



Thrust Direction Optimization: Satisfying Dawn's Attitude Agility Constraints

AAS 13-343

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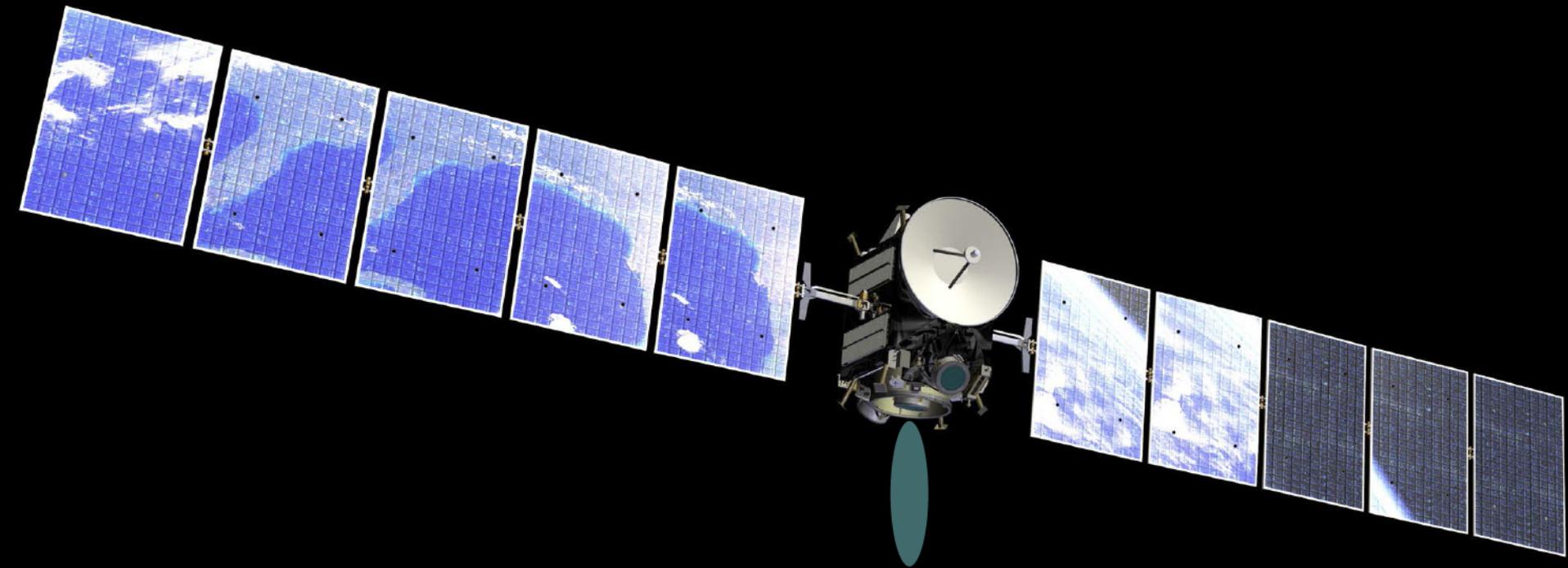
Jet Propulsion Laboratory

February 12, 2013

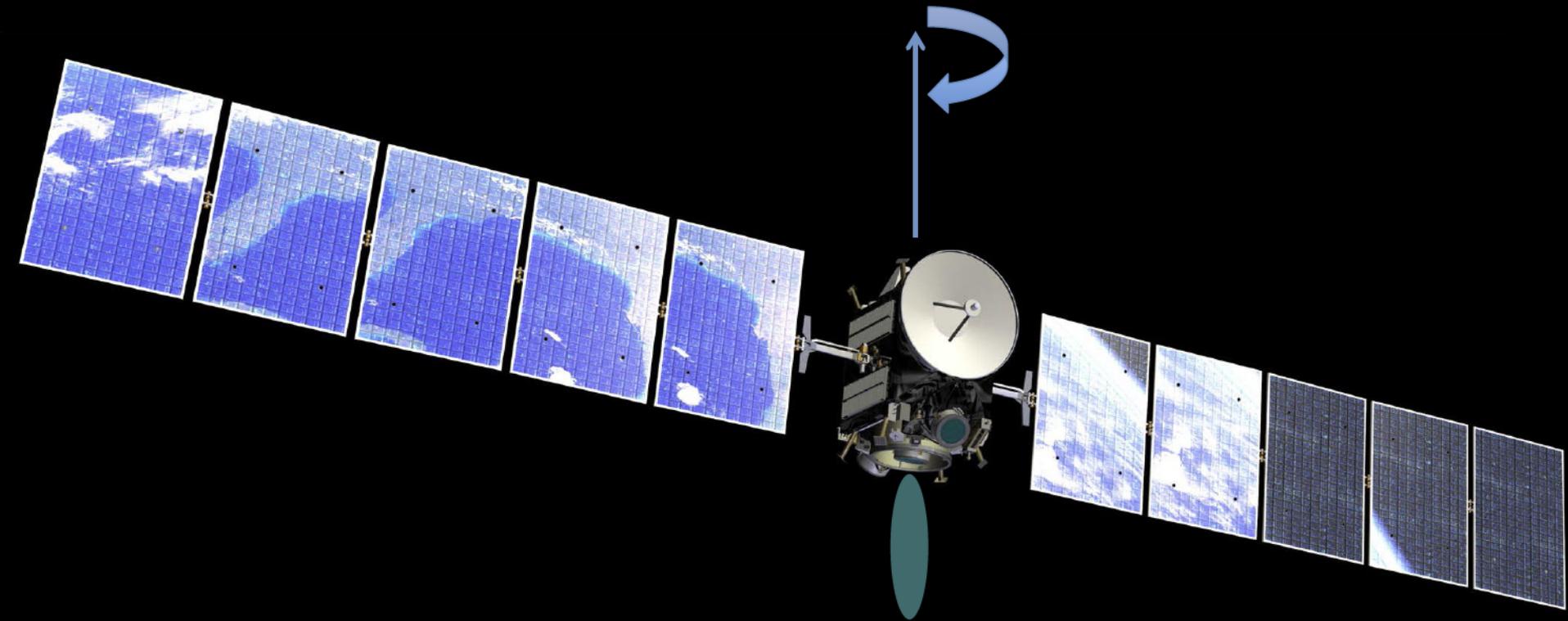
100 Km

A horizontal blue line representing a scale bar for 100 kilometers.

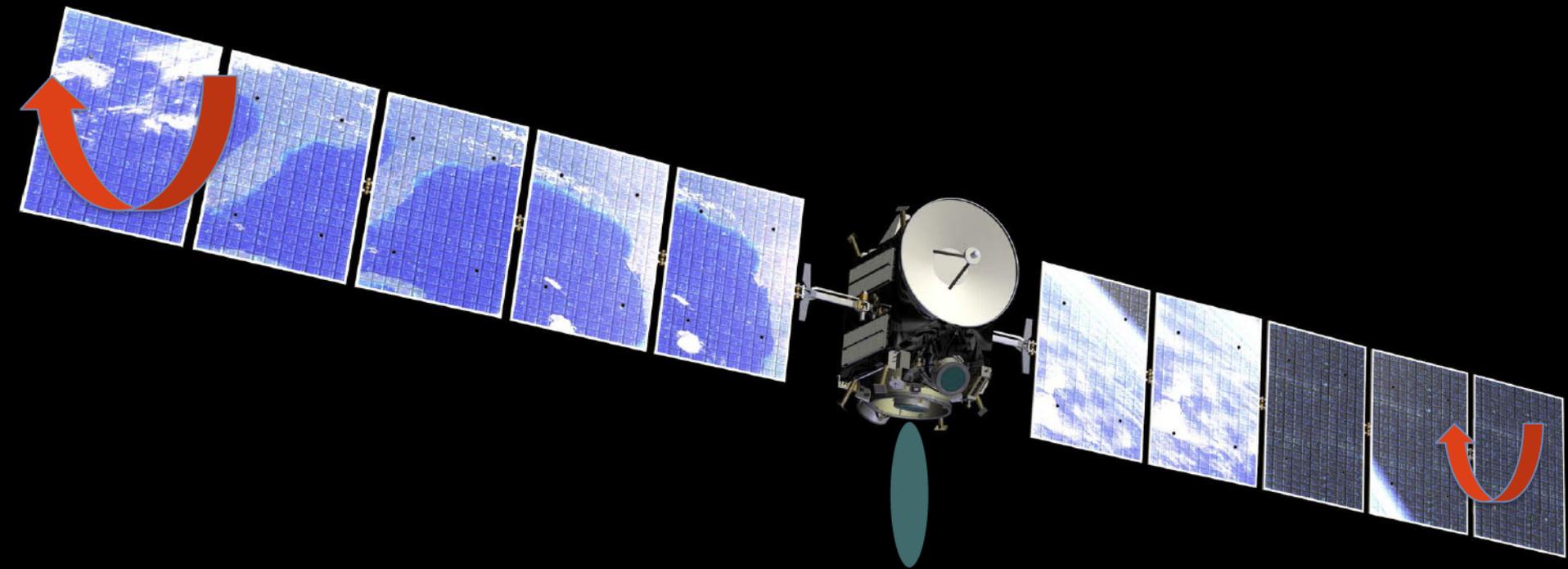
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- The long arrays create a large moment of inertia
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- Given a pointing (thrust) direction, maximize power by keeping the arrays orthogonal to the Sun:



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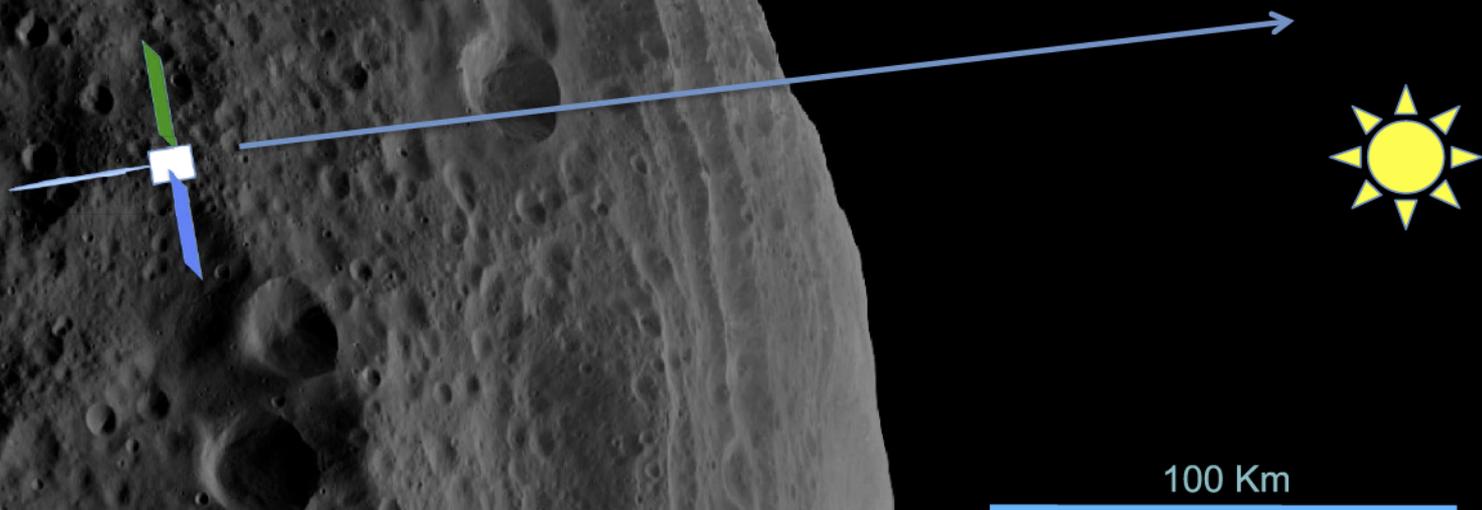


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 - Solar arrays are rotated



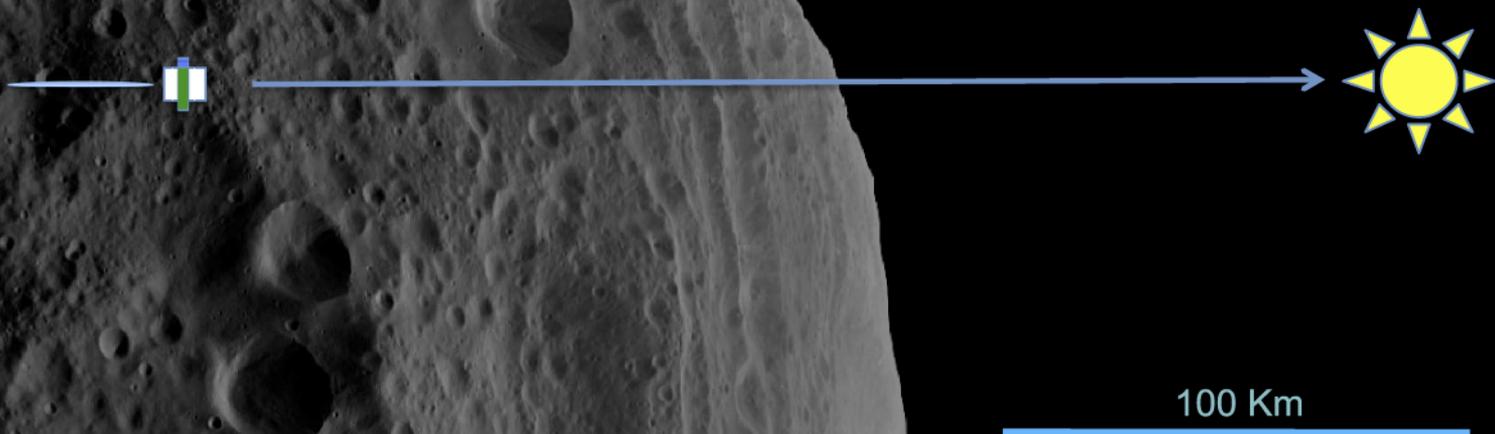
The Problem with Power Steering

- There are two “poles” that can require very rapid 180° attitude flips
- The flip involves the highest moment of inertial (solar arrays)
- The two poles are the Sun and Anti-Sun directions



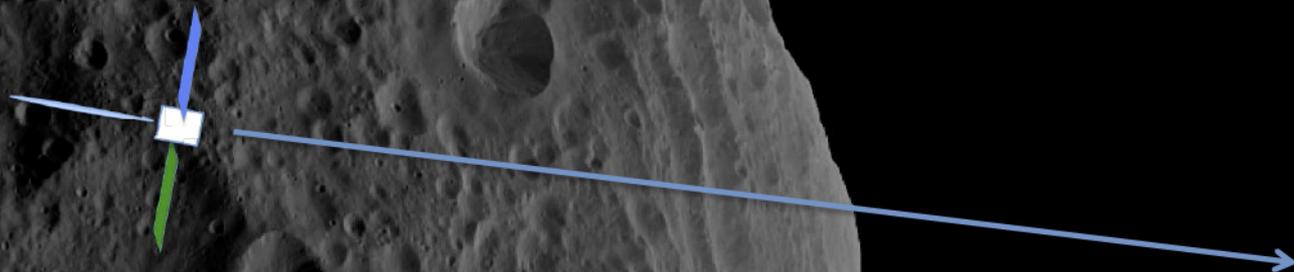
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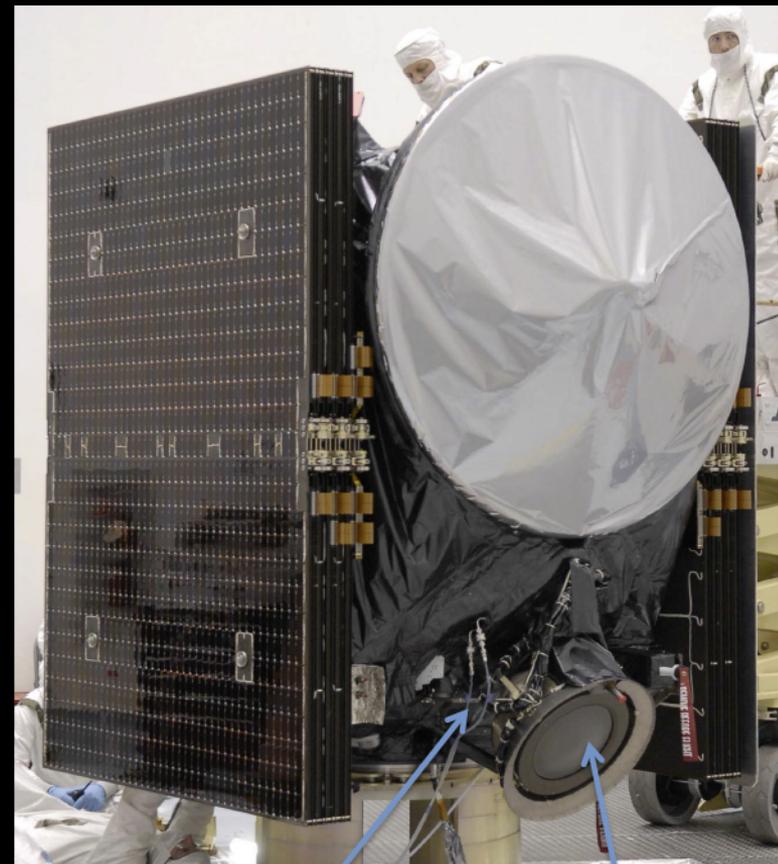


100 Km

Dawn's Attitude Control System

- Dawn's attitude was controlled using thrust vectoring in two axes perpendicular to thrust and reaction wheels parallel to thrust
- Thrust vectoring was achieved with gimbals on the ion thrusters
- max excursion was $< 5^\circ$
- Thrust ~ 50 [mN]
- Spacecraft ~ 1200 [kg]

Weak Control: Low Agility

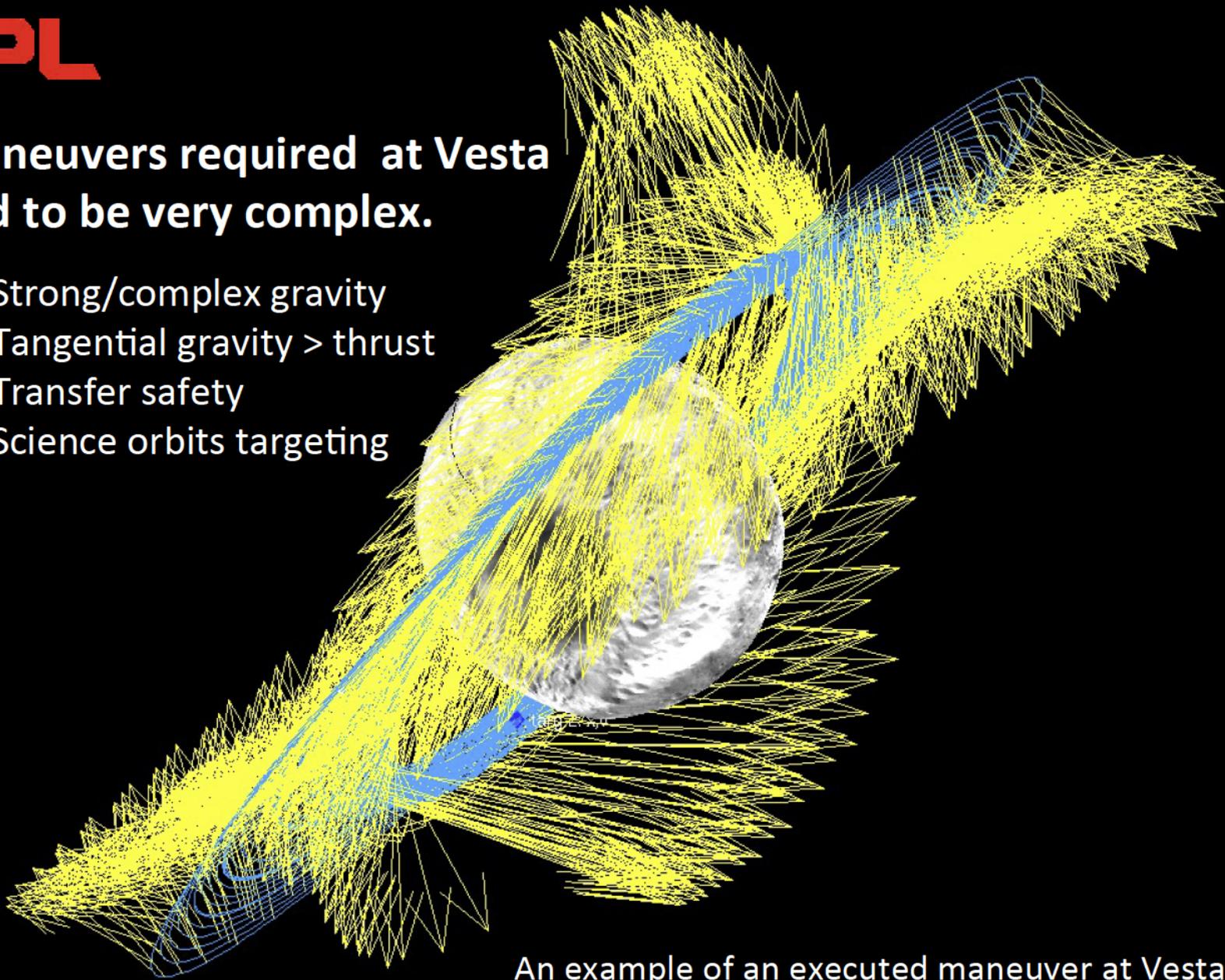


Gimbals

Ion Thruster

Maneuvers required at Vesta had to be very complex.

- Strong/complex gravity
- Tangential gravity $>$ thrust
- Transfer safety
- Science orbits targeting



An example of an executed maneuver at Vesta, November 2011. Yellow vectors are thrust directions

Maneuver Design At Vesta

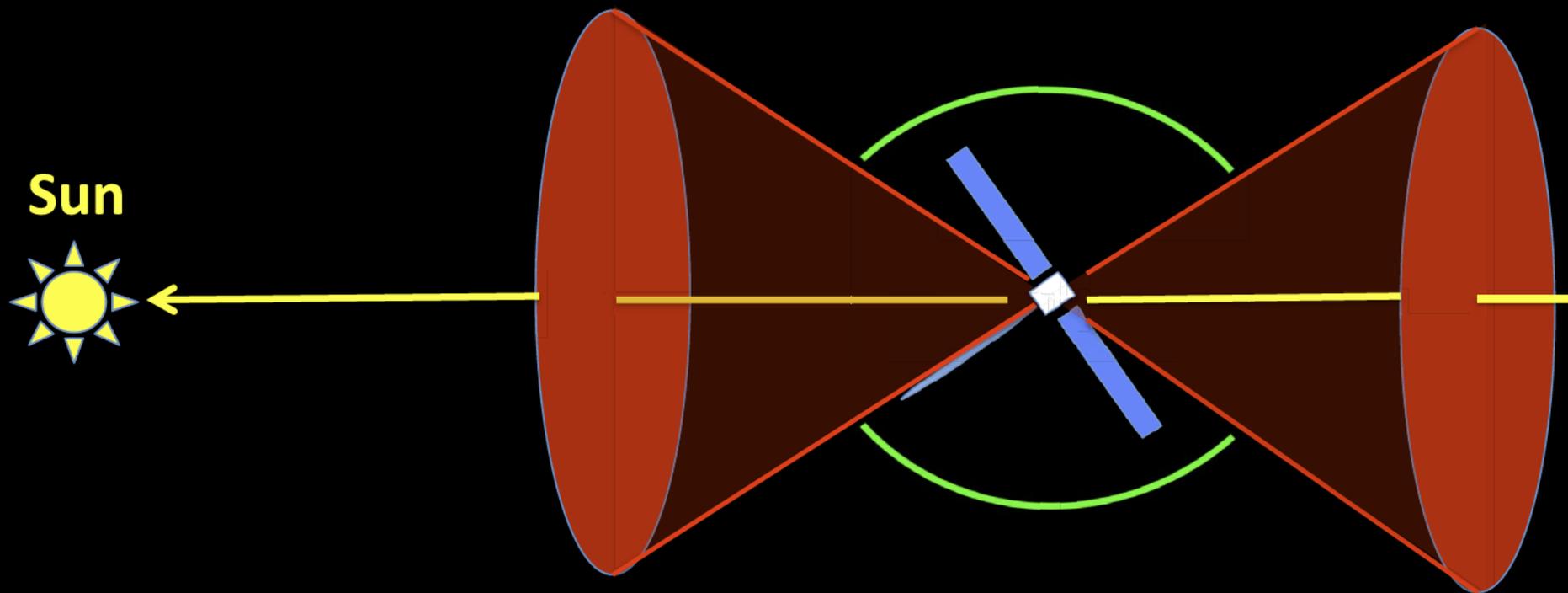


- Software: “Mystic” uses Static Dynamic Optimal Control
- Based on Bellman’s Principal of Optimality and Dynamic Programming (not NLP or calculus of variations)
- Very-high fidelity trajectory design tool used to design all maneuvers (High order gravity harmonics, multi-body gravity, radiation pressure, nonlinear thruster model, desat ΔV , etc.)
- Many operational constraints
- Original objective functions: Minimum Propellant or Minimum Time.

Attitude Agility Constraints

- **Must constrain thrust direction time evolution**
- Attitude agility constraints are:
 - **Not analytic**
 - **Not predictable** (unknown spacecraft momentum)
 - Monte-Carlo analysis necessary to evaluate fly-ability
- General rules exist to improve chances of fly-ability
 - Thrust “further” from Sun and Anti-Sun directions
 - Make attitude rates (accelerations) lower
 - Keep thrust direction movement continuous!

- Cone angle exclusion constraints do not work
 - Result in high accelerations
 - Discontinuous thrust directions
 - Does not address high rates or accelerations



Objective Function:

$$J(v, w) = \int_{t_o=w_1}^{t_f=f(w)} F(x(t), v(t), w, t) dt + \sum_{i=1}^M H_i(x(t_i), v(t_i), w, t_i) + G(x(t_f), v(t_f), w, t_f)$$

State Equation:

$$\frac{dx(t)}{dt} = T(x(t), v(t), w, t)$$

Initial Condition Function:

$$x(t_0) = \Gamma(w)$$

STATE: $x(t)$ = s/c position, velocity, mass

CONTROL: $v(t)$ = thrust vector

CONTROL: w = initial time, flight time, initial state

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So Called "3 DOF" model

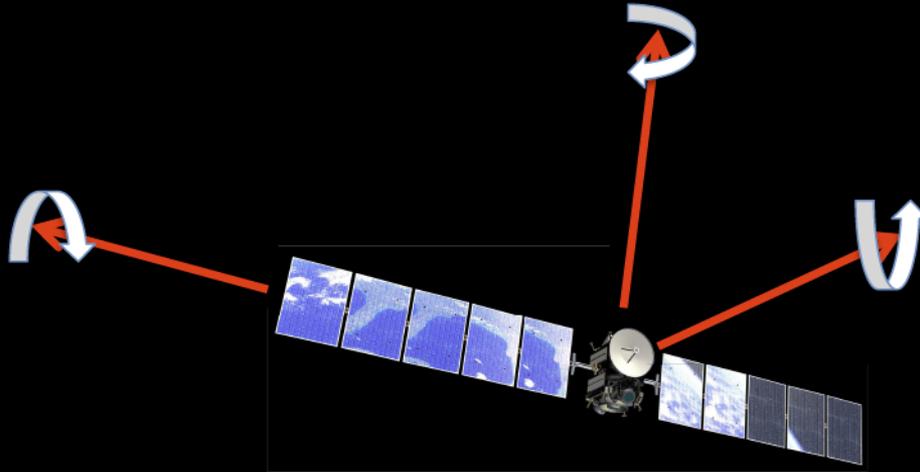
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6 Degree of Freedom Model

- Include 3 attitude angles as part of the state vector



- Natural formulation for constraining attitude rate, accel.
- Account for attitude even when not thrusting
- Complexity of formulation make initial guesses difficult
- Many more local minima from spacecraft revolution
- Power steering algorithm will also create local minima
- **Essentially need to know the answer before starting!**

- Sought a new formulation with the advantages of 3 DOF
 - Fewer local minima
 - Simple initial guesses
- Provide ability to manipulate thrust directions and attitude rates
- Solutions must exhibit thrust direction continuity and smoothness

- (1) Select direction(s) in some frame**
- (2) Find a thrust profile minimally or maximally far away**
- (3) Still achieve all other constraints and state targets**

Direction Attractor

$$\min_{v,w} \int_{t \in \tau} \left[1 - \hat{v}(t) \cdot \hat{D}(x(t), v(t), w, t) \right]^2 dt$$

Thrust

Direction Objective

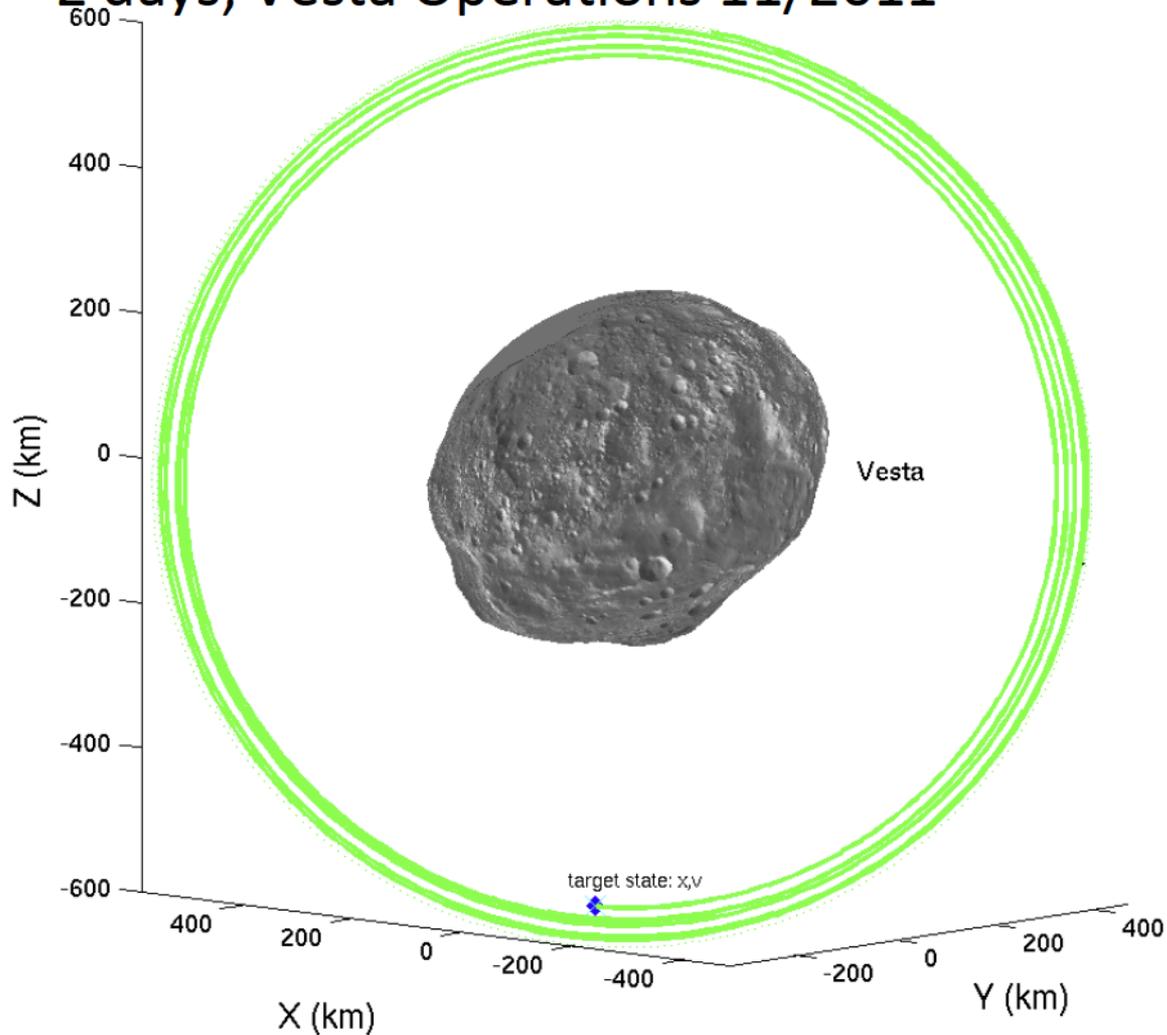
Pole Repulsor

$$\min_{v,w} \int_{t \in \tau} \left[1 - (\hat{v}(t) \times \hat{S}(x(t), v(t), w, t)) \cdot (\hat{v}(t) \times \hat{S}(x(t), v(t), w, t)) \right]^n dt$$

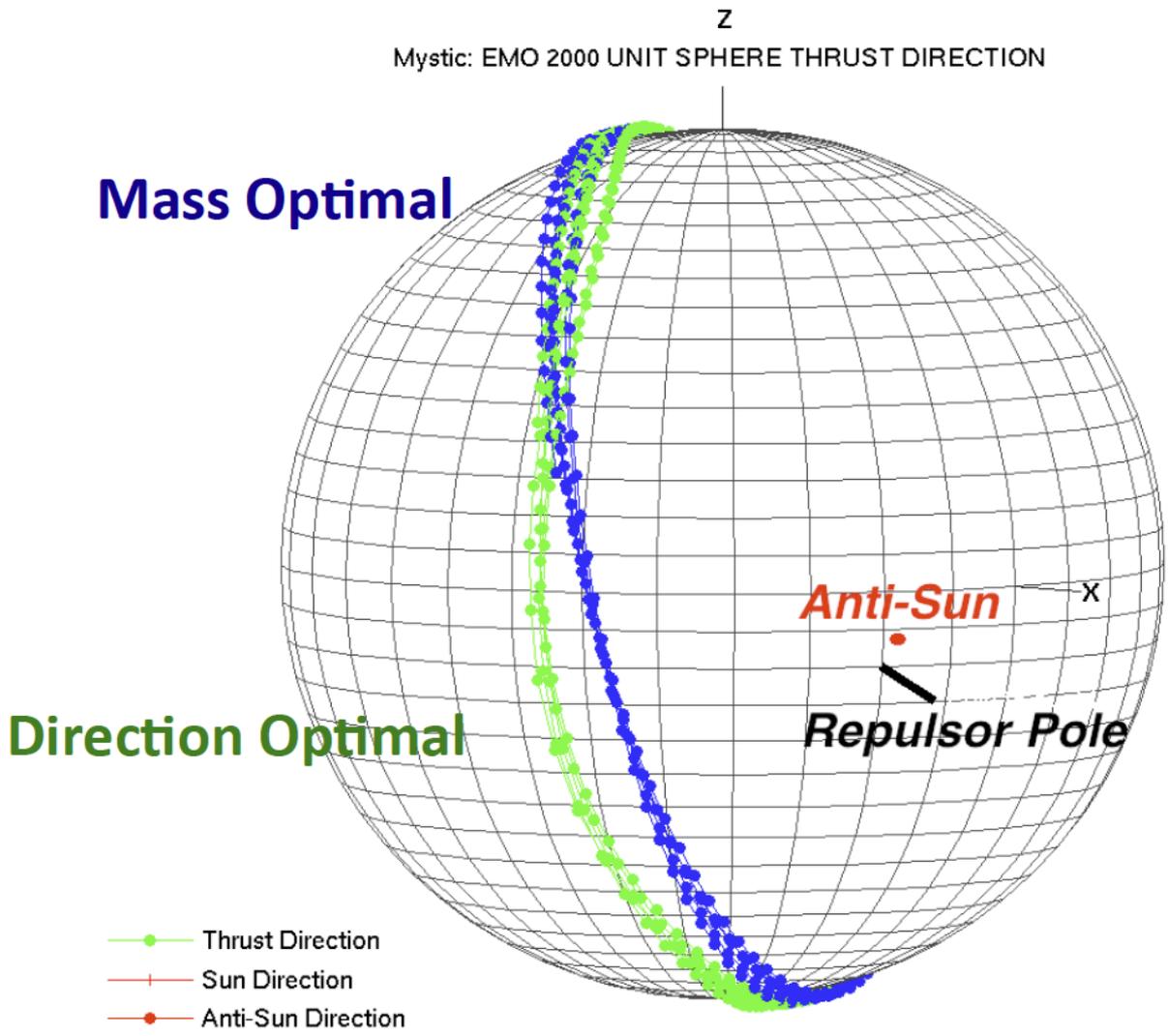
Attitude Pole to Avoid

Direction Optimization Example

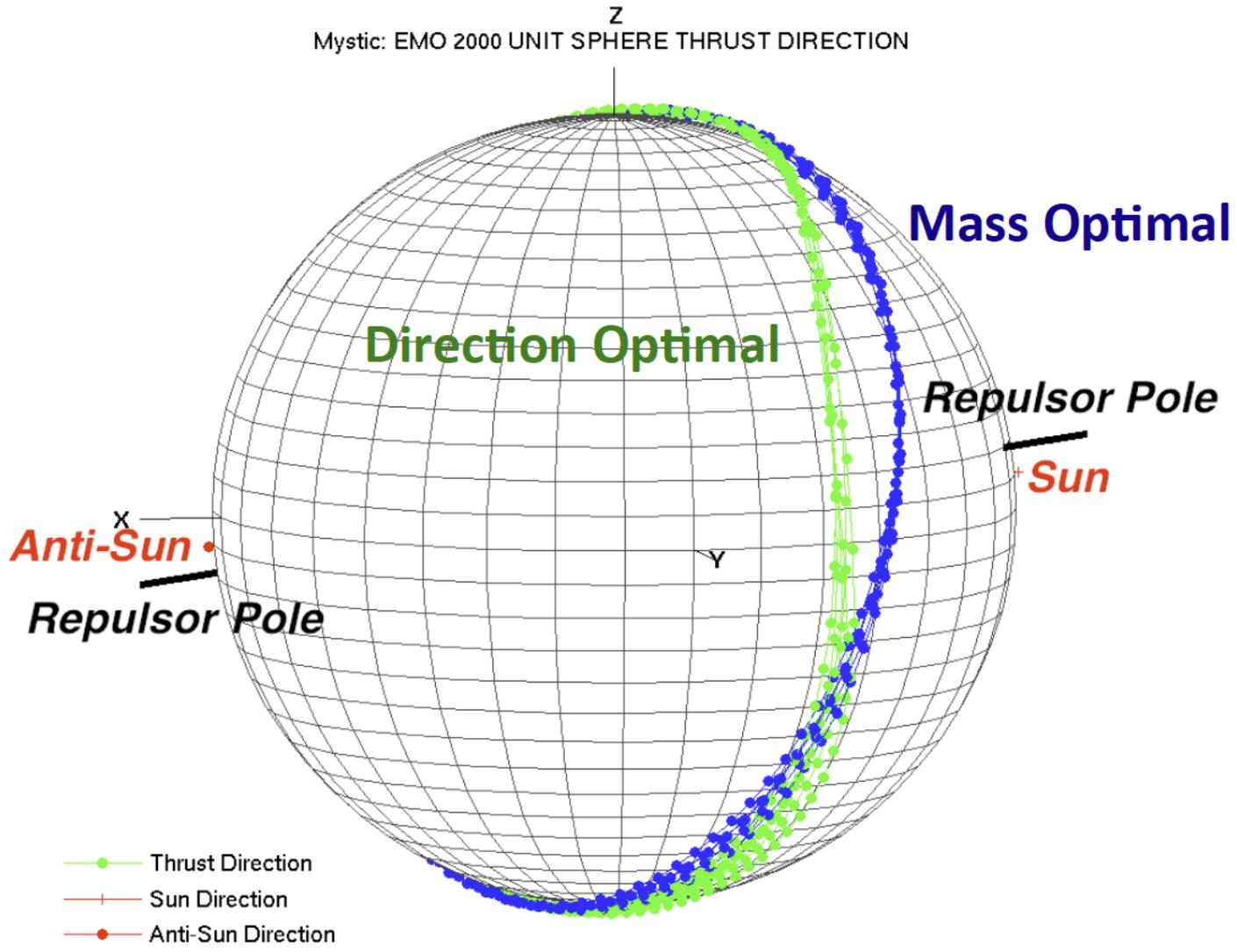
R= 640 to 580 [km] transfer, 7 revolutions around Vesta, Time of flight = 2 days, Vesta Operations 11/2011



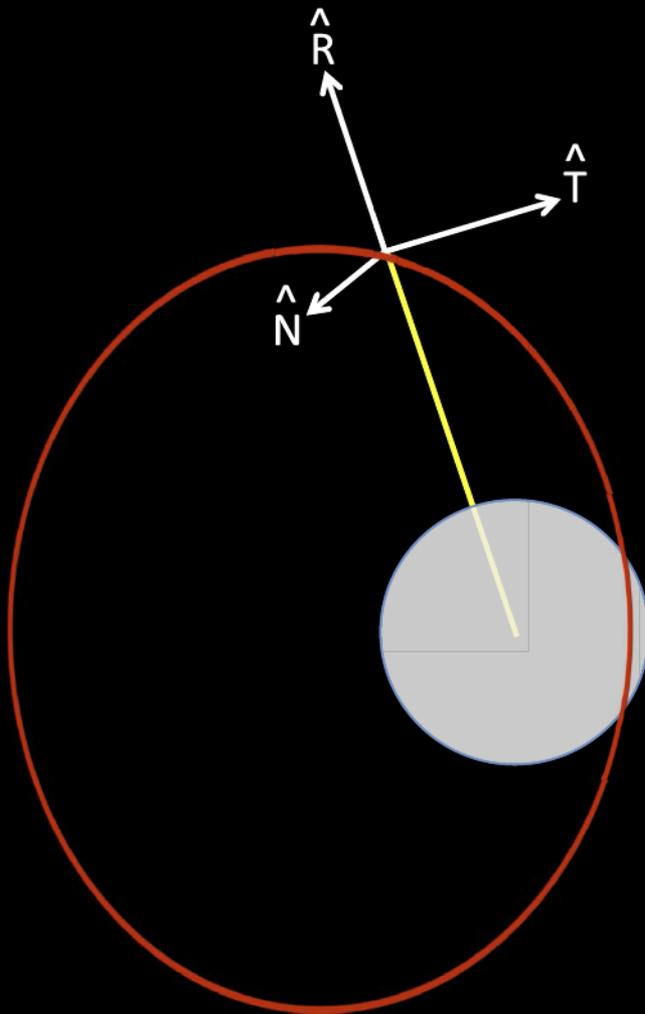
Pole Repulsor Example



Pole Repulsor Example



Radial-Normal-Transverse Frame



Rotating with S/C radius vector:

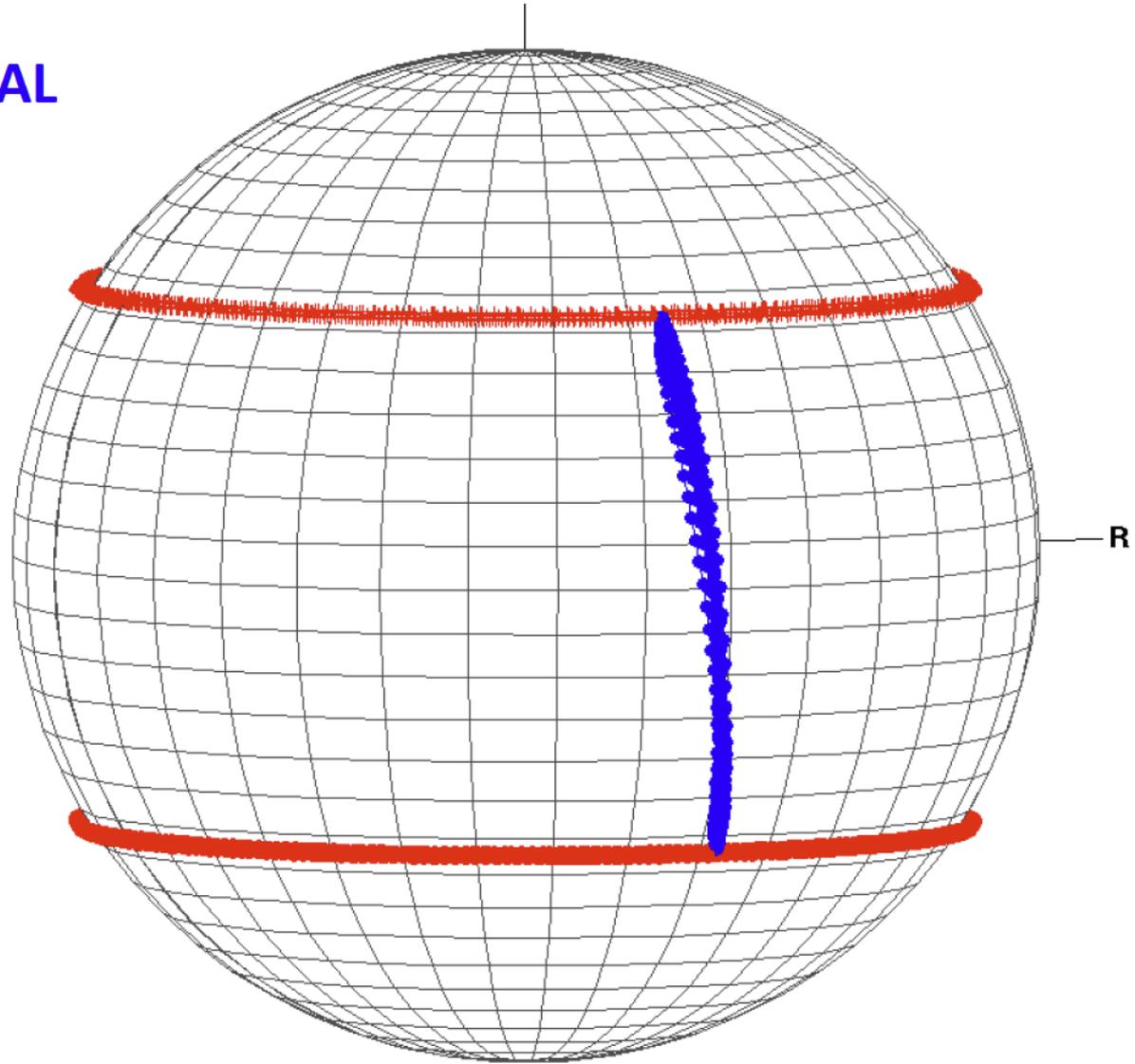
\hat{R} : radial direction

\hat{T} : Transverse direction = local horizontal nearest velocity direction

\hat{N} : orbit normal = $\hat{R} \times \hat{T}$

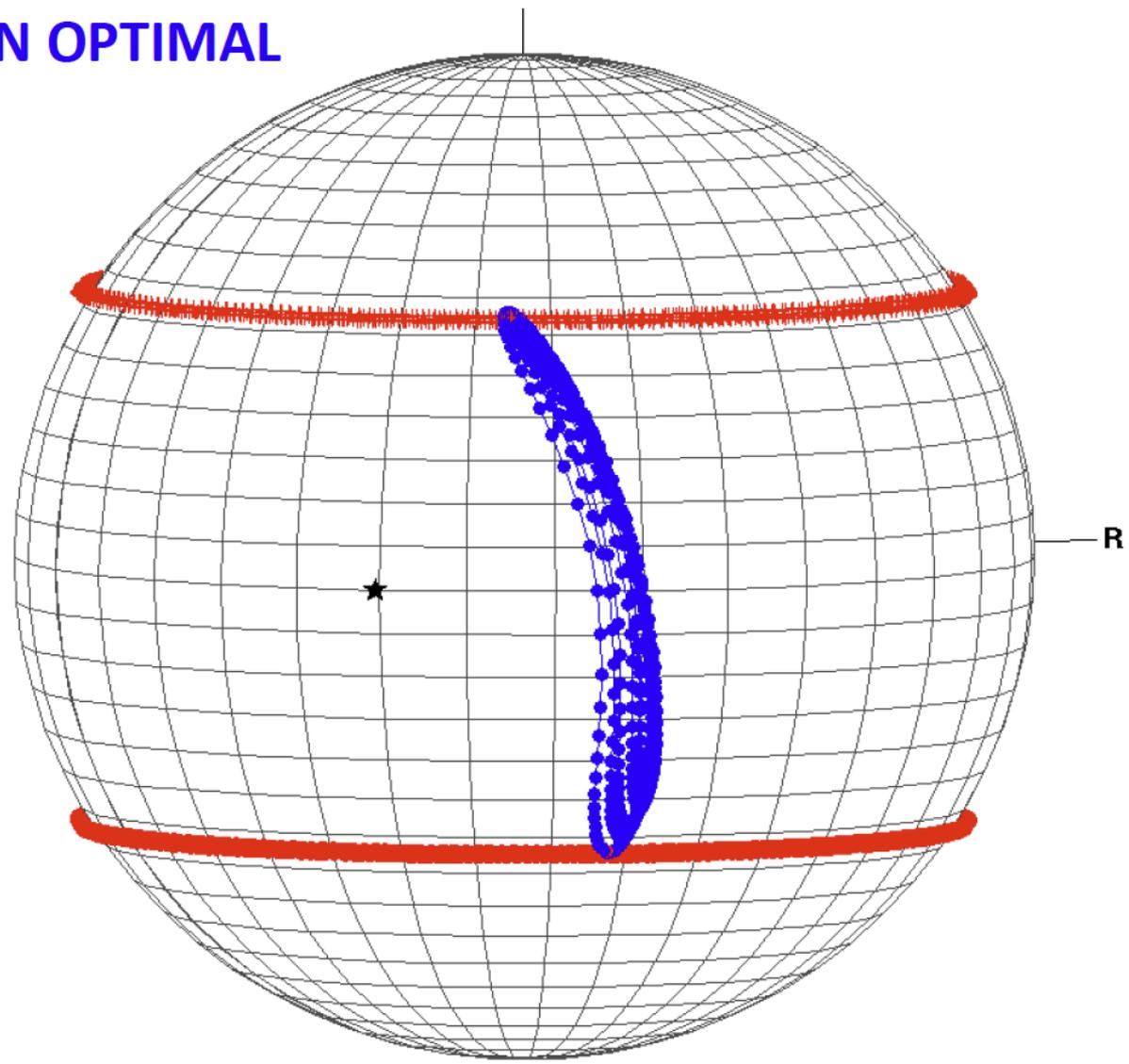
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Mystic: Vesta RTN UNIT SPHERE THRUST DIRECTION

MASS OPTIMAL



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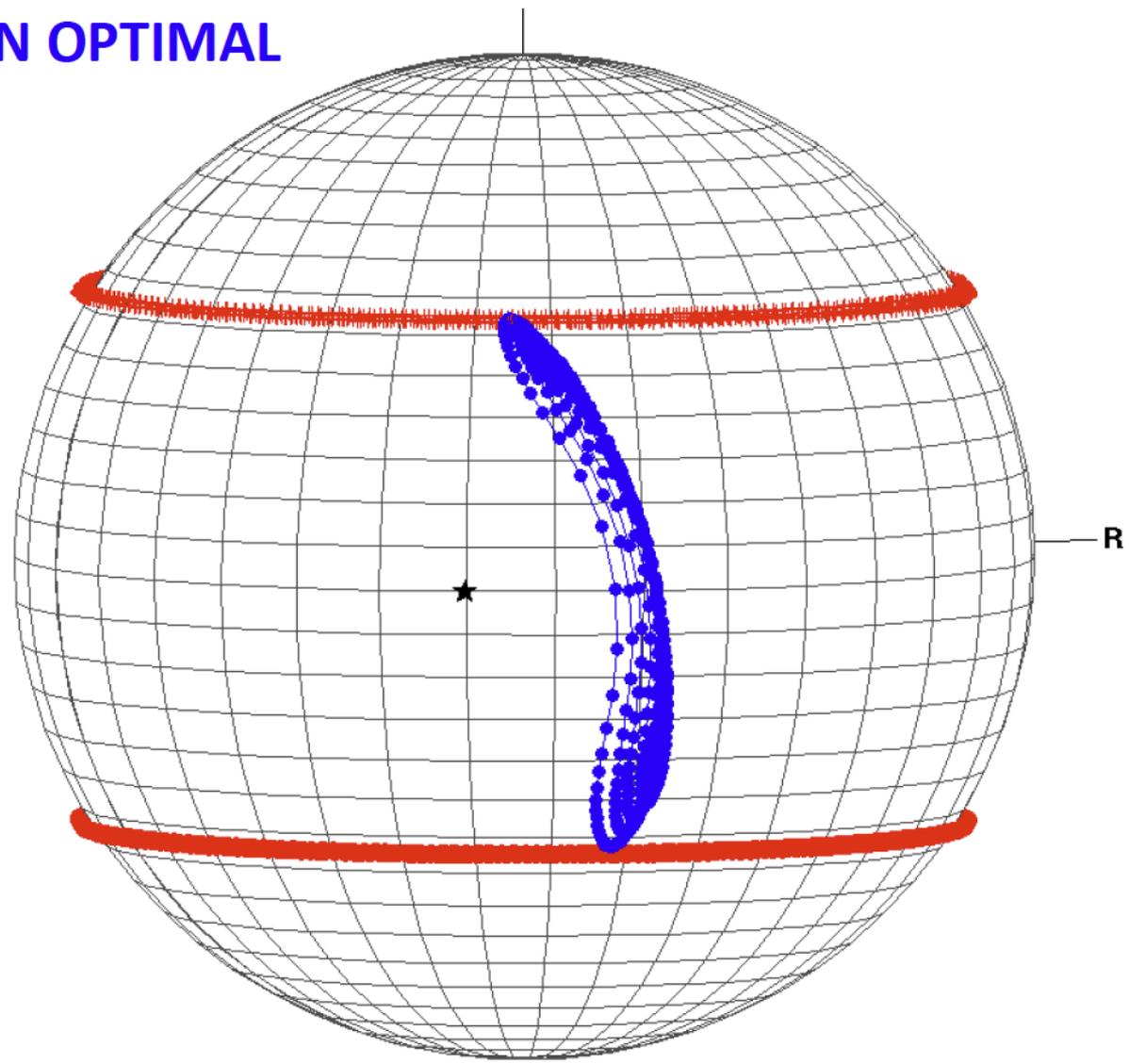
RTN DIRECTION OPTIMAL



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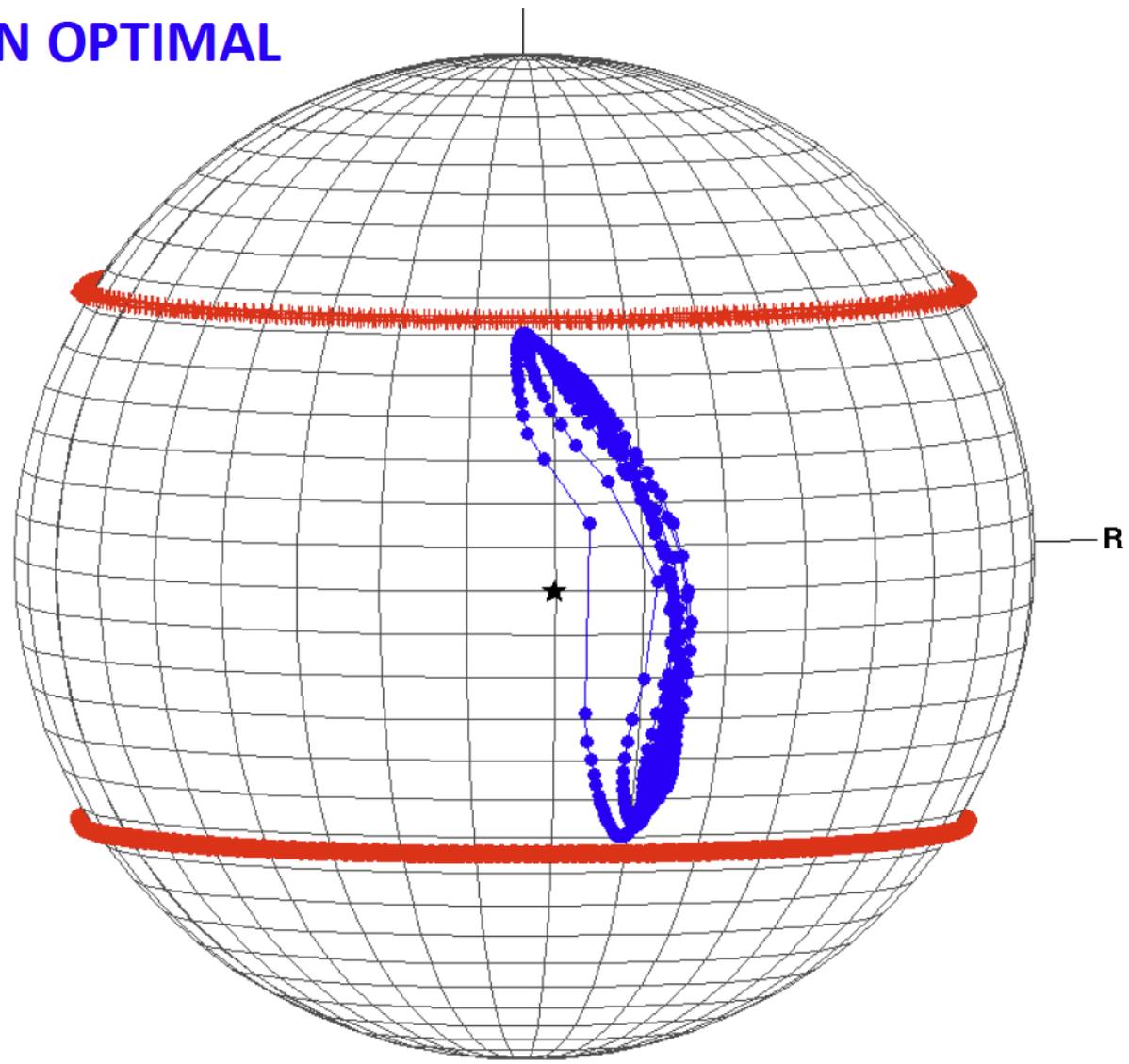
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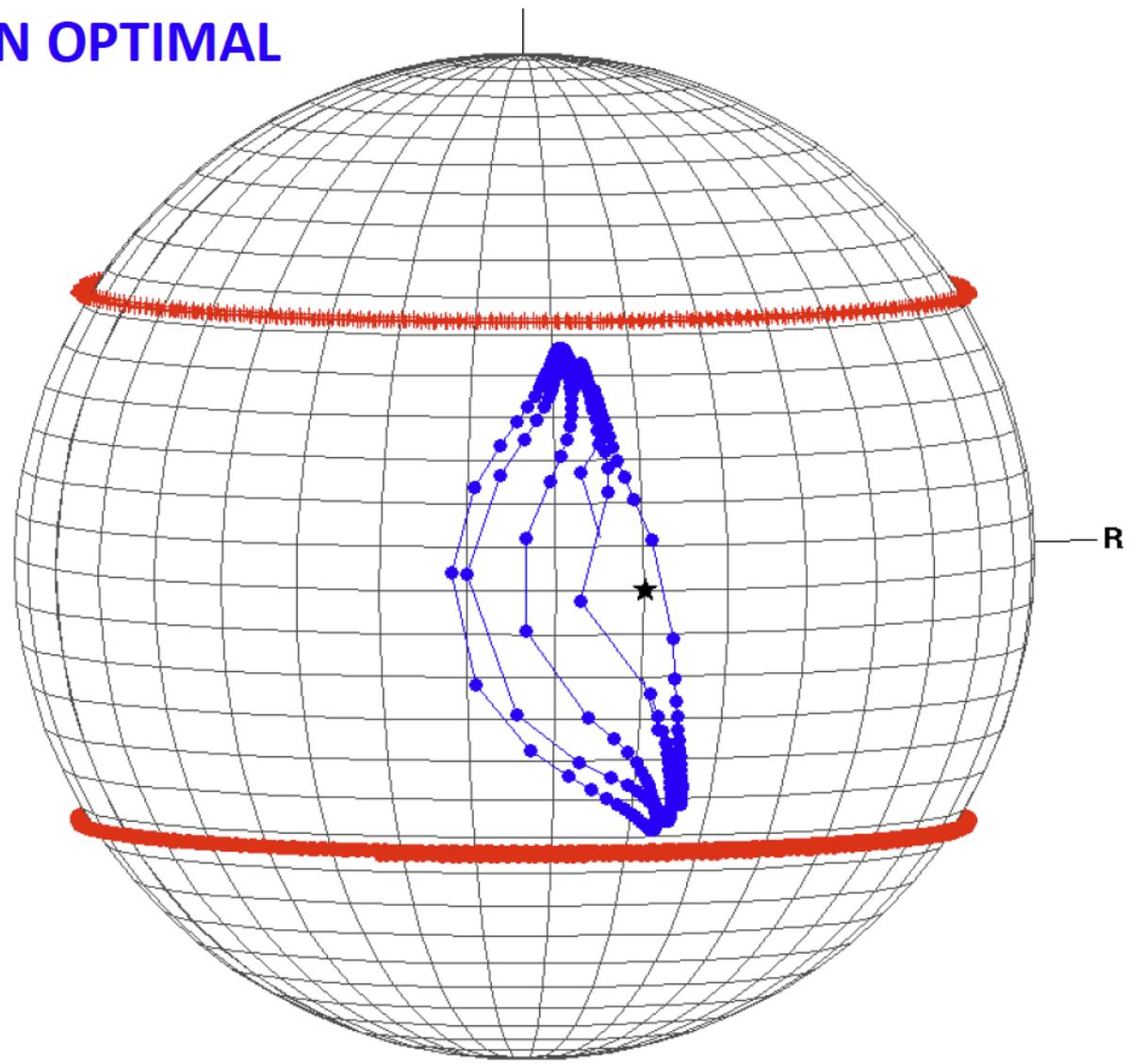
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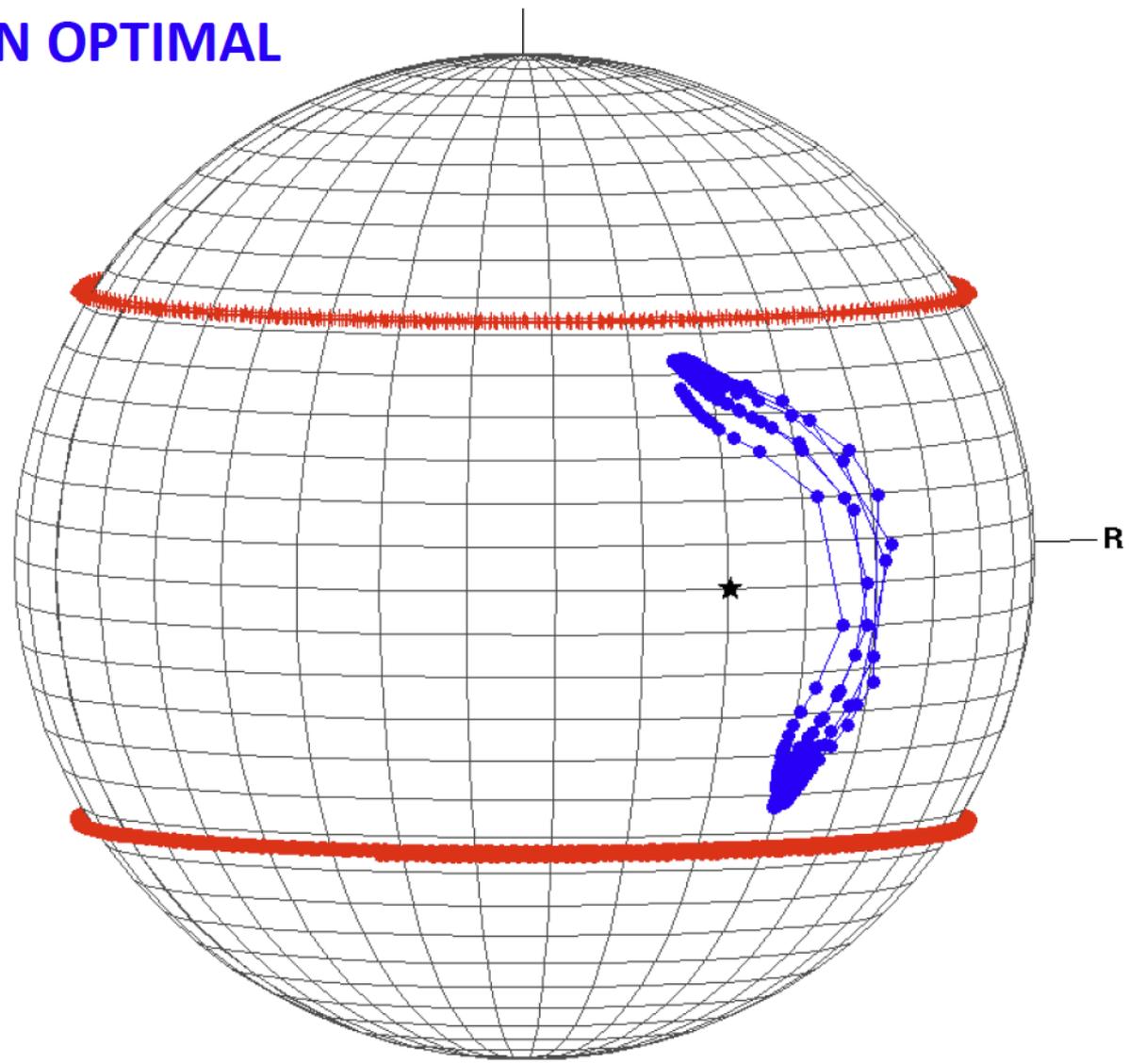
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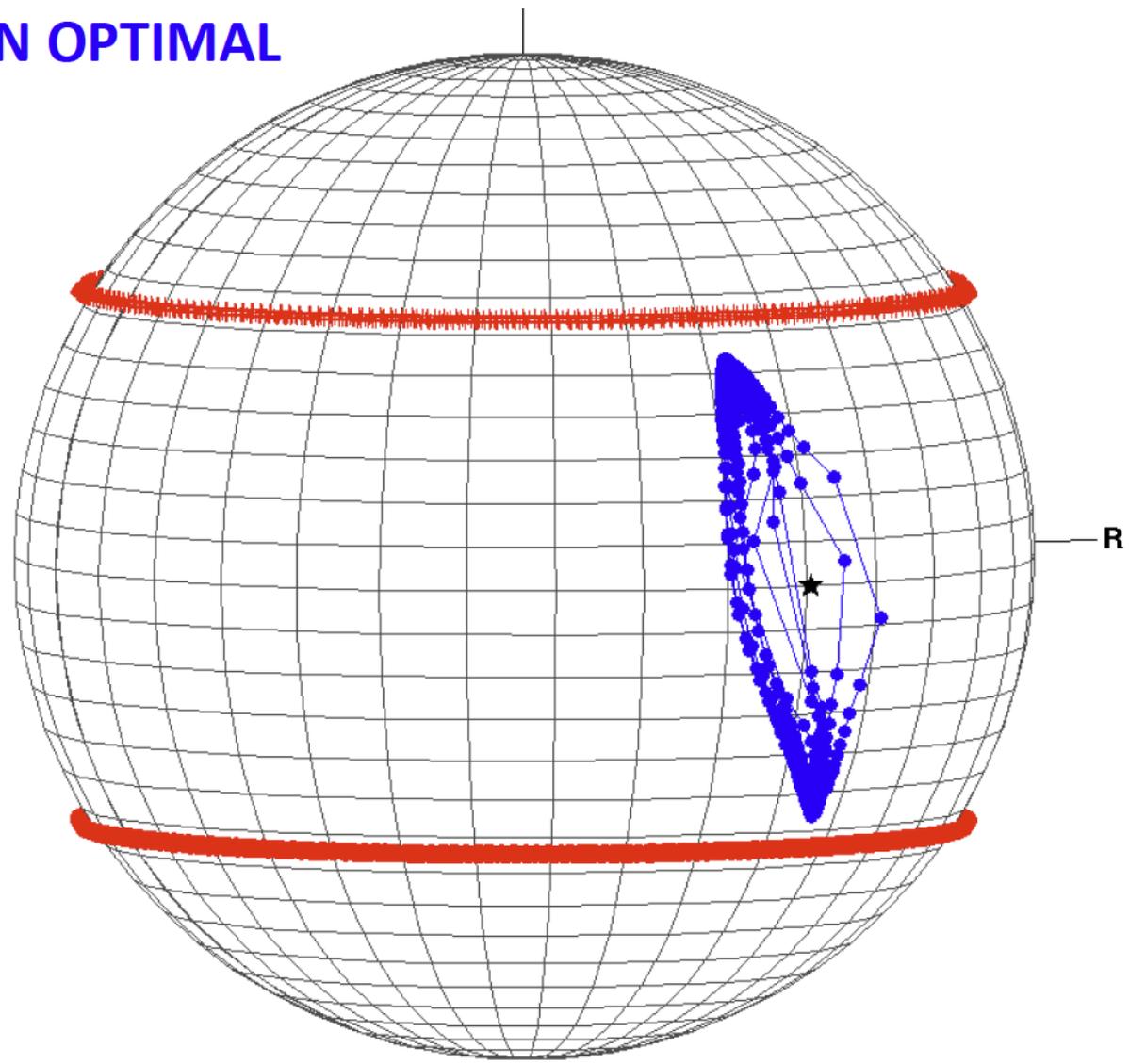
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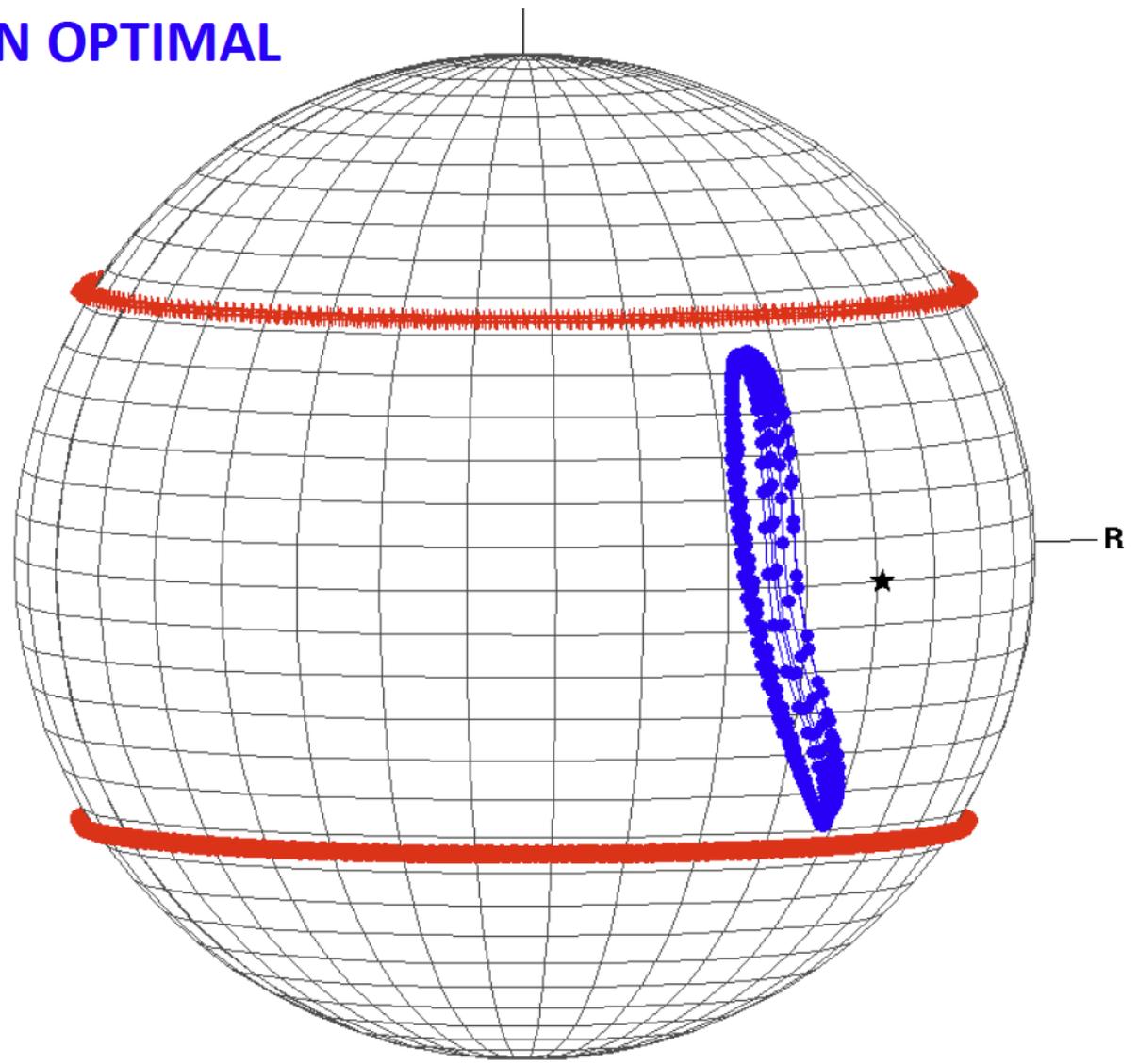
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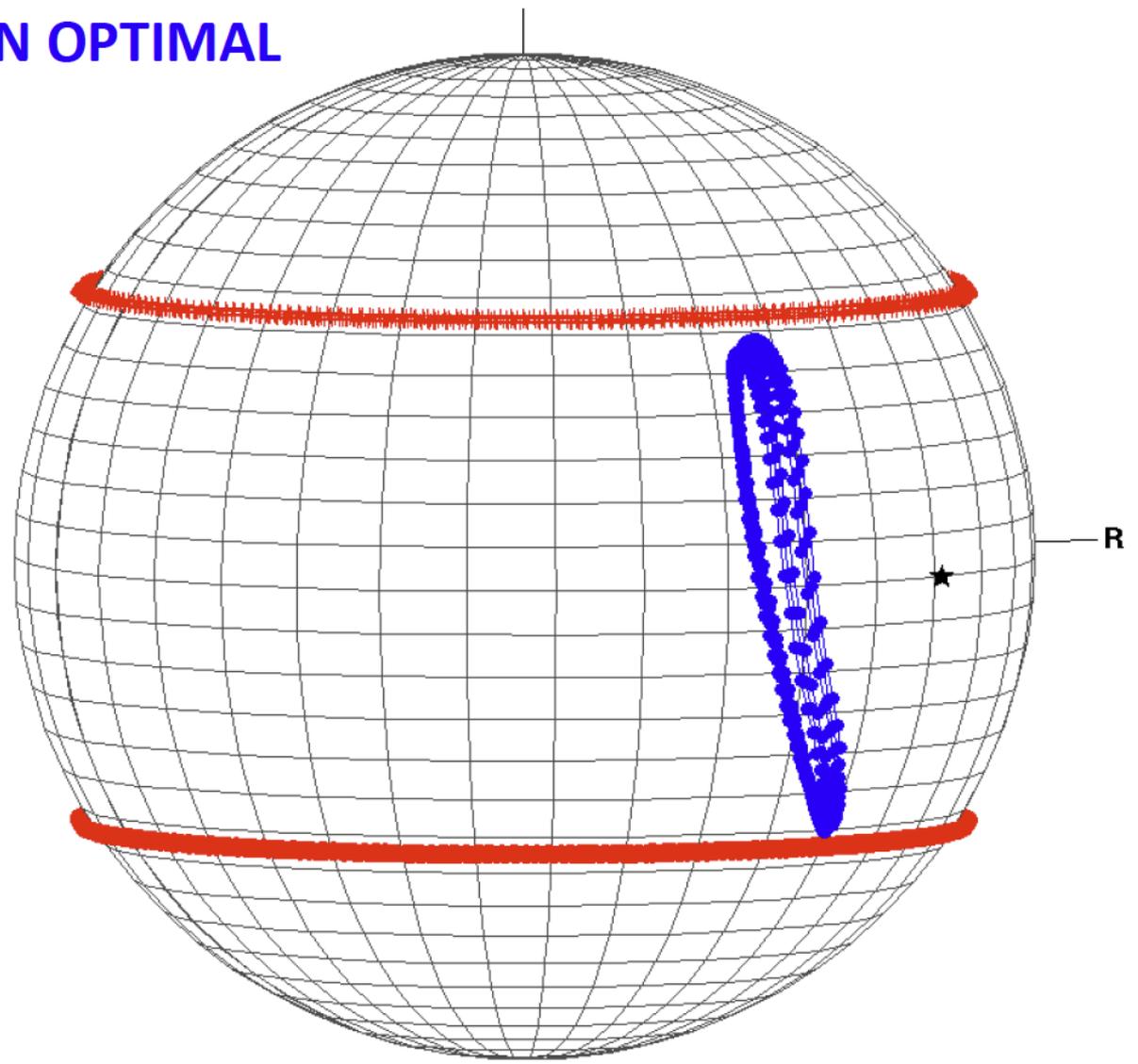
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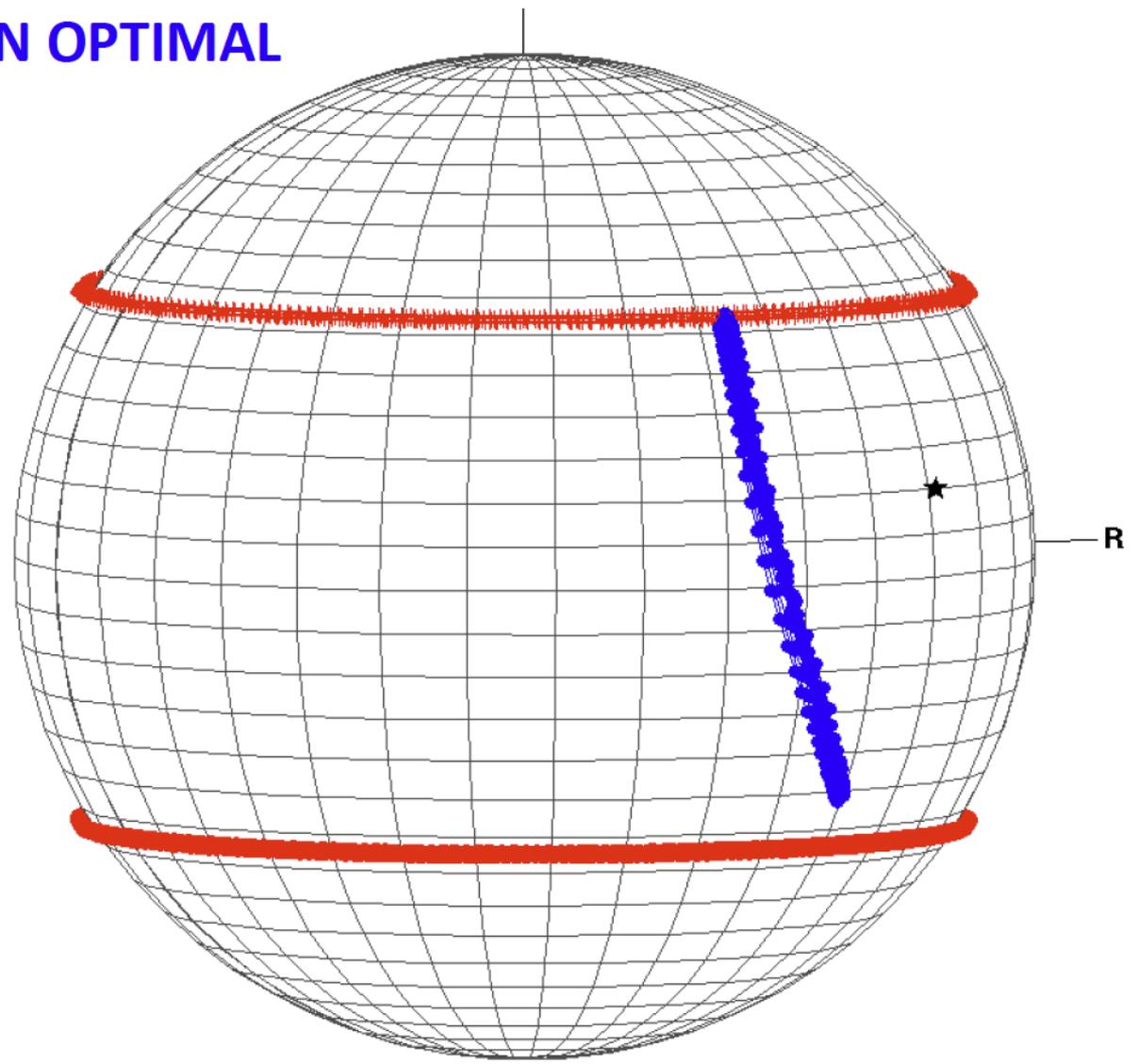
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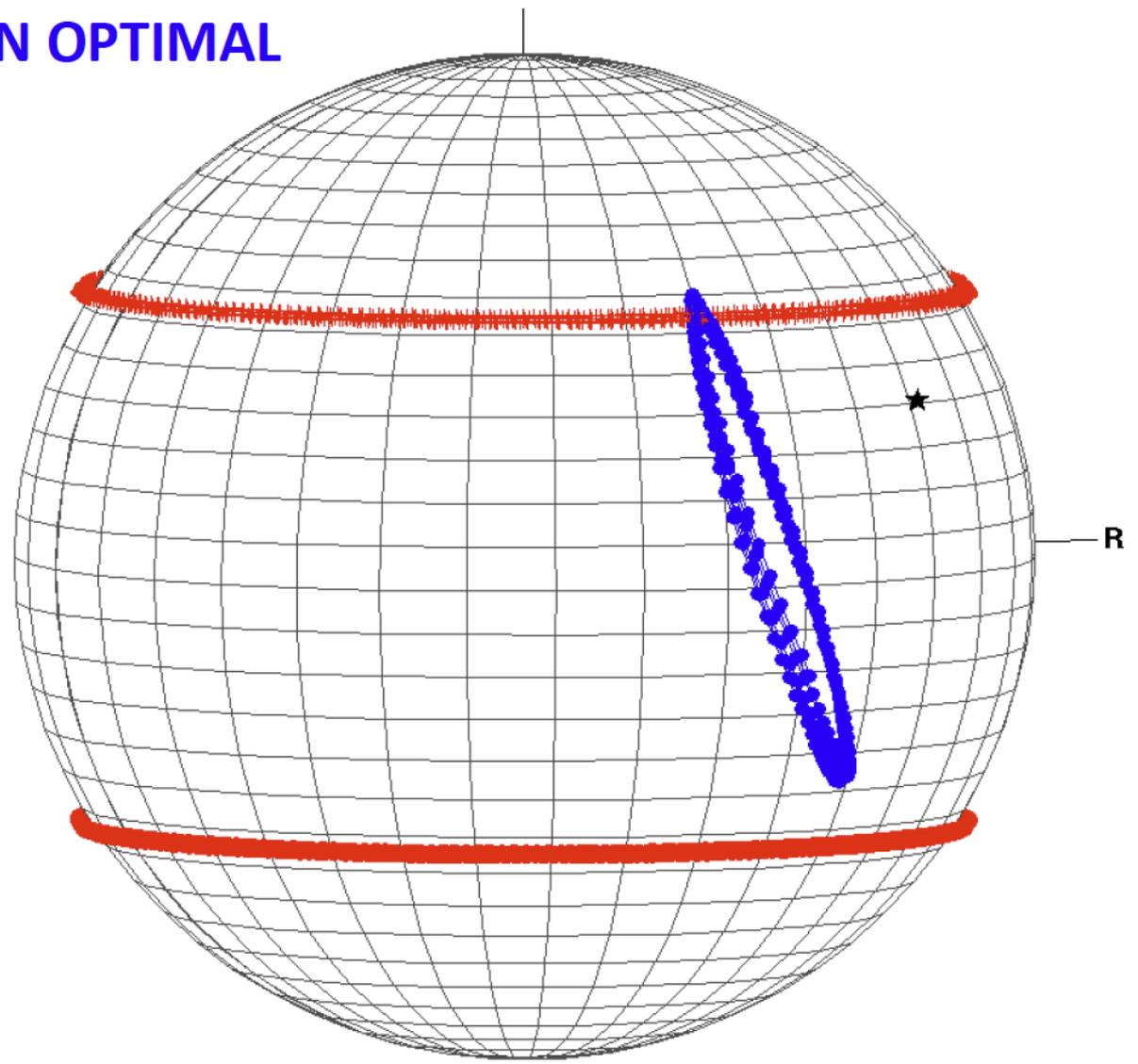
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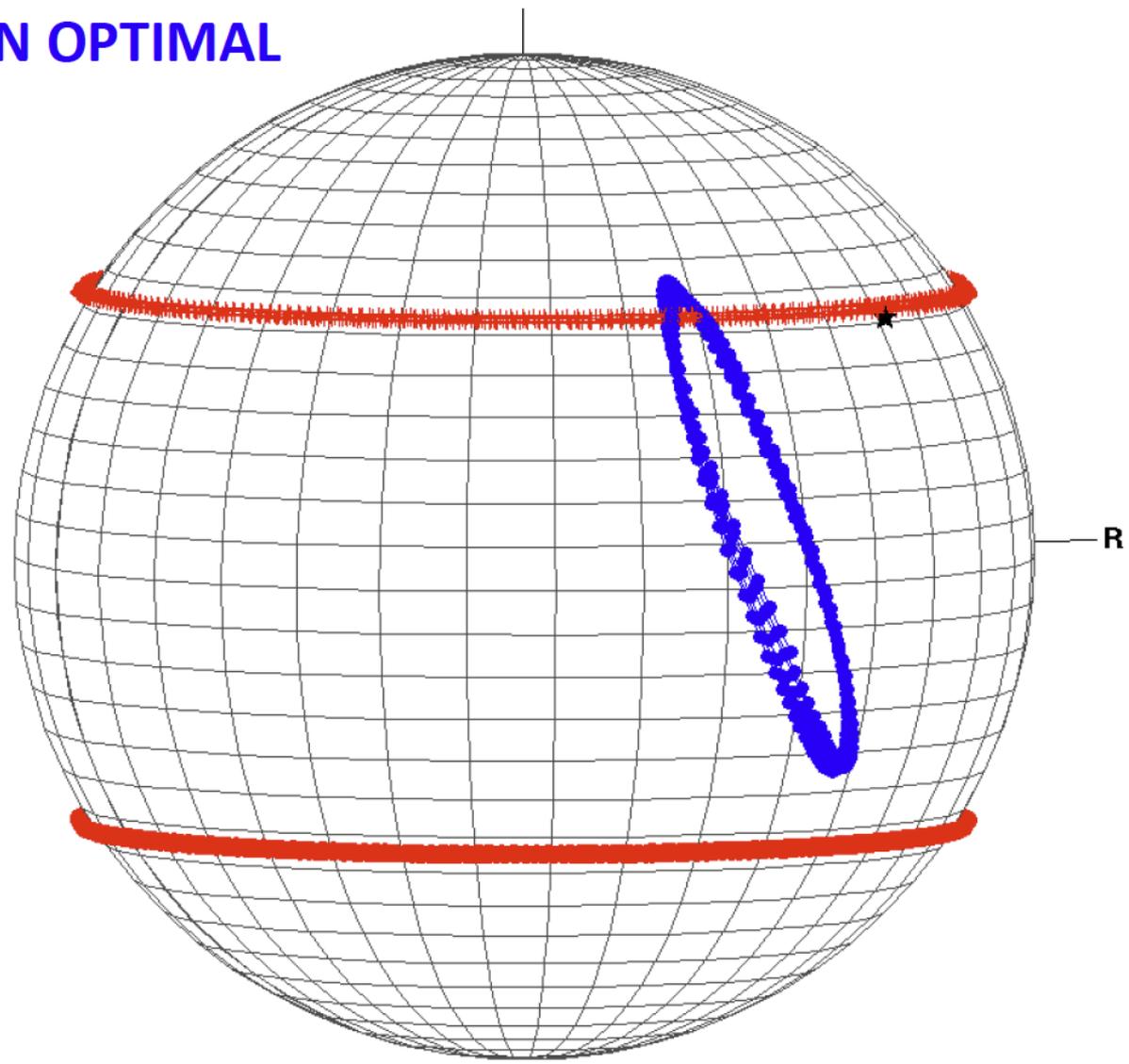
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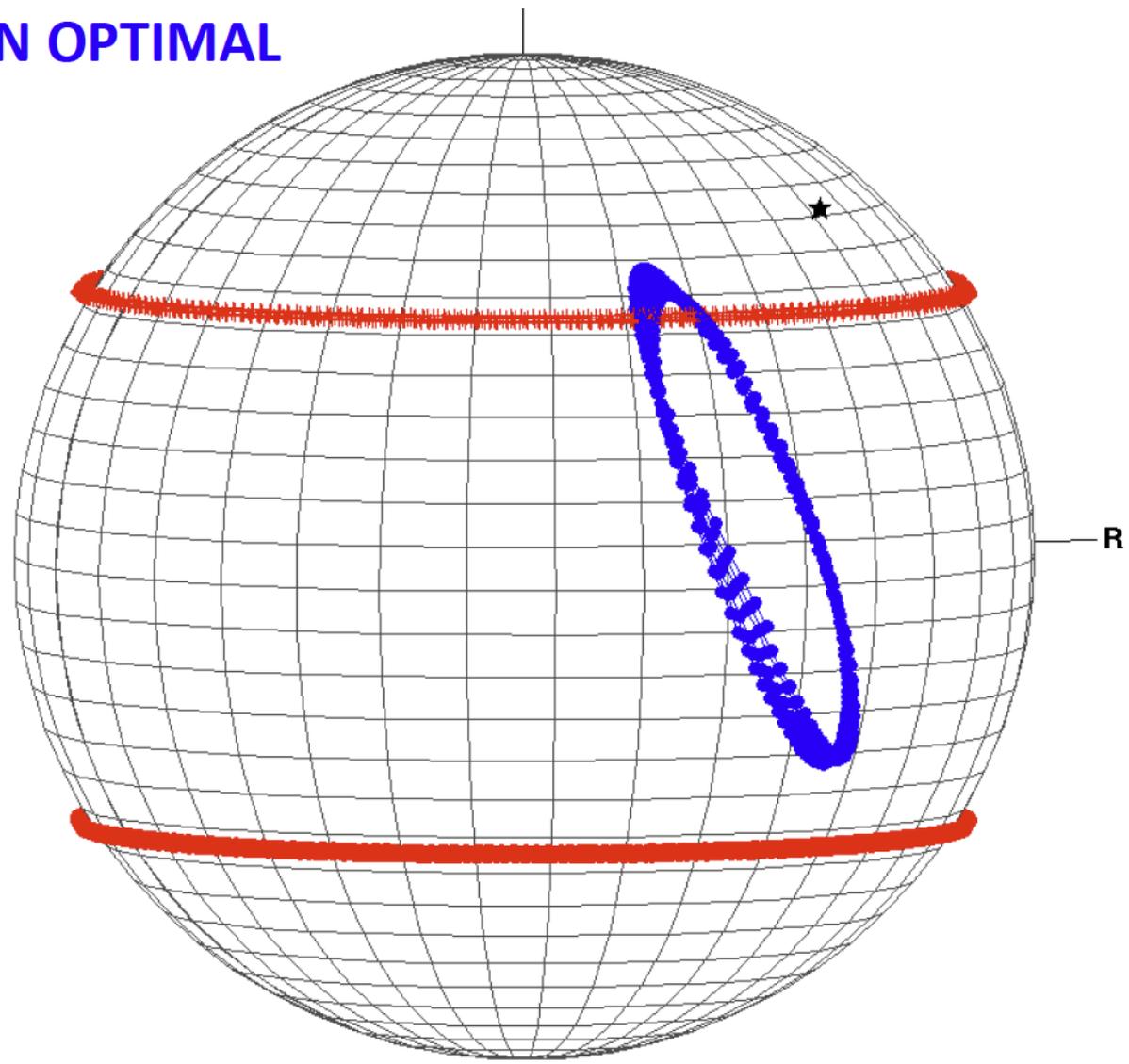
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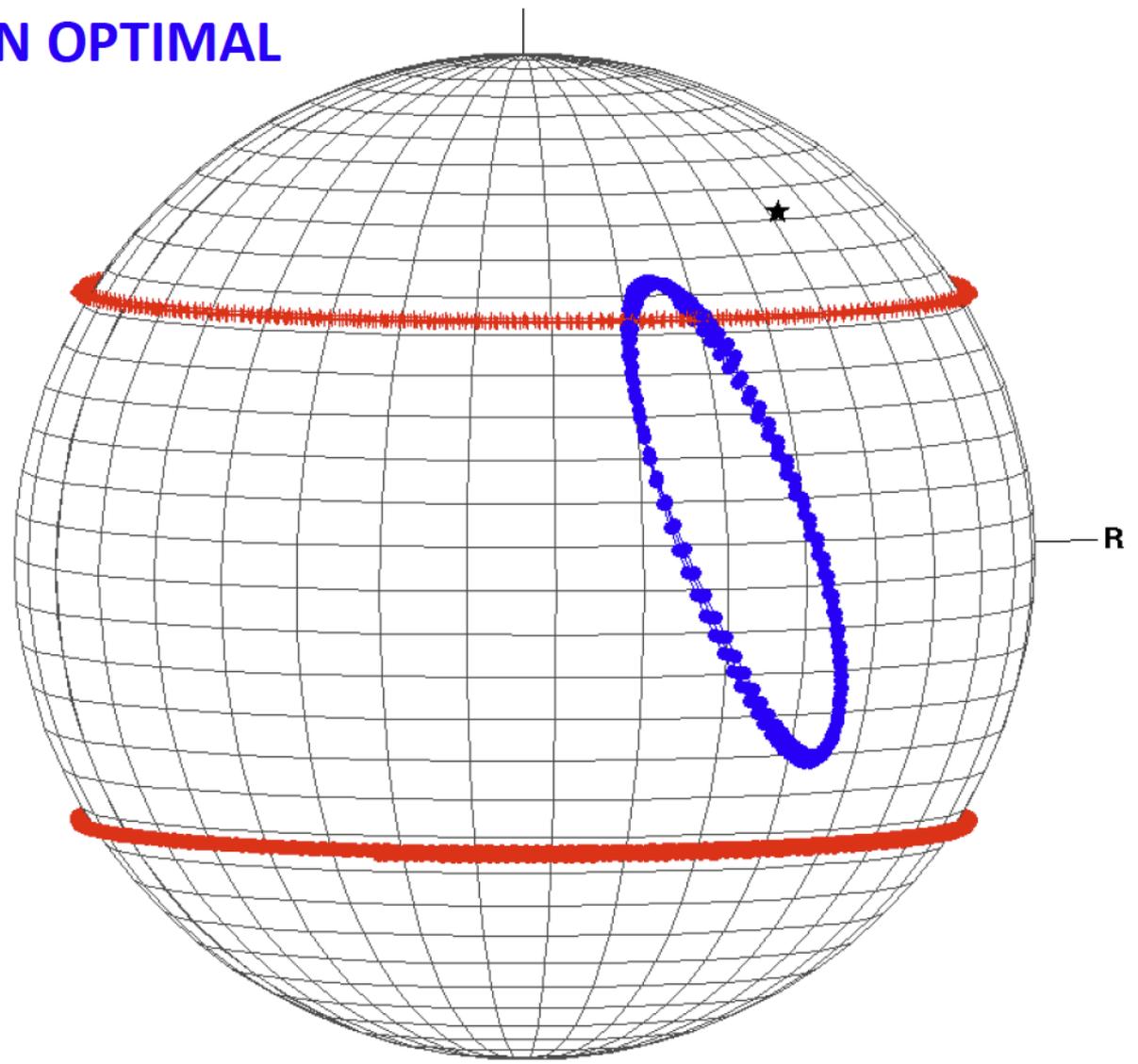
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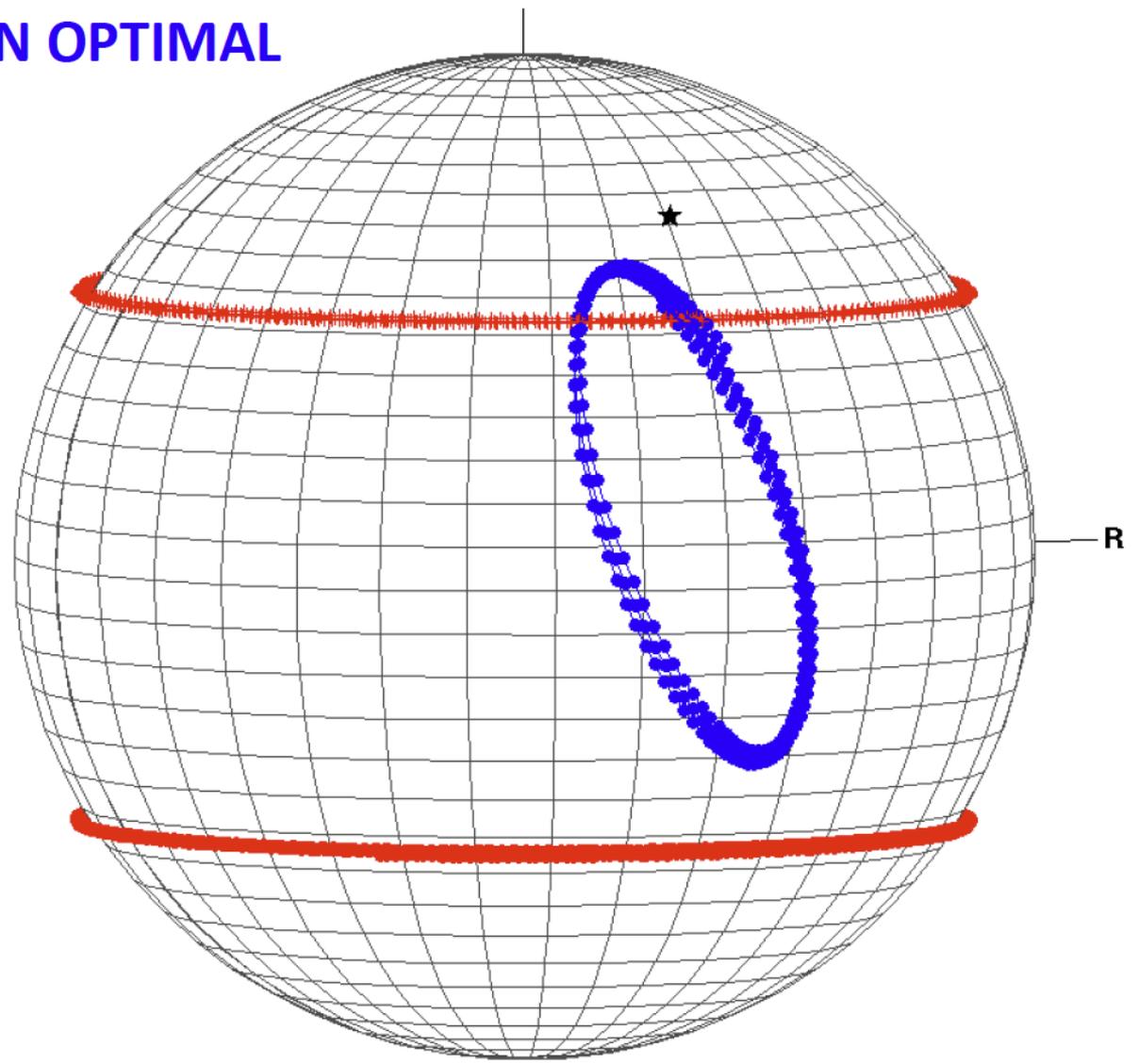
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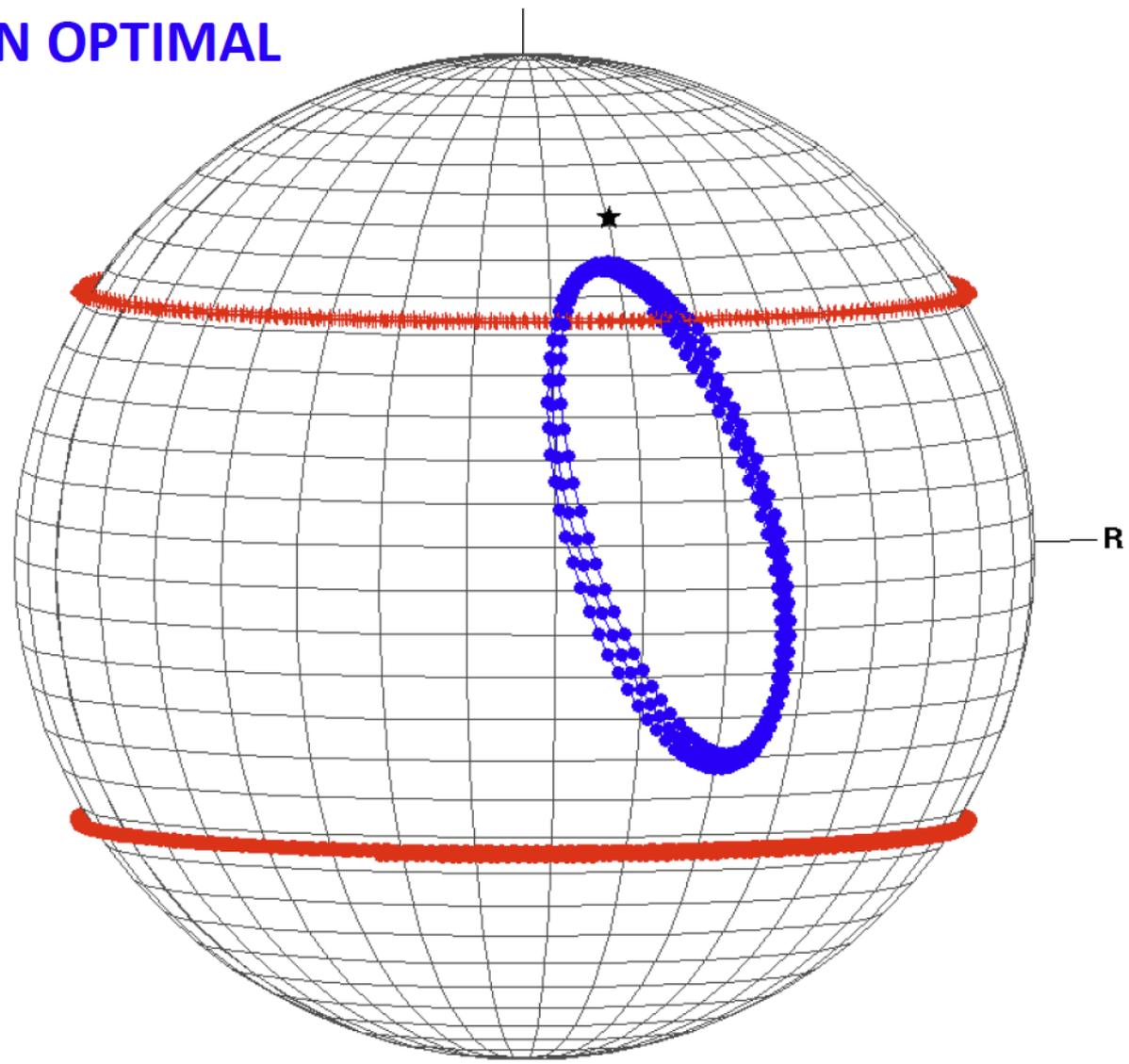
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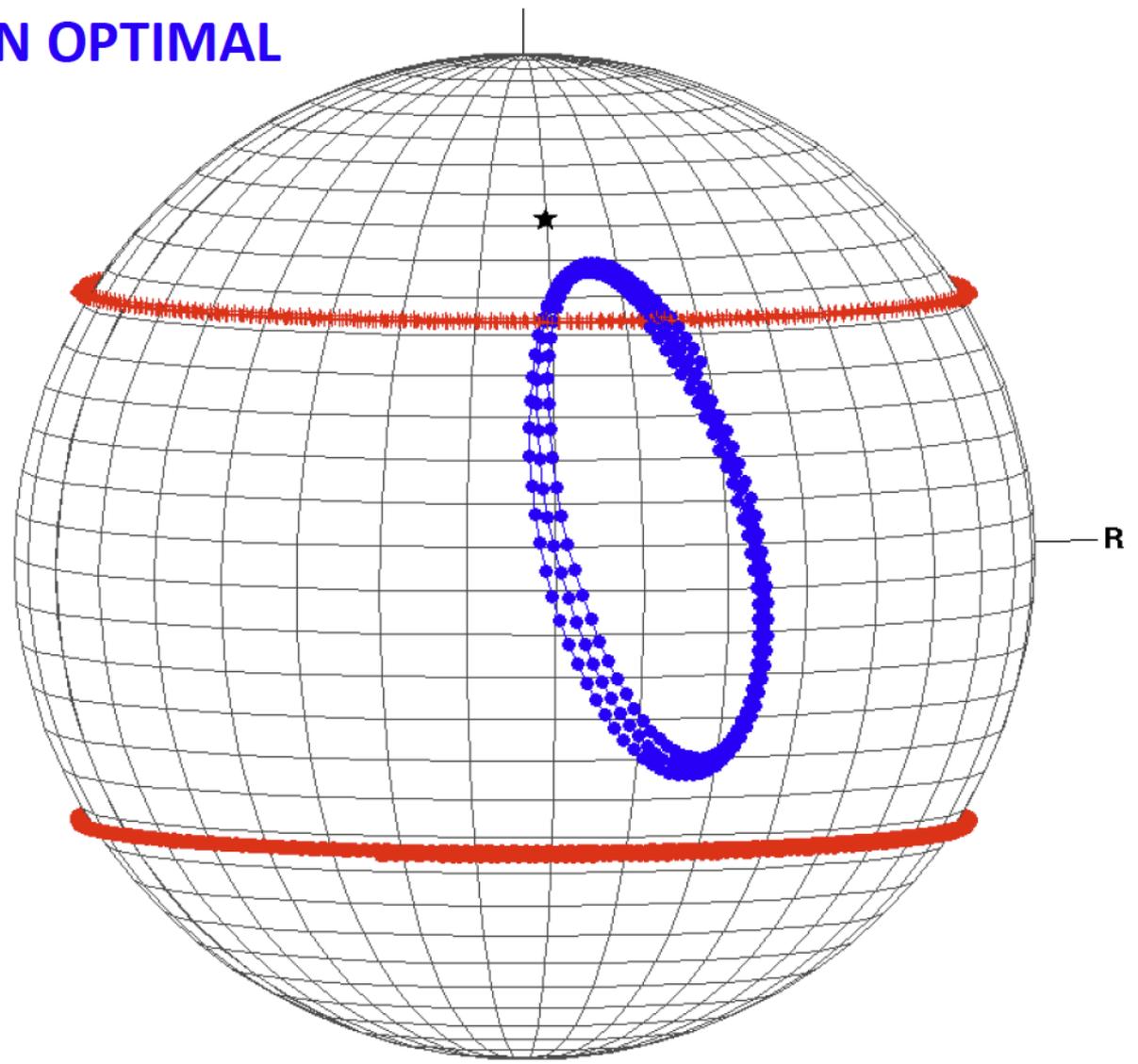
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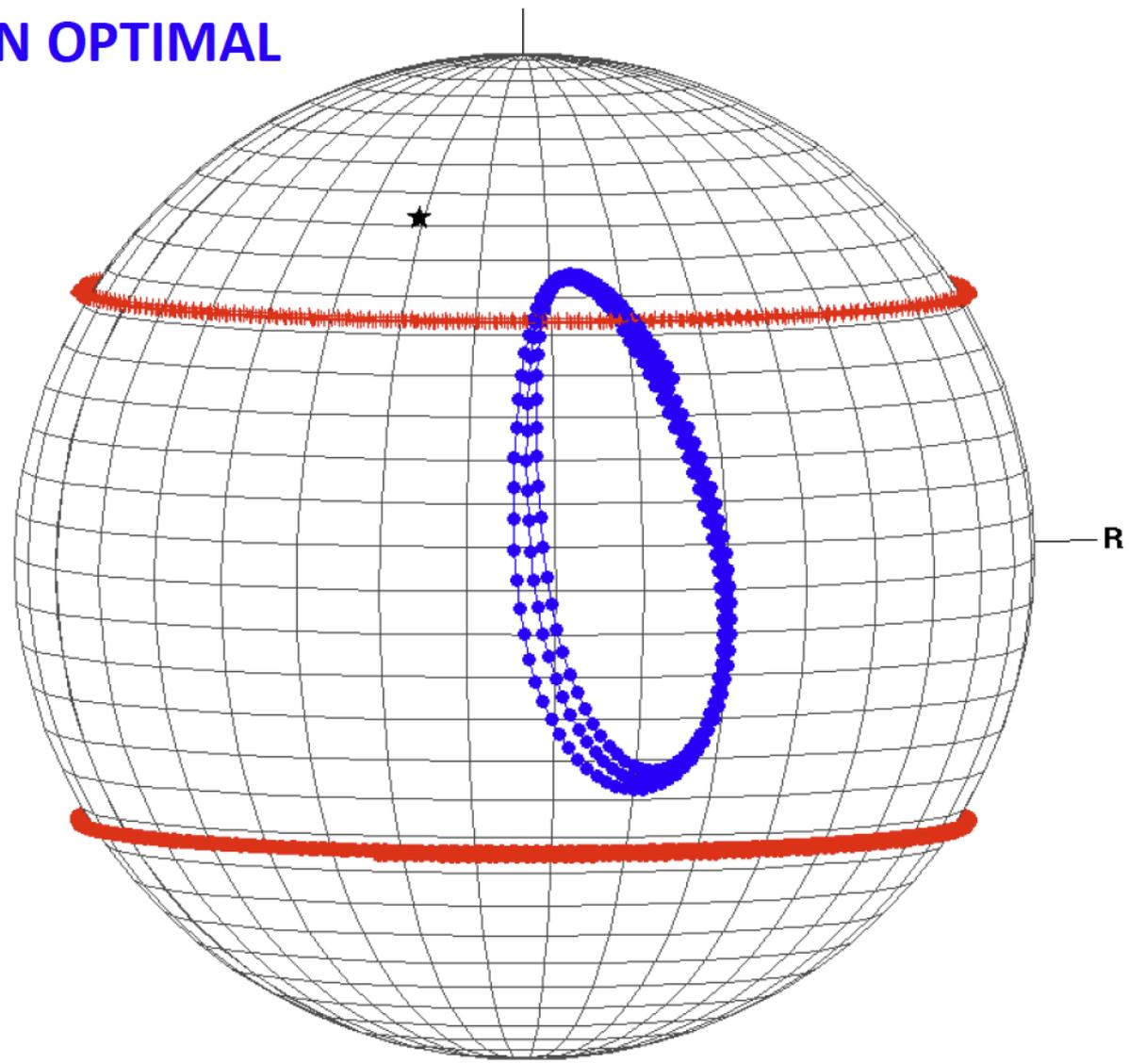
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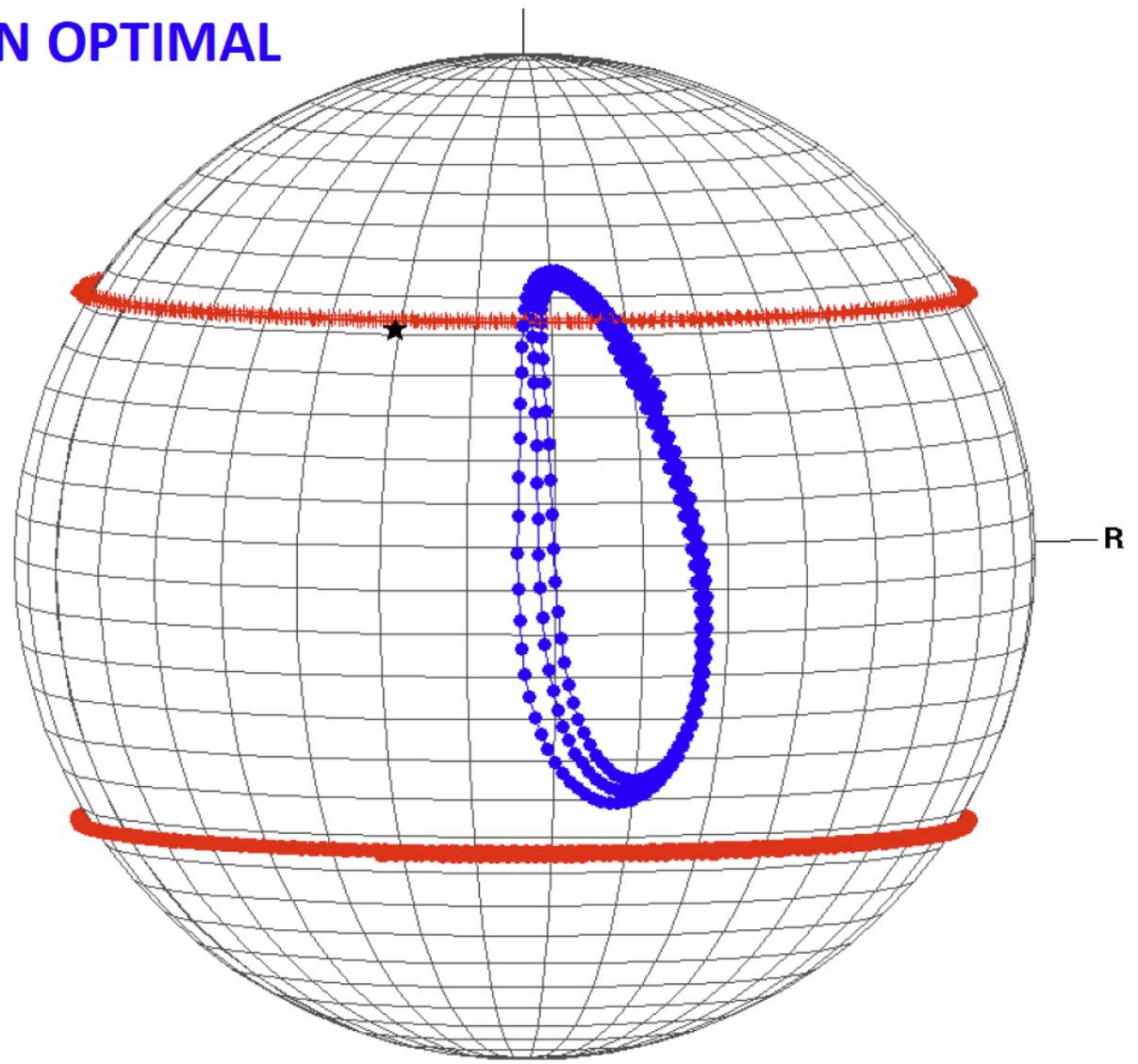
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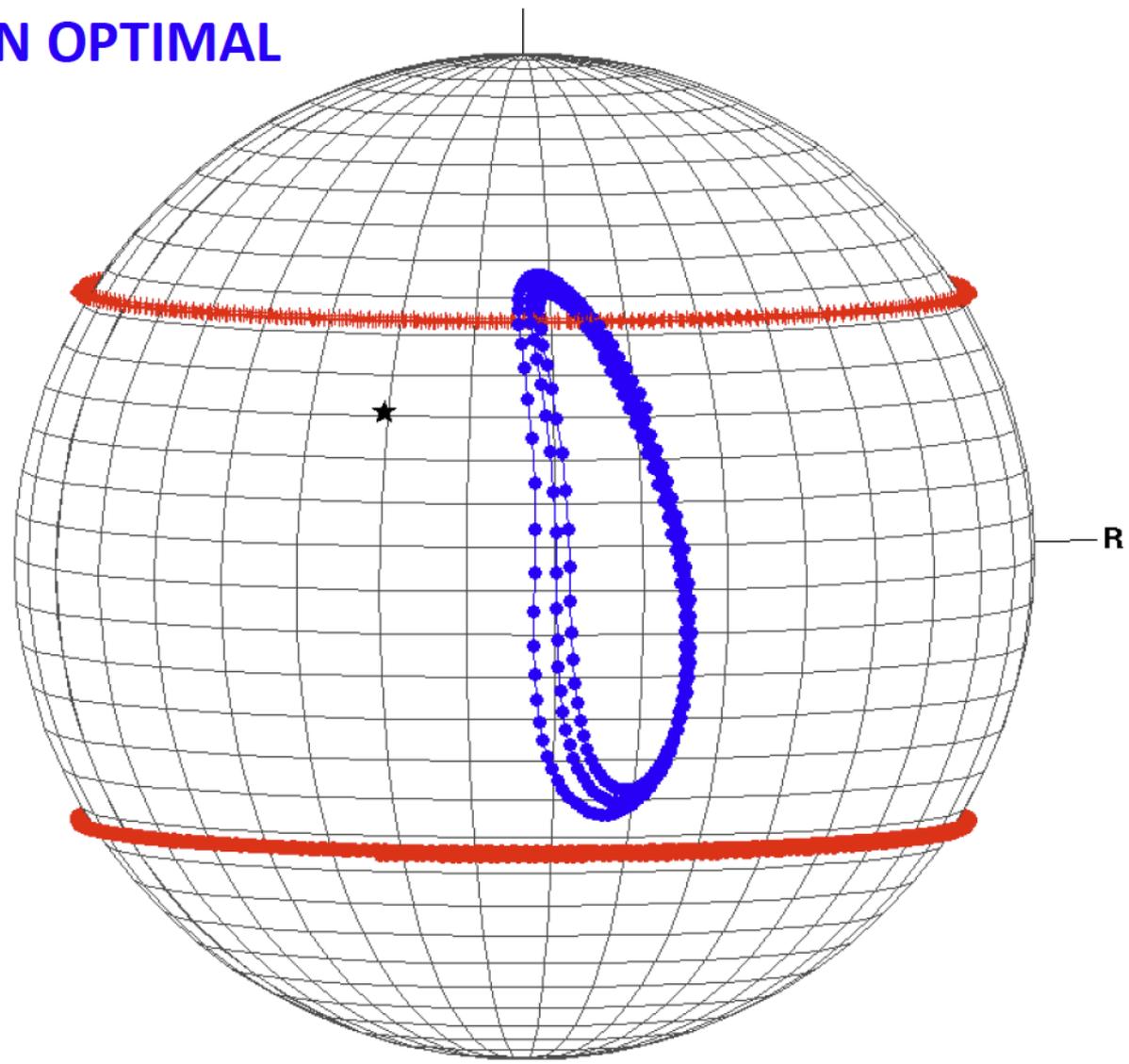
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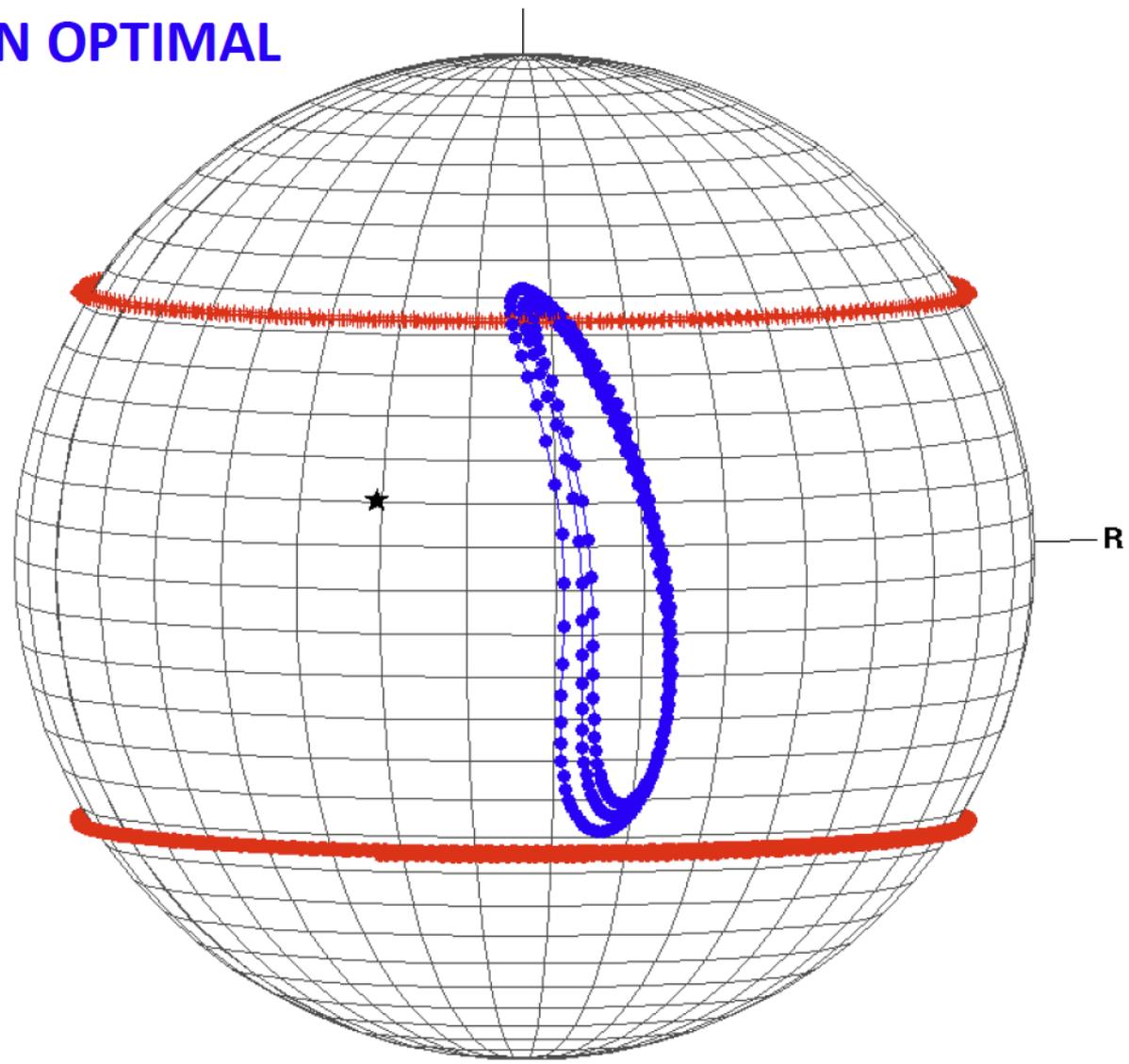
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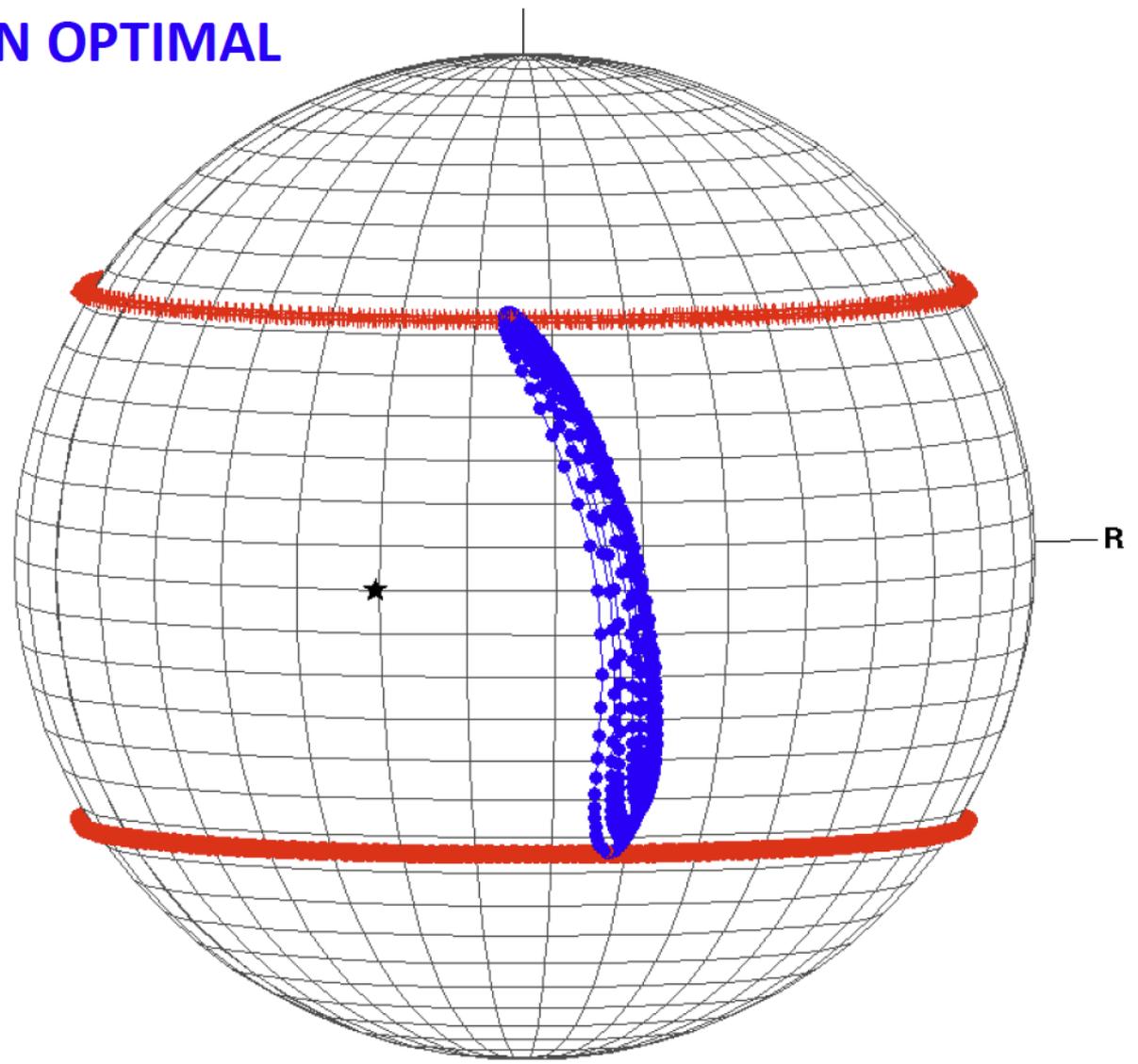
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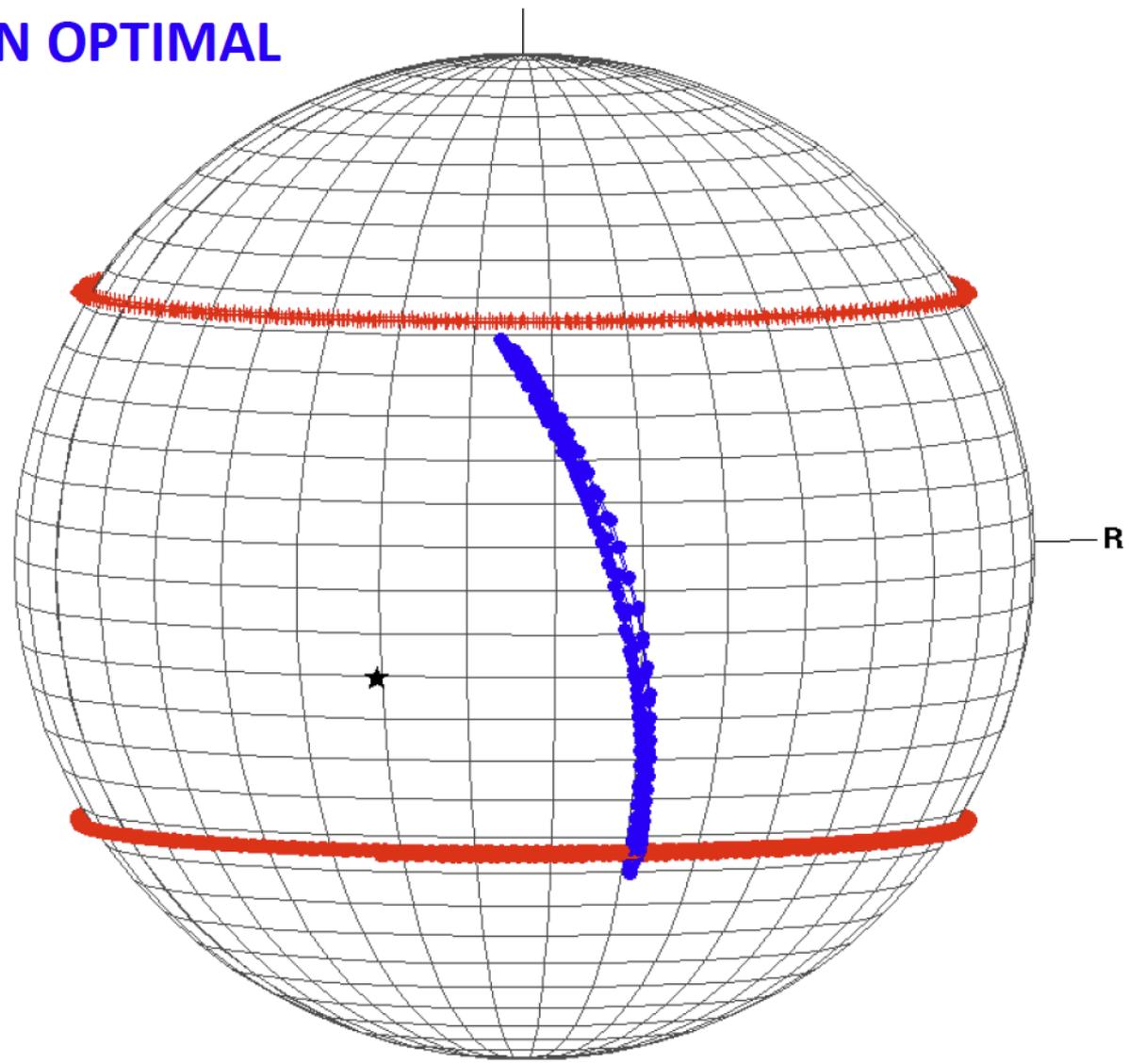
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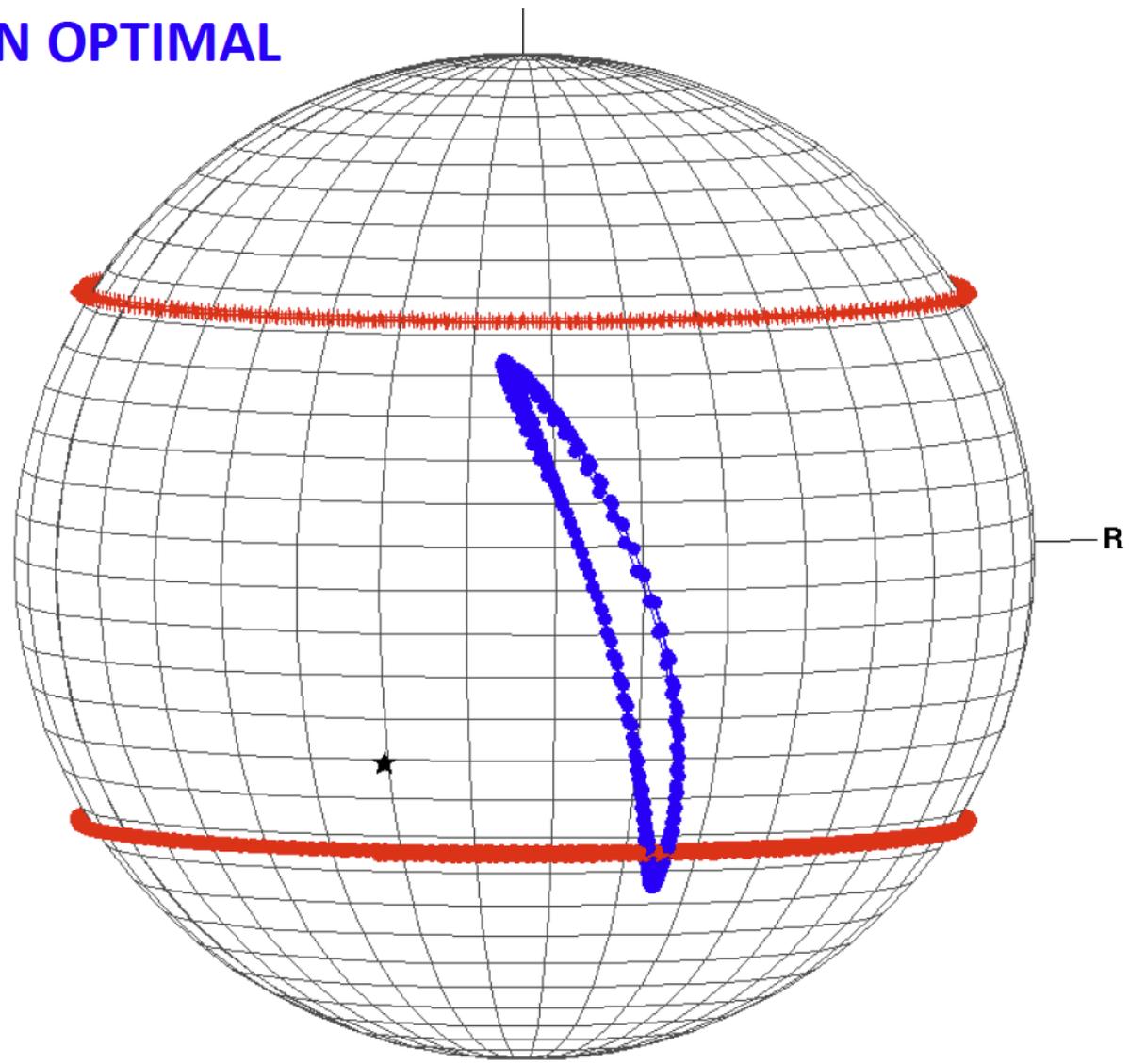
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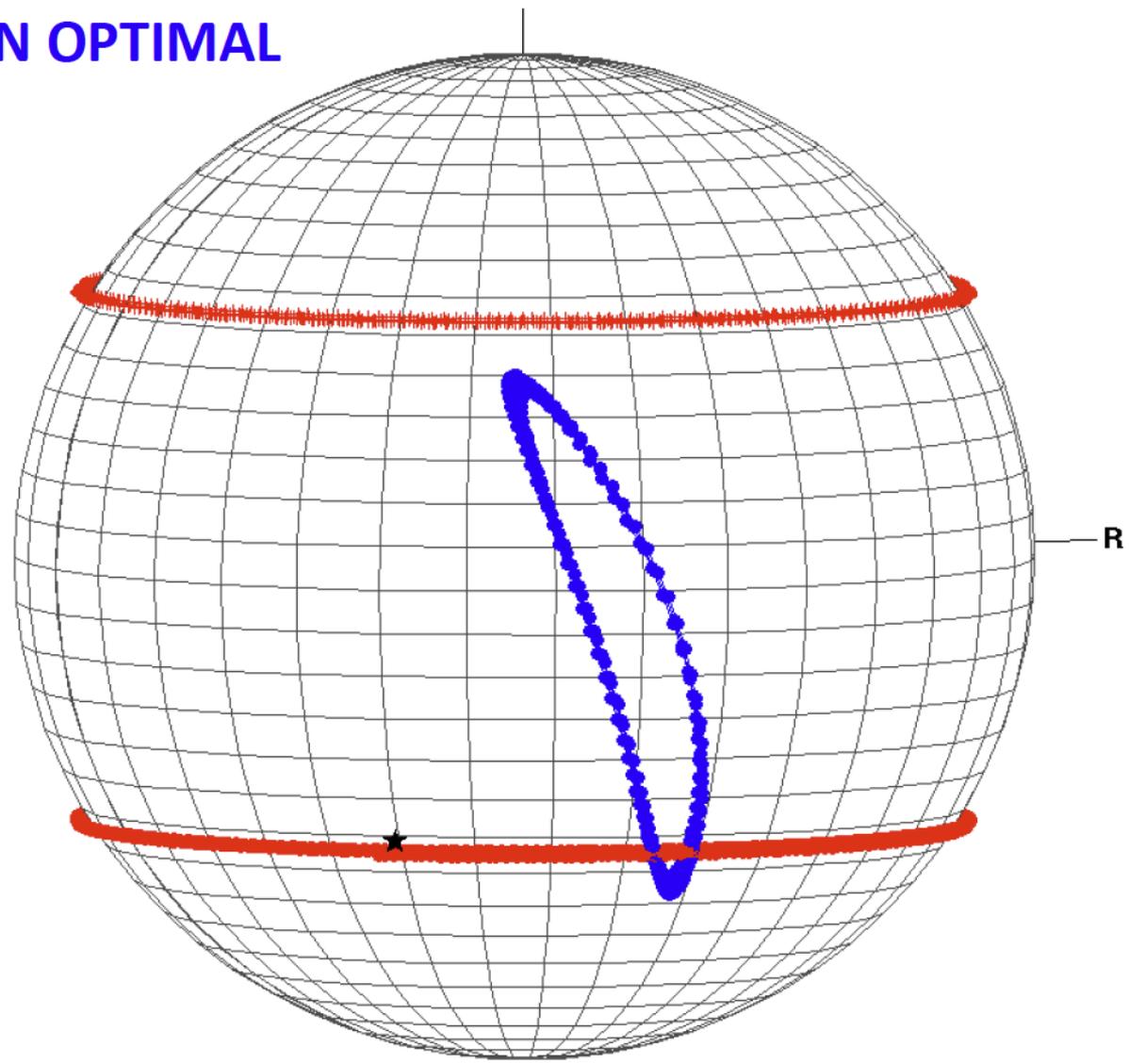
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RTN DIRECTION OPTIMAL



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RTN DIRECTION OPTIMAL



END

- Direction Optimization was essential to Dawn's success at Vesta
- Allowed for timely creation of fly-able maneuvers
- Solutions tended to exhibit direction continuity and smoothness
- Most effective formulation: Direction Attractor in RTN frame. Distant second: inertial frame pole repulsor.
- Generally best to choose frame in which thrust pattern is compact.
- There are many interesting, non-intuitive behaviors of direction optimal solutions