



**Jet Propulsion Laboratory**  
California Institute of Technology

# Model-Transformation-Based Computational Design Synthesis for Mission Architecture Optimization

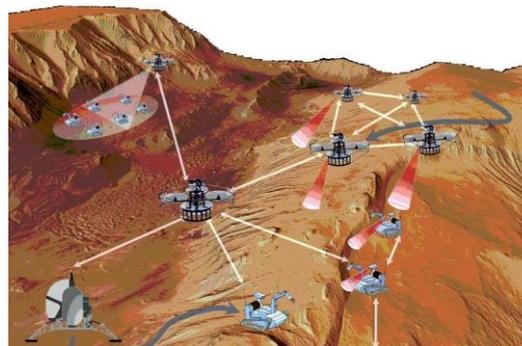
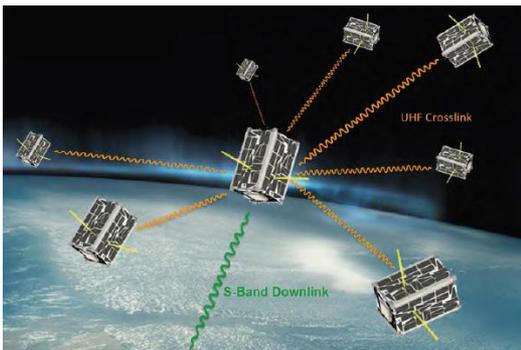
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*Approved For Public Release*

# Networked Constellations of Spacecraft

## JPL Interplanetary Network Initiative

- Small spacecraft may enable the development of innovative low-cost networks and multi-asset science missions
- Goal of initiative is to develop new technologies that support novel mission concept proposals & influence Decadal Survey
  - New approaches to communication, system design, and operations required
  - Our task's work focuses on **design and trade space exploration**



# Motivating Case Study

## Spacecraft-Based Radio Interferometry



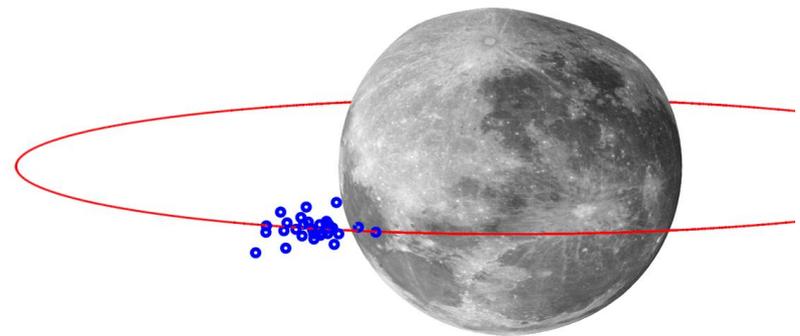
Source: <http://www.passmyexams.co.uk/GCSE/physics/images/radio-telescopes-outdoors.jpg>

### Radio interferometers:

- Radio telescopes consisting of multiple antennas
  - Achieve the same angular resolution as that of a single telescope with the same aperture
- ➔ Typically ground-based

### Want to do this in space:

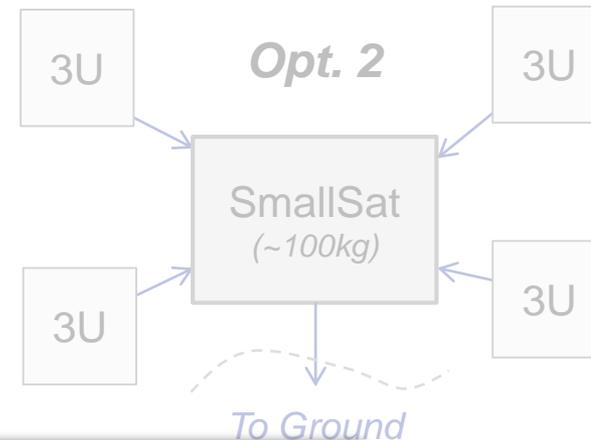
- Frequencies  $< 30\text{MHz}$  blocked by ionosphere
  - Cluster of spacecraft (3 – 50) functioning as telescopes in LLO
- ➔ CubeSats or SmallSats are promising enablers for this



# Which Architecture is Optimal?

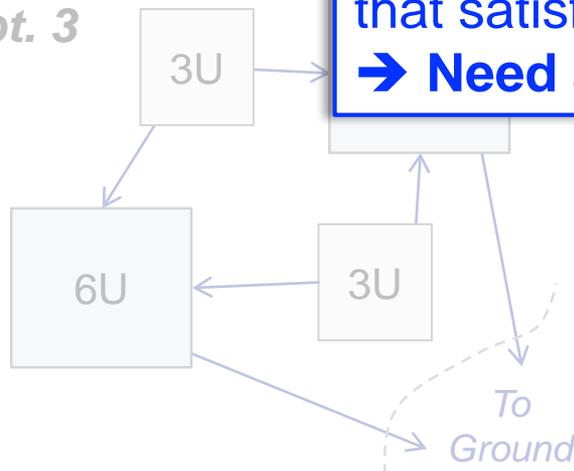
Opt. 1

Same functionality, different qualities / performance  
→ **Examine trade-offs**



Opt. 3

Very large number of architectures that satisfy mission objectives  
→ **Need automation**

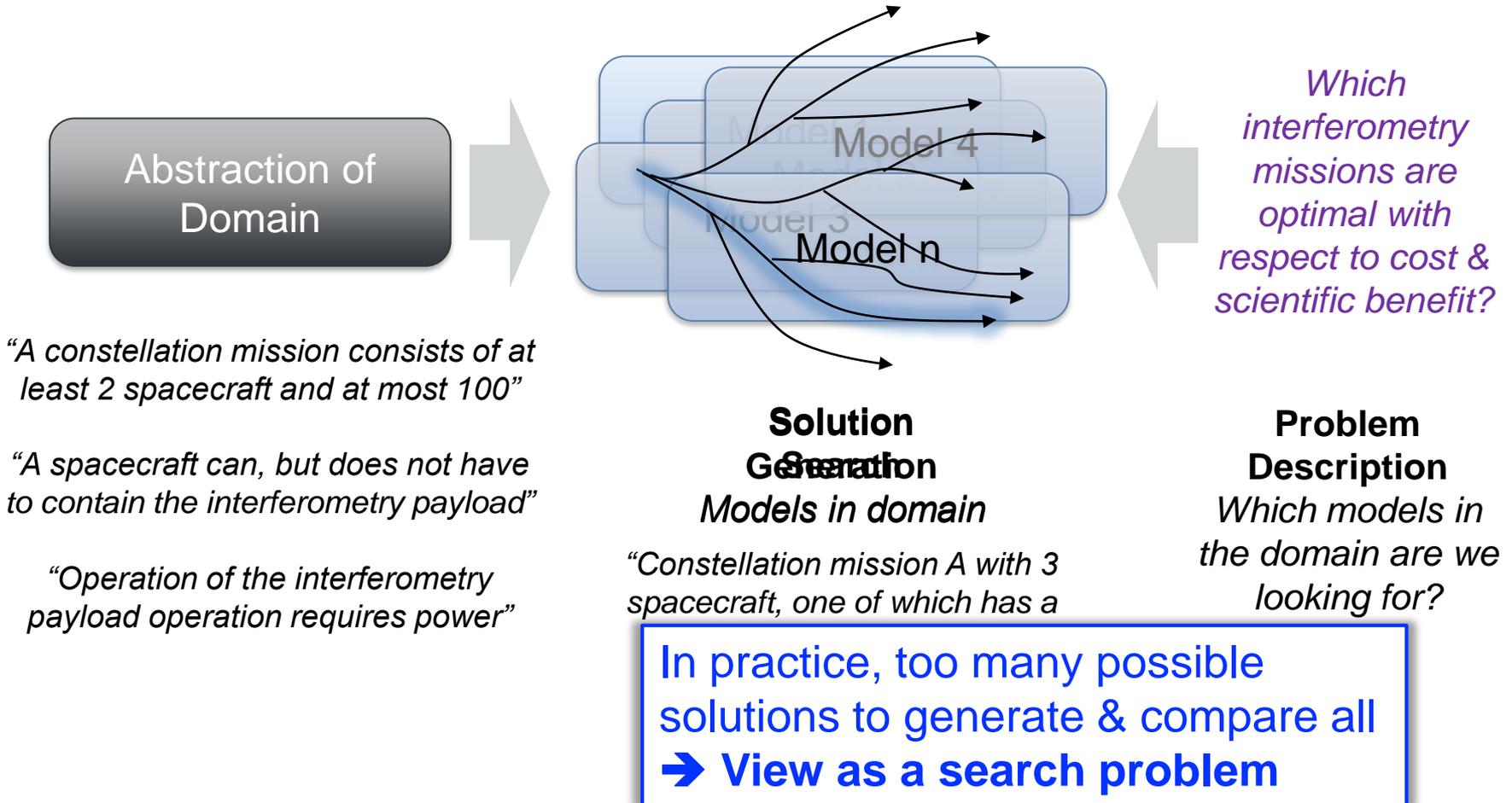


- Very large data Earth
- How many spacecraft?
- Are all equipped with interferometry payload?
  - Who owns the data?
  - What frequency bands? Multi-hop?
  - ...
  - Optimal w.r.t. cost? Science value?

Functional allocation is key  
→ **Synthesis problem**

# Mission Architecture Trade Space Exploration

## Mechanized Exploration



# Domain Model & Well-Formedness Constraints

- Domain model (meta-model)

- Concepts
- Associations / relations
- Attributes

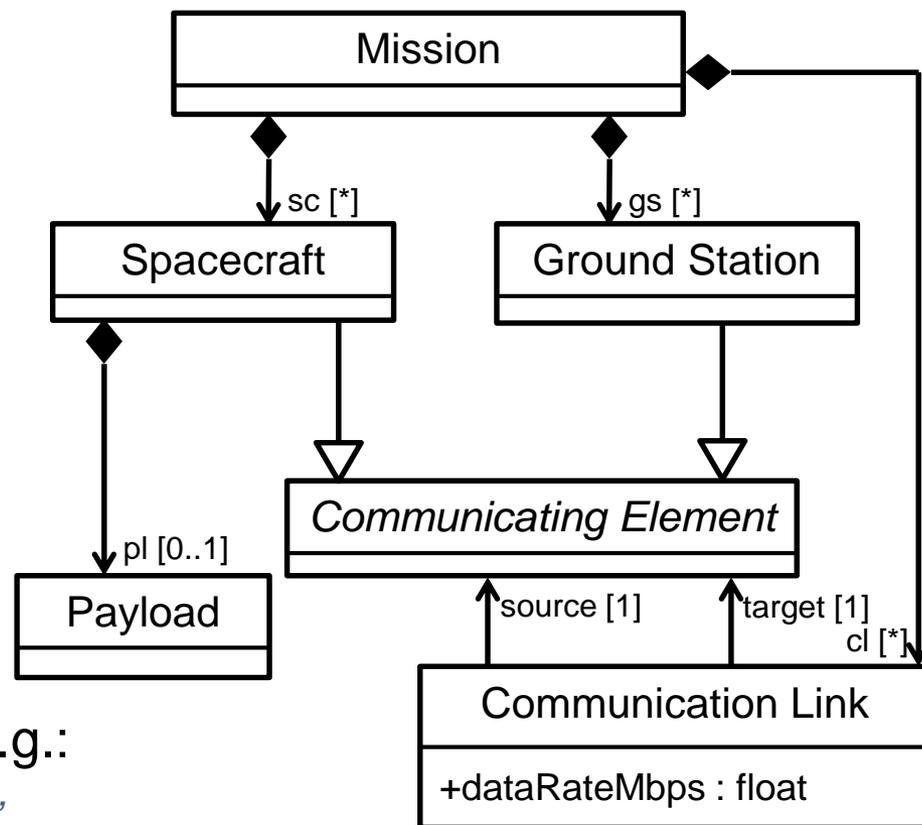
→ Describes a **universe of discourse**: many models in domain

→ Describes structural part of the problem

- Typically annotated with addl. well-formedness constraints, e.g.:

*“No communication loops may exist”*

*“All spacecraft must (transitively) be connected to at least one ground station through a communication link”*

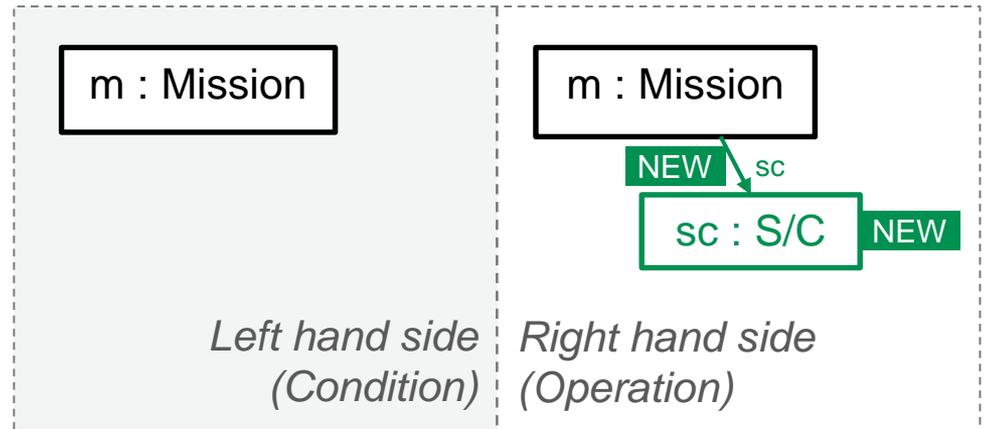


Any model in the domain is a (structurally) valid solution

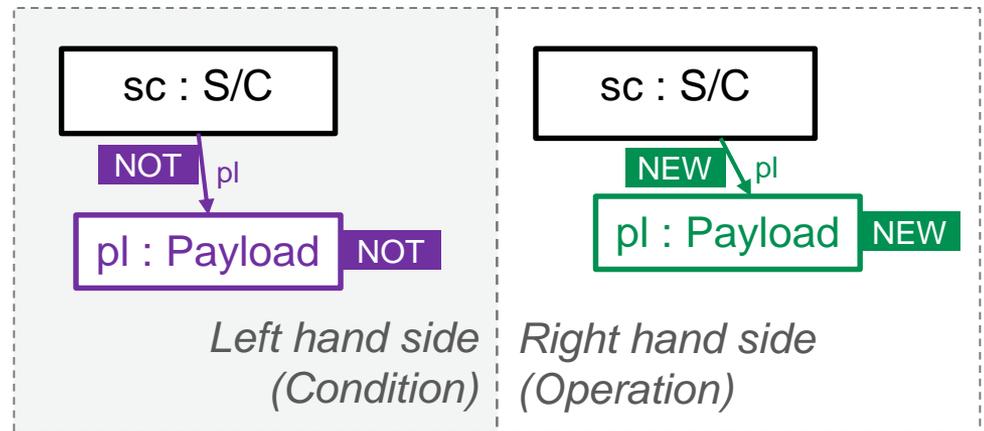
# Model-Transformation-Based Exploration

## Model Transformation Rules as Enablers for Evolving Solutions

- Transformation Rules
  - **LHS:** **Condition** for match in input model (e.g., “*find an element of type Mission*”)
  - **RHS:** **Operation** to be performed (e.g., “*create a new element of type S/C (Spacecraft) and attach it to the matched mission*”)
- Here: *endogenous* transformations
  - Source and target meta-models are the same
- Used for generating **models in domain** (~design rules)



**Rule “createSpacecraft”**

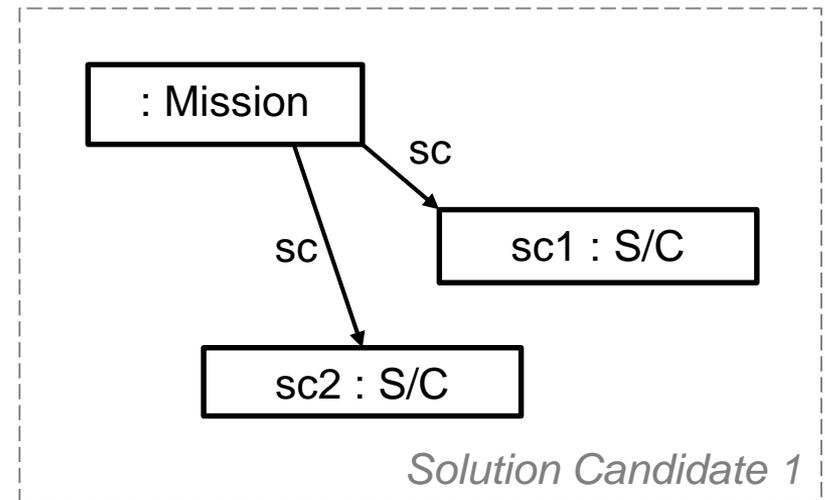


**Rule “addPayload”**



# Evaluating the Objectives

- Evaluating objectives requires **analysis** of the candidate solution (*interpretation by a solver*)
  - Determine performance and determine values for measures of effectiveness
  - Determine objective function values
- Analyses defined at level of domain: part of formal interpretation of models within domain



```
12@ /**
13  * Calculates the expected coverage given a number of spacecraft.
14  *
15  * @param numSpacecraft
16  * @param obsTime
17  * @return
18  */
19@ public static float computeCoverage(int numObservingSpacecraft, int
20  if (numObservingSpacecraft > 1 && obsTime > 0)
21  return (float) (Math.pow(1.0-2.0/(numObservingSpacecraft**
22  else
23  return 0;
24  }
25
26 )
```

**Solver**



**“Scientific value of candidate 1 is 0.34”**

# Driving Exploration Towards Optima

Using Evolutionary Algorithms to find Pareto-Optimal Solutions

## Crossover

**Individual x:**  
(Selection from population)

Add Spacecraft	Add X-Band Comm	Add Spacecraft	Add Comm Link
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fitness=0.6  
(Obj. Fct. Values)

**Individual y:**

Add Spacecraft	Add Ka-Band Comm	Add Payload	Add Spacecraft
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fitness=0.5

Here, individuals are **sequences of transformation rule activations**

→ Each genome in population is a variable with set of trafo rules as range

**New:**

(Recombined individual in next generation)

Add Ka-Band Comm

fitness=0.8

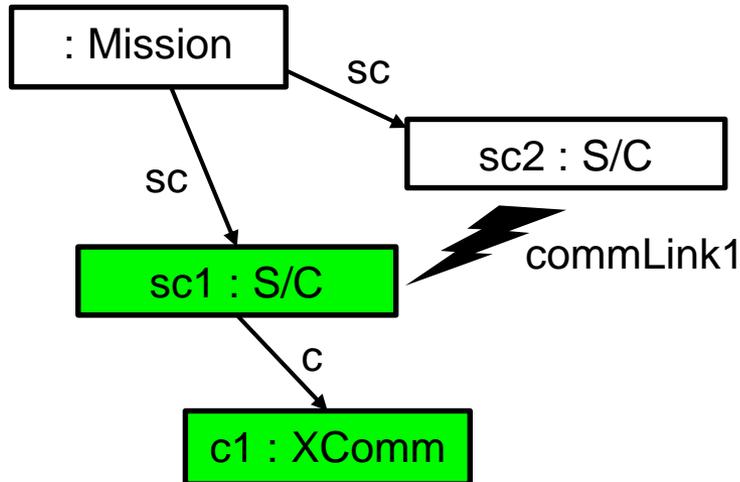
**Mutation**

Could also be a “placeholder” transformation (= rule “do nothing”)

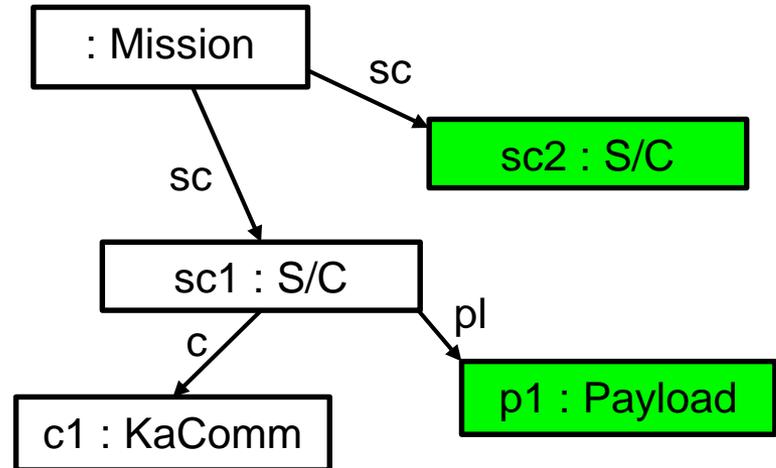
# Driving Exploration Towards Optima

Models Resulting from Executing Transformations

Individual x:

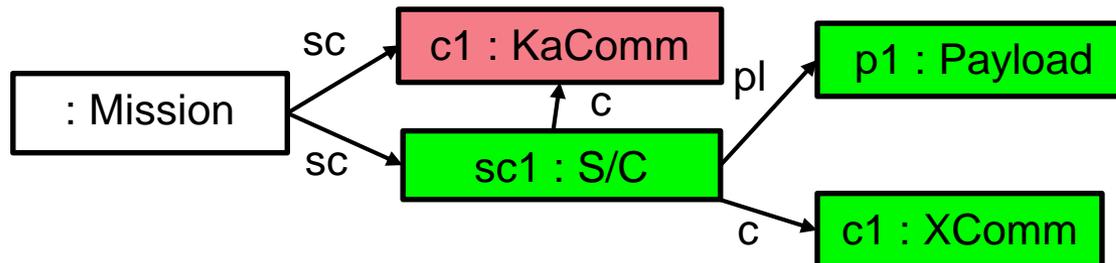


Individual y:



recombined to Mutation

New:



# Implementation

## Open Source Technologies Used in Implementation

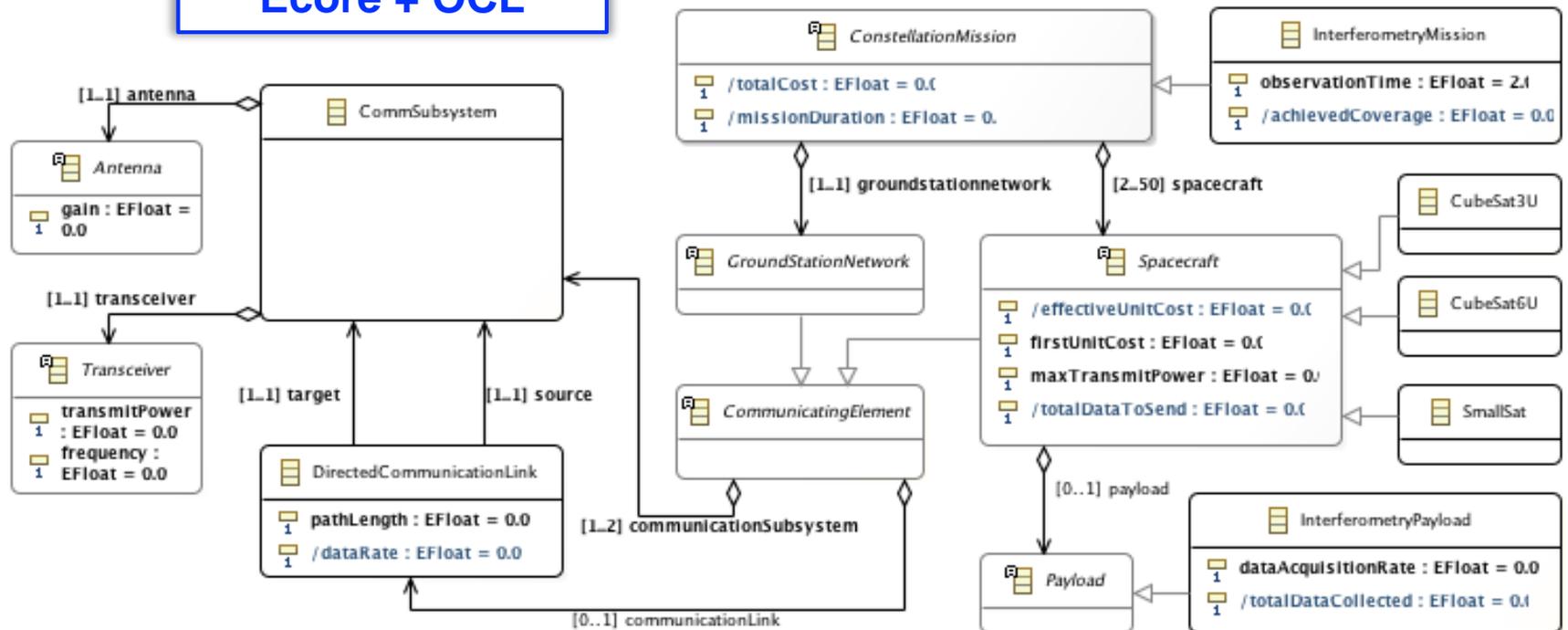
- Representation of Domain  
→ **Ecore / Eclipse EMF + OCL**
- Exploration Rules  
→ **Henshin**
- Analyses / Fitness Functions  
→ **Java**
- Optimization Using Genetic Algorithms  
→ **MOMoT, MOEA**



# Application to Case Study

## Representation of Domain (Excerpt)

Domain model in  
Ecore + OCL



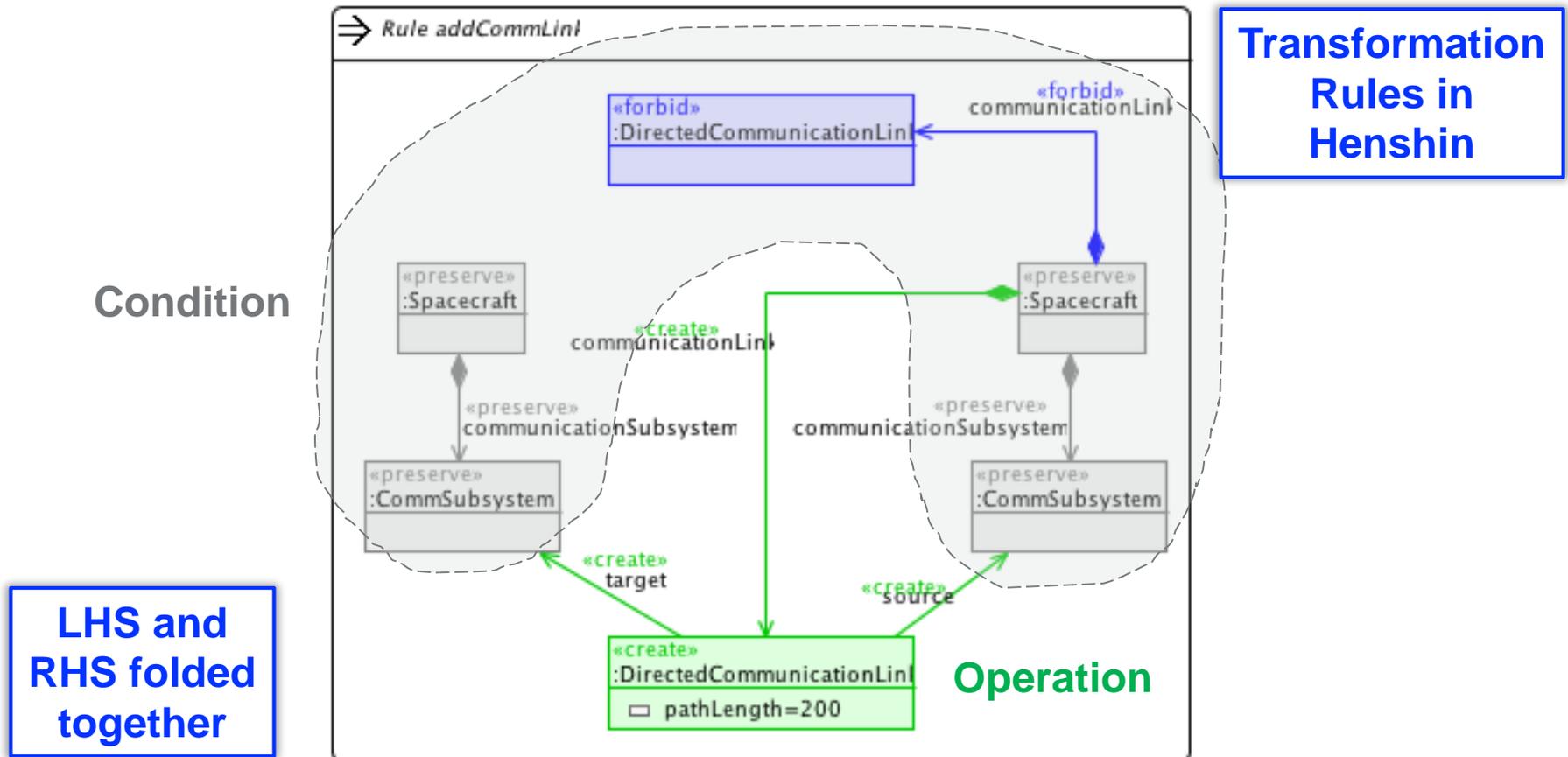
20 concepts, 9 associations, 15 attributes / parameters

>  $48^{10}$  possible models

Too many for  
exhaustive search

# Application to Case Study

Transformation Rule Example (Henshin Syntax): Add Comm. Link

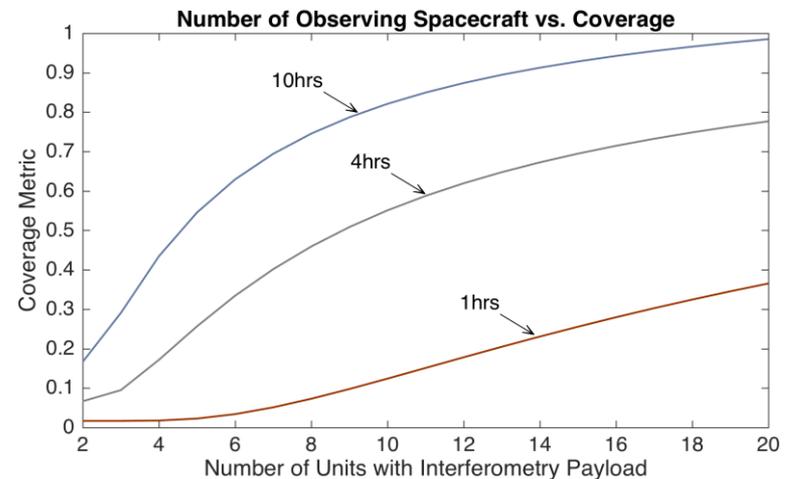
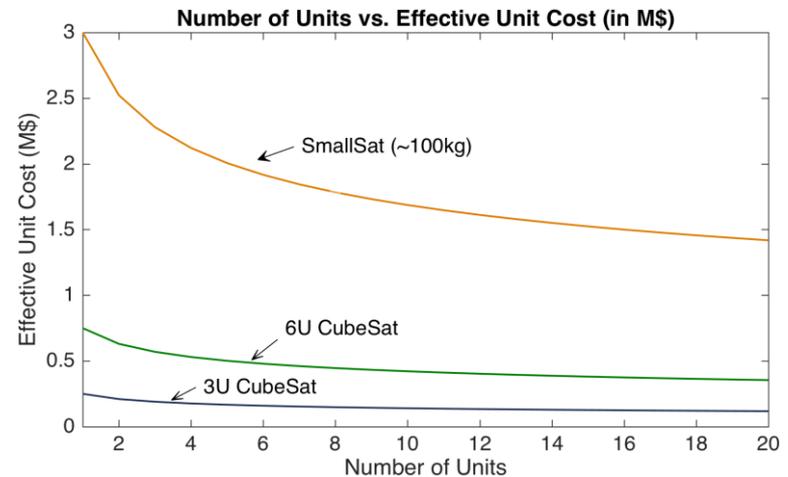


*In Prose: “Find 2 distinct spacecraft instances, and add a communication link between them”*

# Application to Case Study

- Three objectives:
  - Minimize **cost**
  - Maximize **coverage** (measure of scientific benefit)
  - Minimize **mission time**
- Typical link budget for data rates
- Data collection & transfer model
- Abstracted away orbit design through coverage model
- Experiment setup:
  - 16 transformation rules
  - 180 variables per individual
  - NSGA-II with population size 1000, and 1000 generations
  - 30 runs, 7 minutes each\*

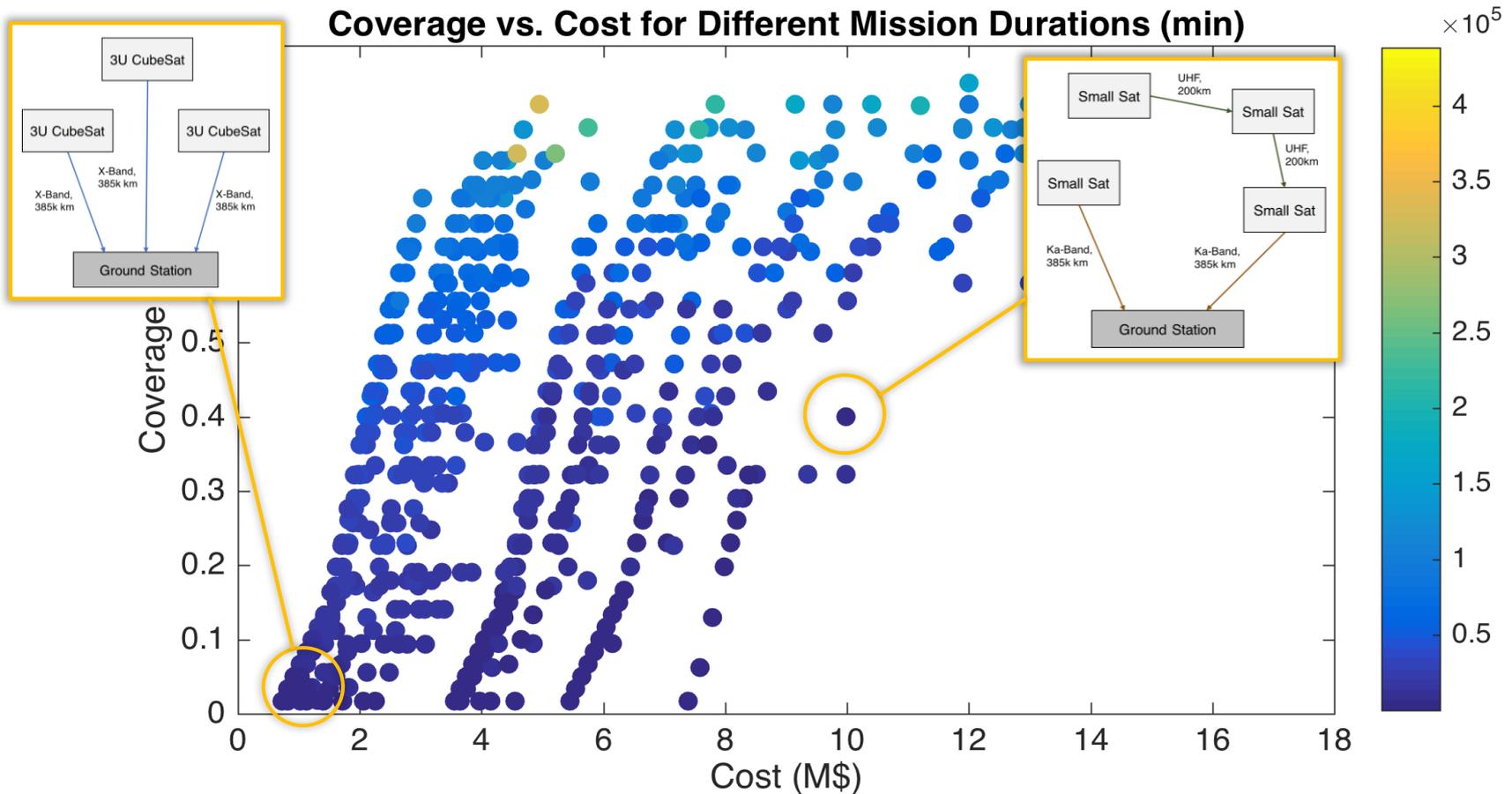
\* 8 core Intel i7 @ 2.7Ghz, 16GB DDR3 RAM



*Fictitious cost model (top)  
and coverage model (bottom)*

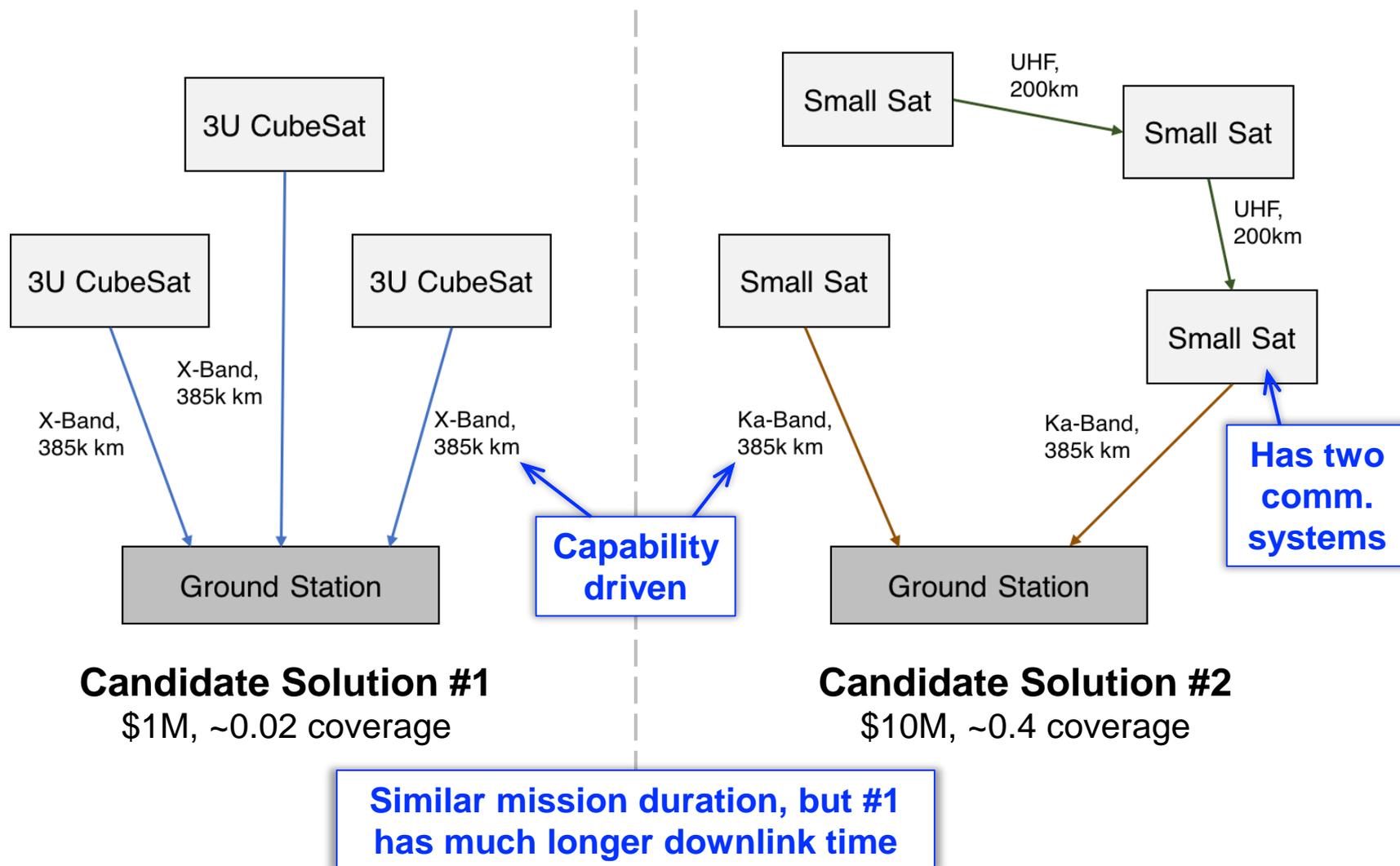
# Results from Application to Case Study

## Visualization of Trade Space



# Results from Application to Case Study

Examples of Pareto-Optimal (Nondominated) Solutions



# Conclusions

- Demonstrated method for **solving highly complex synthesis problems** and going beyond parametric trade space exploration
  - Generate diverse set of alternatives in a reasonable timeframe
  - Solutions generated based on abstract, description of problem
  - Enables designers to focus on **analysis**, and consider more options
- The generated candidate solutions can **help spark creativity**, but don't replace a designer
  - Method meant to **support** designers and the creative process
  - Many solutions sensible to experts; however, some may required slight modification or additional local search → **many constraints required**
- **Good performance** for relatively limited problems, but should investigate methods for subdividing problem further in future work



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[jpl.nasa.gov](http://jpl.nasa.gov)

Government sponsorship acknowledged. All technical data was obtained from publicly available sources and / or is fictitious.



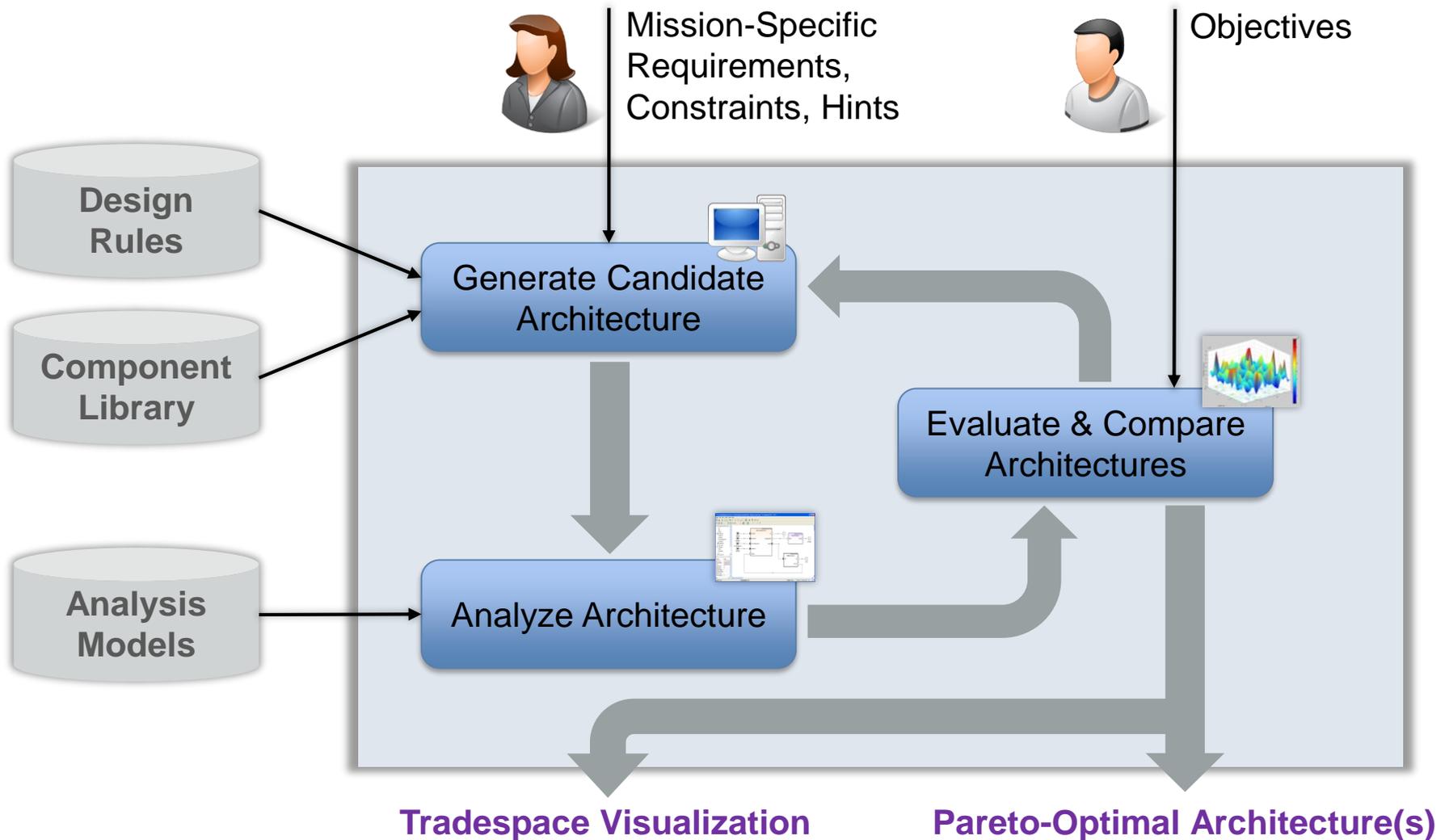
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# Backup Slides

IEEE Aerospace 2017 Presentation on *“Model-Transformation-Based Computational Design Synthesis for Mission Architecture Optimization”*

# Framework

## CDS for Mission Architecture Design



# Application to Case Study

## Link Calculations

- Derived from standard link budget, assuming above average noise due to expected interference from Moon

**Table 1. Computed communication rates. 385k km case assumes 72 dBi receive antenna gain for X-band, and 85 dBi for Ka-band (similar to DSN).**

<b>Transmitter Configuration</b>	<b>200 km</b>	<b>385k km</b>
<b>UHF, 3 W, 1 dBi</b>	5 Mbps	-
<b>X-Band, 5 W, 10 dBi</b>	1.6 Mbps	0.7 Mbps
<b>Ka-Band, 15 W, 25 dBi</b>	220 Mbps	80 Mbps

# Application to Case Study

## Cost Calculations

- Cost per spacecraft calculation incorporates a learning curve
- Assuming \$ 100,000 per hour of observation to estimate observation and data processing cost

$$c_i = c_{base,type(i)} \cdot n_{type(i)}^{-0.25} + c_{conf,i} \quad (5)$$

$$c_{total} = \sum_{i=1}^{n_{sc}} c_i + 100,000 t_{obs} \quad (6)$$

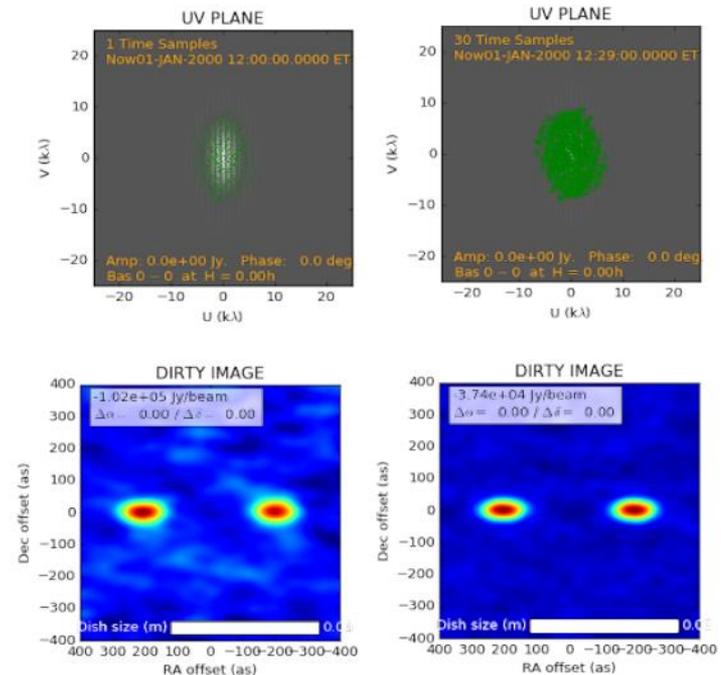
# Application to Case Study

## Coverage

- Simple coverage calculation

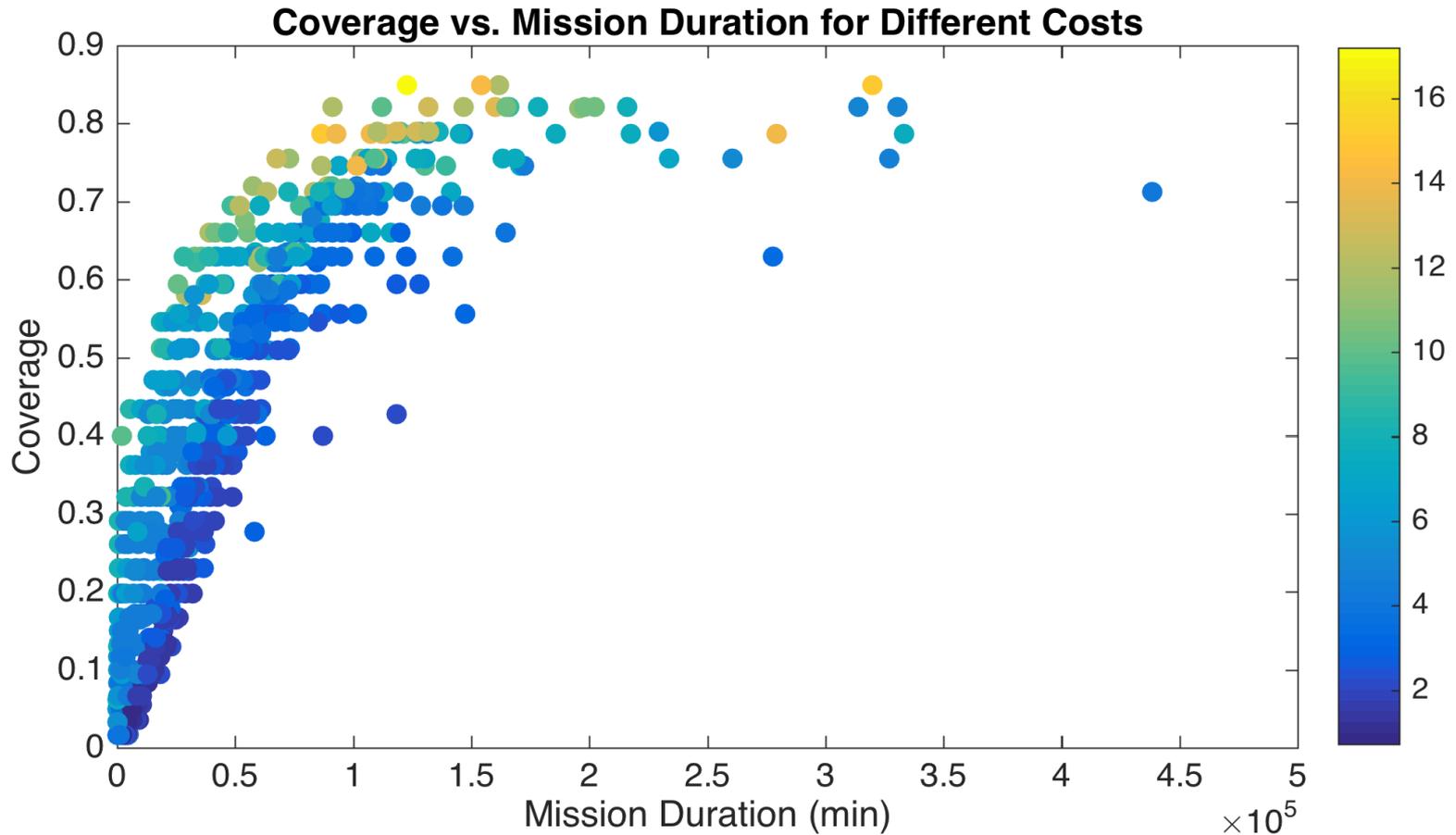
$$cov = \left(1 - \frac{2}{n_{obs}}\right)^{1+9(1/t_{obs})} + 0.05 \frac{t_{obs}}{3} \quad (1)$$

- Surrogate model that reflects trends observed from more sophisticated telescope array simulation performed by Alexander Hegedus (<https://github.com/alexhege/Orbital-APSYNSIM/>)



# Results from Application to Case Study

## Coverage vs. Mission Duration



# Results from Application to Case Study

## Cost vs. Mission Duration

