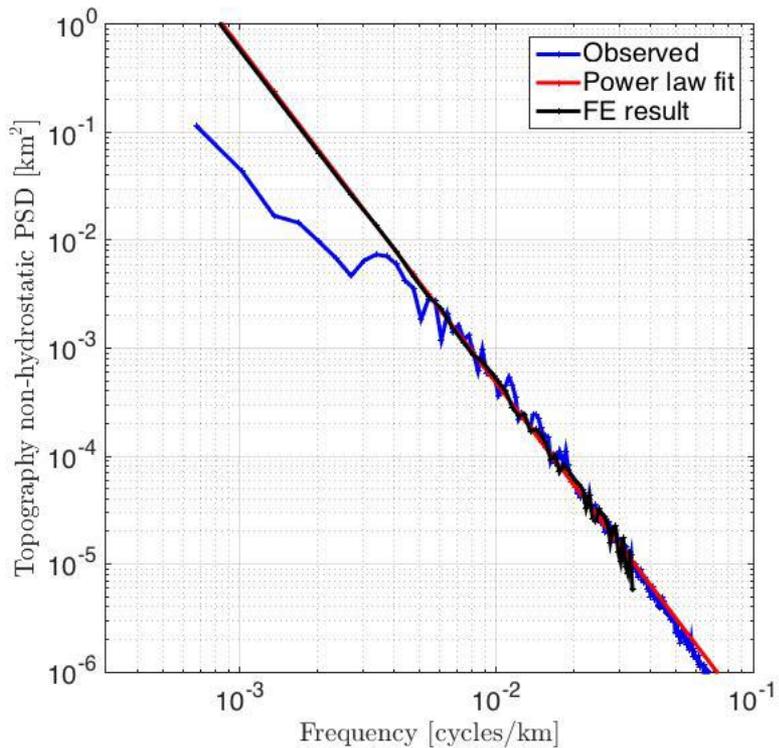
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$$\partial_i(2\eta\dot{\epsilon}_{ij}) - \partial_i p = -g_i\rho$$

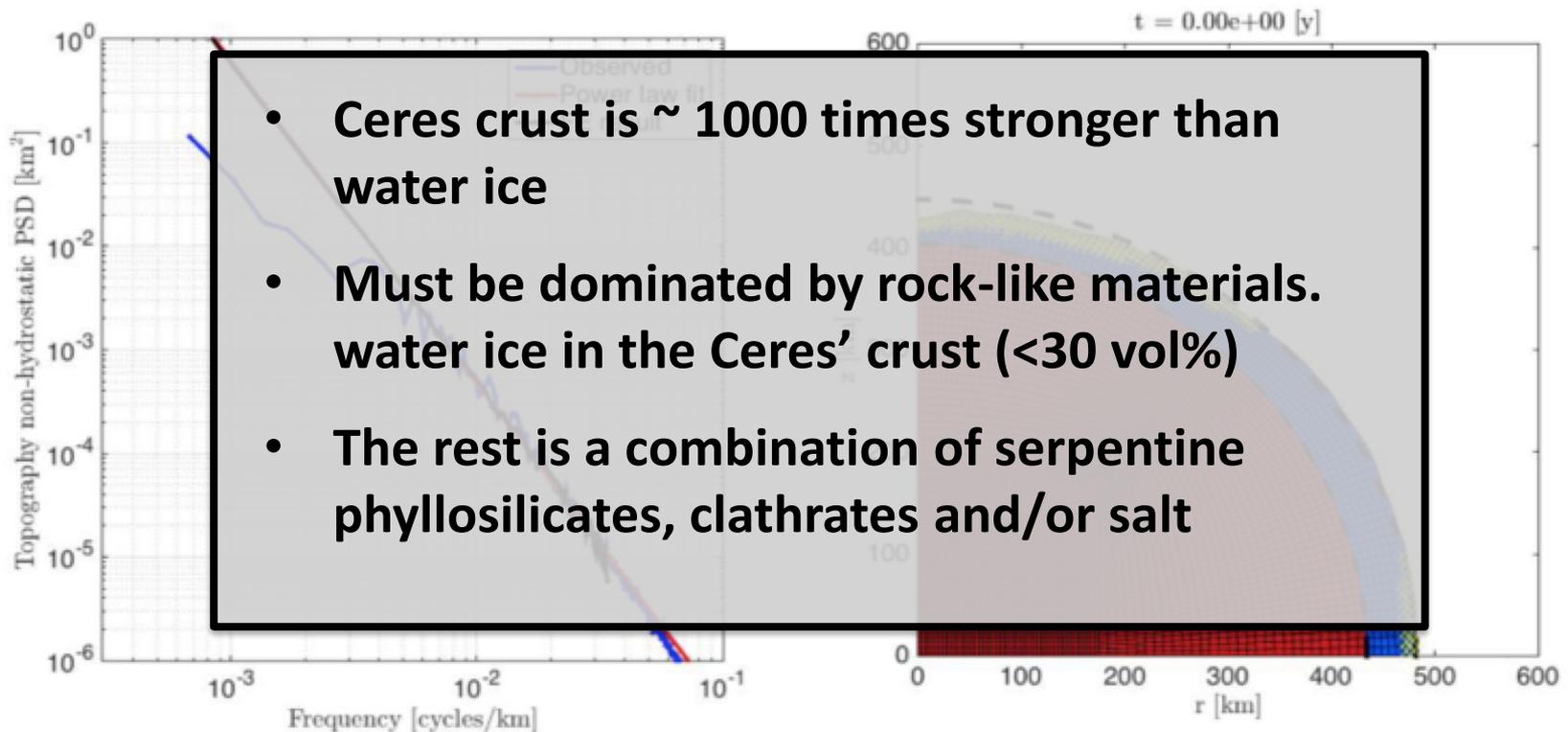
$$\nabla_i u_i = 0$$

- Compute the evolution of the outer surface power spectrum

# Example of a FE modeling run



# Finite element modeling results



# Gravity and topography in spherical harmonics

- Shape radius vector

$$r(f, l) = R_0 \sum_{n=1}^{\infty} \sum_{m=0}^n (A_{nm} \cos(m l) + B_{nm} \sin(m l)) P_{nm}(\sin f)$$

- Gravitational potential

$$U(r, f, l) = \frac{GM}{R} + \sum_{n=2}^{\infty} \sum_{m=0}^n \frac{R_0^n}{r^{n+1}} (C_{nm} \cos(m l) + S_{nm} \sin(m l)) P_{nm}(\sin f)$$

- Power Spectral Density

$$S_n^{gg} = \sum_{m=0}^n \frac{C_{nm}^2 + S_{nm}^2}{2n+1}$$

gravity

$$S_n^{tt} = \sum_{m=0}^n \frac{A_{nm}^2 + B_{nm}^2}{2n+1}$$

topography

$$S_n^{gt} = \sum_{m=0}^n \frac{A_{nm} C_{nm} + B_{nm} S_{nm}}{2n+1}$$

gravity-topography  
cross power

# Isostatic model

$Z_n$  - gravity-topography admittance

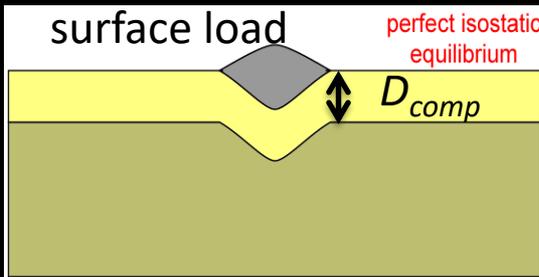
$$Z_n = \frac{S_{gt}}{S_{tt}}$$

➤ Linear two-layer hydrostatic model

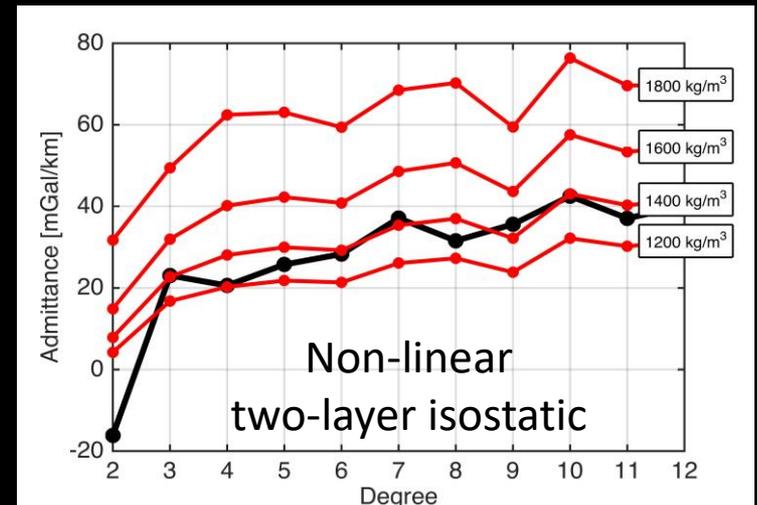
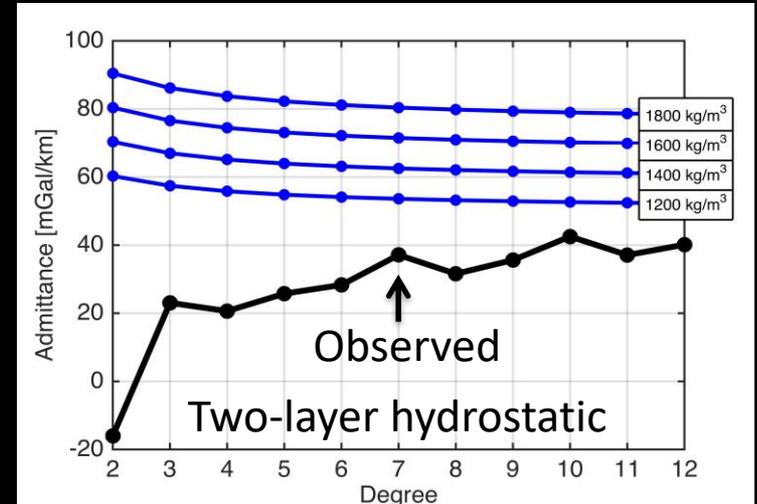
$$Z_n = \frac{GM}{R^3} \frac{3(n+1)}{2n+1} \frac{r_{crust}}{r_{mean}}$$

➤ Linear isostatic model

$$Z_n = \frac{GM}{R^3} \frac{3(n+1)}{2n+1} \frac{r_{crust}}{r_{mean}} \left( 1 - \frac{D_{comp}}{R} \right)$$



$D_{comp}$  - depth of compensation

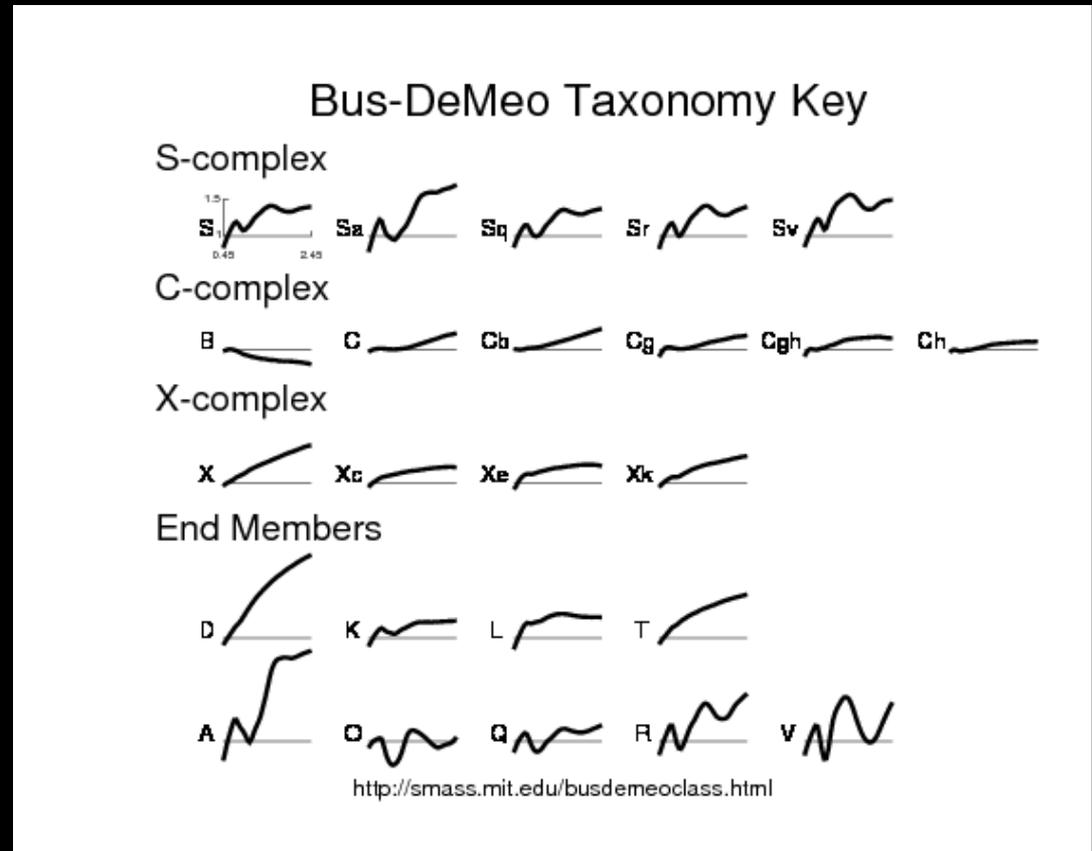




# Why Vesta?

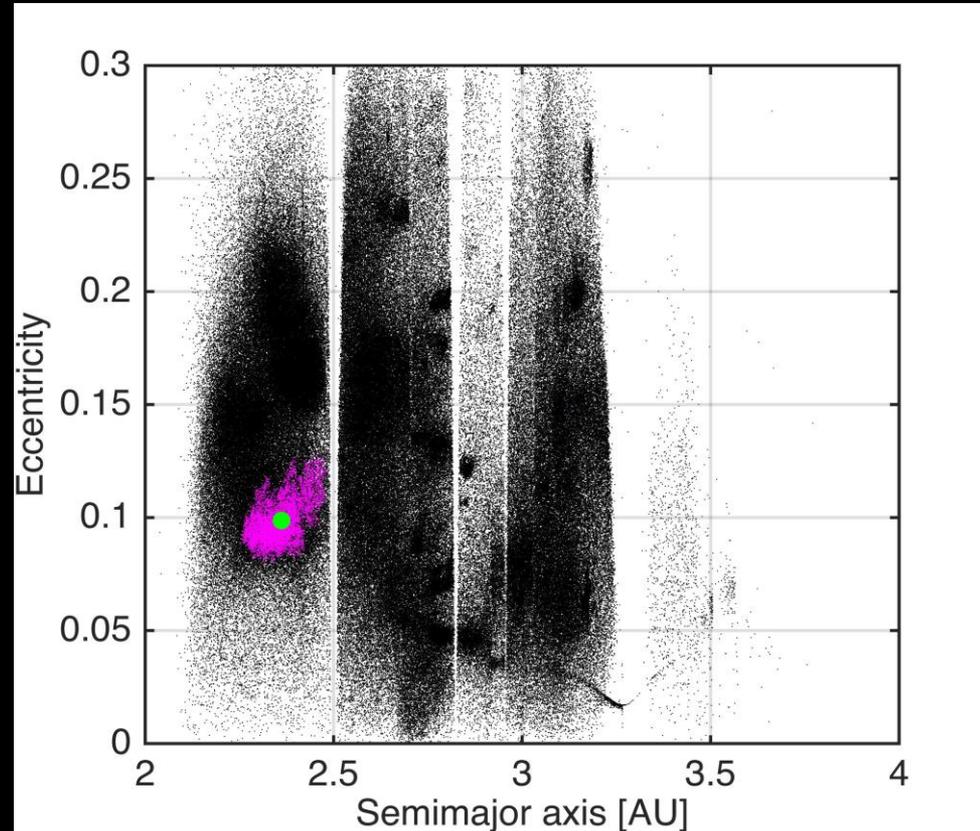


- Unique basaltic spectrum



# Why Vesta?

- **Unique basaltic spectrum**
- **A group of asteroids in the dynamical vicinity of Vesta with similar spectra**



# Why Vesta?

- Unique basaltic spectrum
- A group of asteroids in the dynamical vicinity of Vesta with similar spectra
- Large depression in the southern hemisphere of Vesta

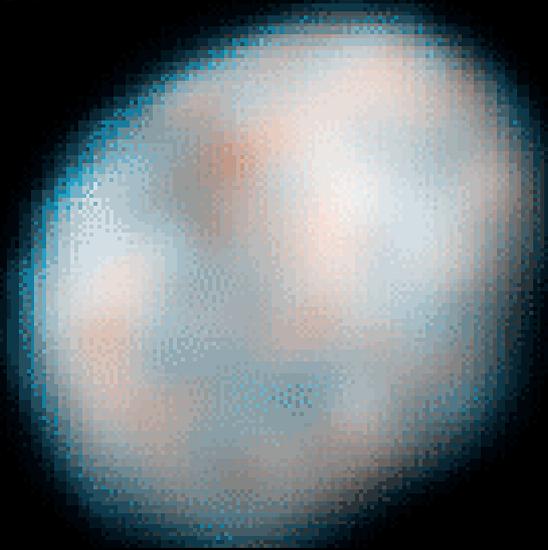
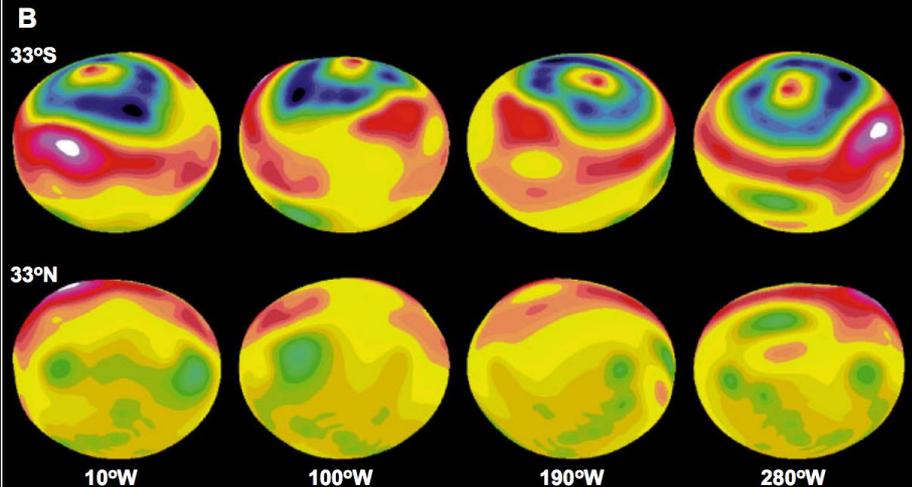
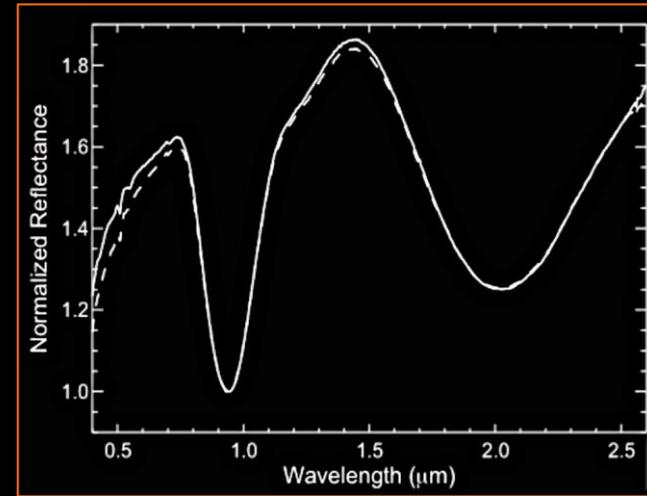


Image credit: NASA/HST



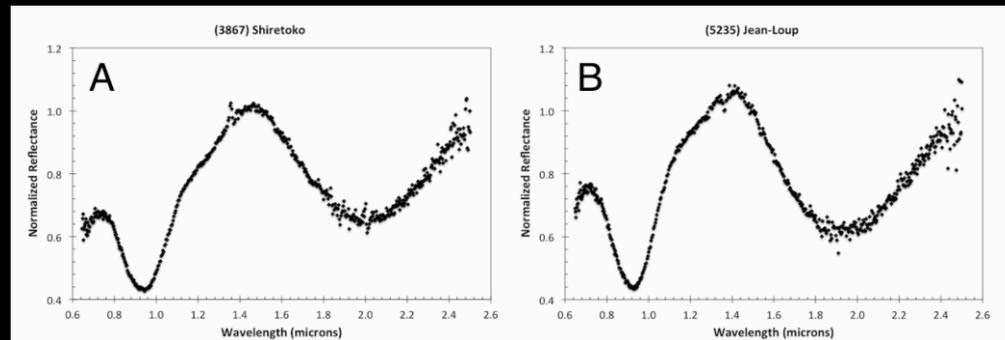
# Why Vesta?

- **Unique basaltic spectrum**
- **A group of asteroids in the dynamical vicinity of Vesta with similar spectra**
- **Large depression in the southern hemisphere of Vesta**
- **A group of Howardite-Eucrite-Diogenite (HED) meteorites, with similar reflectance spectra**



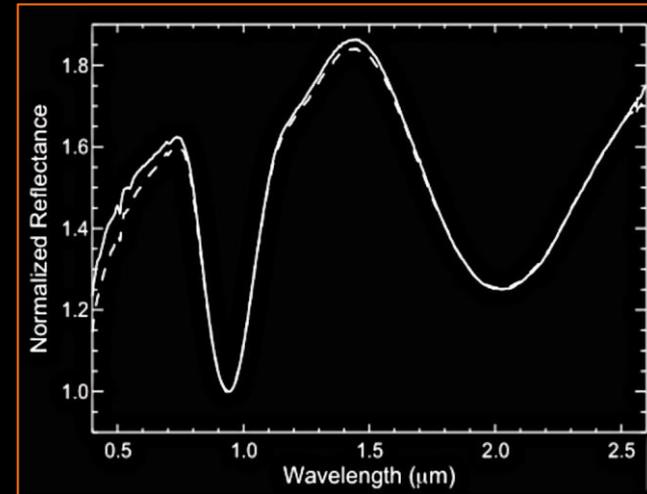
↑ Reflectance spectra of eucrite Millbillillie from Wasson et al. (1998)

↓ V-type asteroids spectra from Hardensen et al., (2014)



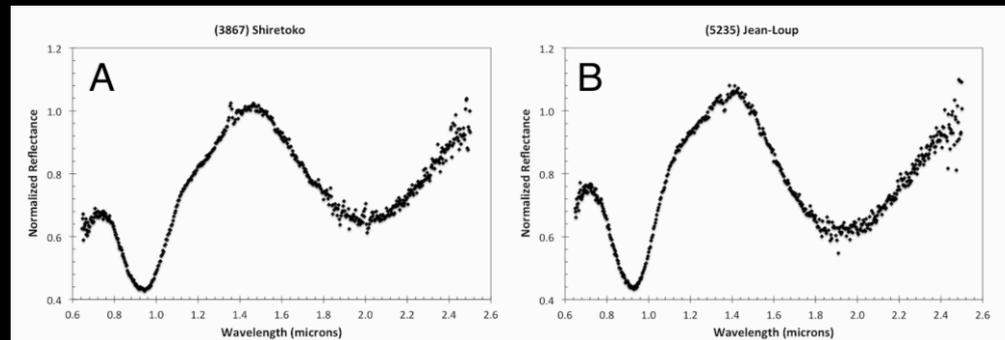
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- **A group of Howardite-Eucrite-Diogenite (HED) meteorites, with similar reflectance spectra**
- **Strongest connection between a class of meteorites and an asteroidal family**



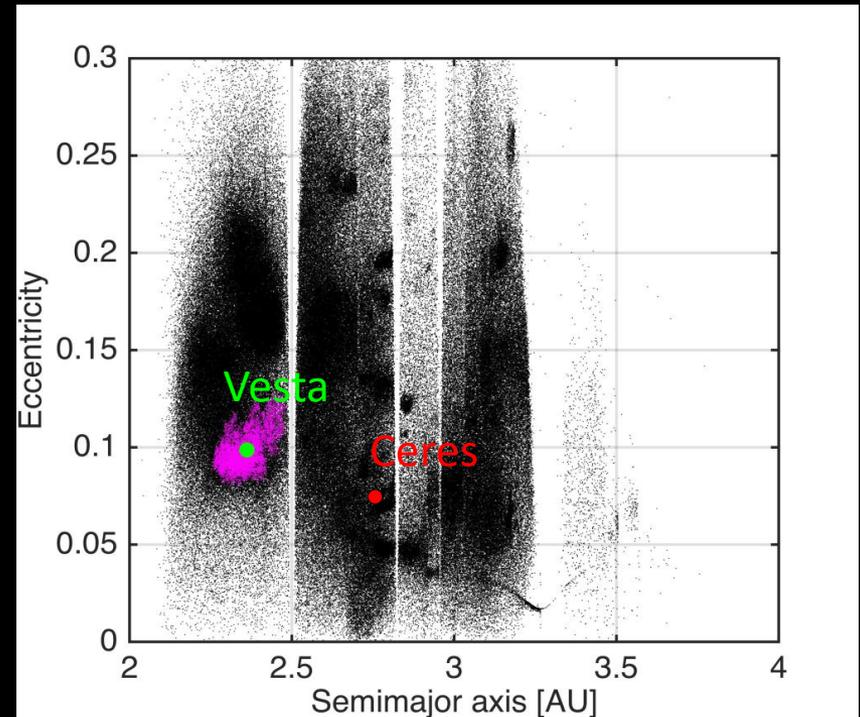
↑ Reflectance spectra of eucrite Millbillillie from Wasson et al. (1998)

↓ V-type asteroids spectra from Hardensen et al., (2014)



# Why Ceres?

- Largest body in the asteroid belt
- Low density implies high volatile content
- Conditions for subsurface ocean
- Much easier to reach than other ocean worlds





# What did we know before Dawn

- **Castillo-Rogez and McCord 2010**

Ceres accreted as a mixture of ice and rock just a few My after the condensation of Calcium Aluminum-rich Inclusions (CAIs), and later differentiated into a water mantle and a mostly anhydrous silicate core.

- **Zolotov 2009**

Ceres formed relatively late from planetesimals consisting of hydrated silicates.

- **Bland 2013**

If Ceres *does* contain a water ice layer, its warm diurnally-averaged surface temperature ensures extensive viscous relaxation of even small impact craters especially near equator