MODIS MOD21 Land Surface Temperature and Emissivity Algorithm Theoretical Basis Document

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1 Introduction

This document outlines the theory and methodology for generating the Moderate Resolution Imaging Spectroradiometer (MODIS) Level-2 daily daytime and nighttime 1-km land surface temperature (LST) and emissivity product using the Temperature Emissivity Separation (TES) algorithm. The MODIS-TES (MOD21_L2) product, will include the LST and emissivity for three MODIS thermal infrared (TIR) bands 29, 31, and 32, and will be generated for data from the NASA-EOS AM and PM platforms. This is version 1.0 of the ATBD and the goal is maintain a ‘living’ version of this document with changes made when necessary. The current standard baseline MODIS LST products (MOD11*) are derived from the generalized split-window (SW) algorithm (Wan and Dozier 1996), which produces a 1-km LST product and two classification-based emissivities for bands 31 and 32; and a physics-based day/night algorithm (Wan and Li 1997), which produces a 5-km (C4) and 6-km (C5) LST product and emissivity for seven MODIS bands: 20, 22, 23, 29, 31–33.

The land surface temperature and emissivity (LST&E) are derived from the surface radiance that is obtained by atmospherically correcting the at-sensor radiance. LST&E data are used for many Earth surface related studies such as surface energy balance modeling (Zhou et al. 2003b) and land-cover land-use change detection (French et al. 2008), while they are also critical for accurately retrieving important climate variables such as air temperature and relative humidity (Yao et al. 2011). The LST is an important long-term climate indicator, and a key variable for drought monitoring over arid lands (Anderson et al. 2011a; Rhee et al. 2010). The LST is an input to ecological models that determine important variables used for water use management such as evapotranspiration and soil moisture (Anderson et al. 2011b). Multispectral emissivity retrievals are also important for Earth surface studies. For example, emissivity spectral signatures are important for geologic studies and mineral mapping studies (Hook et al. 2005; Vaughan et al. 2005). This is because emissivity features in the TIR region are unique for many different types of materials that make up the Earth’s surface, such as quartz, which is ubiquitous in most of the arid regions of the world. Emissivities are also used for land use and land cover change mapping since vegetation fractions can often be inferred if the background soil is observable (French et al. 2008). Accurate knowledge of the surface emissivity is critical.
for accurately recovering the LST, especially over land where emissivity variations can be large both spectrally and spatially.

The MODTES algorithm derives its heritage from the ASTER TES algorithm (Gillespie et al. 1998). ASTER is a five-channel multispectral TIR scanner that was launched on NASA’s Terra spacecraft in December 1999 with a 90-m spatial resolution and revisit time of 16 days. The MODTES LST&E products will be produced globally over all land cover types, excluding open oceans for all cloud-free pixels. It is anticipated that the Level-2 products will be merged to produce weekly, monthly, and seasonal products, with the monthly product most likely producing global coverage, depending on cloud coverage. The generation of the higher level merged products will be considered a project activity. The MODTES Level 2 products will be initially inter-compared with the standard MOD11 products to identify regions and conditions for divergence between the products, and validation will be accomplished using a combination of temperature-based (T-based) and radiance-based (R-based) methods over dedicated field sites.

Maximum radiometric emission for the typical range of Earth surface temperatures, excluding fires and volcanoes, is found in two infrared spectral “window” regions: the midwave infrared (3.5–5 µm) and the thermal infrared (8–13 µm). The radiation emitted in these windows for a given wavelength is a function of both temperature and emissivity. Determining the separate contribution from each component in a radiometric measurement is an ill-posed problem since there will always be more unknowns—N emissivities and a single temperature—than the number of measurements, N, available. For MODIS, we will be solving for one temperature and three emissivities (MODIS TIR bands 29, 31, and 32). To solve the ill-posed problem, an additional constraint is needed, independent of the data. There have been numerous theories and approaches over the past two decades to solve for this extra degree of freedom. For example, the ASTER Temperature Emissivity Working Group (TEWG) analyzed ten different algorithms for solving the problem (Gillespie et al. 1999). Most of these relied on a radiative transfer model to correct at-sensor radiance to surface radiance and an emissivity model to separate temperature and emissivity. Other approaches include the SW algorithm, which extends the sea-surface temperature (SST) SW approach to land surfaces, assuming that land emissivities in the window region (10.5–12 µm) are stable and well known. However, this assumption leads to unreasonably large errors over barren regions where emissivities have large variations both spatially and spectrally. The ASTER TEWG finally decided on a hybrid algorithm, termed the TES algorithm,
which capitalizes on the strengths of previous algorithms with additional features (Gillespie et al. 1998).

TES is applied to the land-leaving TIR radiances that are estimated by atmospherically correcting the at-sensor radiance on a pixel-by-pixel basis using a radiative transfer model. TES uses an empirical relationship to predict the minimum emissivity that would be observed from a given spectral contrast, or minimum-maximum difference (MMD) (Kealy and Hook 1993; Matsunaga 1994). The empirical relationship is referred to as the calibration curve and is derived from a subset of spectra in the ASTER spectral library (Baldridge et al. 2009). A MODIS calibration curve, applicable to MODIS TIR bands 29, 31, and 32 will be computed. Numerical simulations have shown that TES is able to recover temperatures within 1.5 K and emissivities within 0.015 for a wide range of surfaces and is a well-established physical algorithm that produces seamless images with no artificial discontinuities such as might be seen in a land classification type algorithm (Gillespie et al. 1998).

The remainder of the document will discuss the MODIS instrument characteristics, provide a background on TIR remote sensing, give a full description and background on the TES algorithm, provide quality assessment, discuss numerical simulation studies and uncertainty analysis, and, finally, outline a validation plan.

2 MODIS Background

The MODIS sensors on NASA’s Terra (AM) and Aqua (PM) platforms are currently the flagship instruments for global studies of Earth’s surface, atmosphere, cryosphere, and ocean processes (Justice et al. 1998; Salomonson et al. 1989). In terms of LST&E products, the strength of the MODIS is its ability to retrieve daily data at 1 km for both day- and nighttime observations on a global scale.

2.1 Calibration

There are now multiple satellite sensors that measure the mid- and thermal infrared radiance emitted from the Earth’s surface in multiple spectral channels. These sensors include the Advanced Along Track Scanning Radiometer (AATSR), ASTER, Advanced Very High Resolution Radiometer (AVHRR), and MODIS instruments. A satellite calibration interconsistency study is currently underway for evaluating the interconsistency of these sensors.
at the Lake Tahoe and Salton Sea cal/val sites. This effort has indicated that further work is needed to consistently inter-calibrate the ATSR series and AVHRR series whereas ASTER and MODIS have a clearly defined calibration and well-understood performance.

In-flight performance of TIR radiance data (3–14 µm) used in LST&E products is typically determined through comparison with ground validation sites. Well-established automated validation sites at Lake Tahoe, CA/NV, and Salton Sea, CA have been used to validate the TIR data from numerous sensors including ASTER and MODIS (Hook et al. 2007). Results from this work demonstrate that the MODIS (Terra and Aqua) instruments have met their required radiometric calibration accuracy of 0.5–1% in the TIR bands used to retrieve LST&E with differences of ±0.25% (~0.16K) for the lifetime of the missions. Similar work for ASTER indicates its performance also meets the 1% requirements, provided additional steps are taken to account for drift between calibrations (Tonooka et al. 2005).

2.2 Instrument Characteristics

The MODIS instrument acquires data in 36 spectral channels in the visible, near infrared, and infrared wavelengths. Infrared channels 20, 22, 23, 29, 31, and 32 are centered on 3.79, 3.97, 4.06, 8.55, 11.03, and 12.02 µm respectively. Channels 29, 31, and 32 are the focus of the MODTES algorithm. MODIS scans ±55° from nadir and provides daytime and nighttime imaging of any point on the Earth every 1–2 days with a continuous duty cycle. MODIS data are quantized in 12 bits and have a spatial resolution of ~1 km at nadir. They are calibrated with a cold space view and full aperture blackbody viewed before and after each Earth view. A more detailed description of the MODIS instrument and its potential application can be found in Salomonson et al. (1989) and Barnes et al. (1998). The MODIS sensor is flown on the Terra and Aqua spacecraft launched in 1999 and 2002, respectively.

2.3 LST&E Standard Products

Current standard LST&E products (MOD11 from Terra, and MYD11 from Aqua) are generated by two different algorithms: a generalized split-window (GSW) algorithm (product MOD11_L2) (Wan and Dozier 1996) that produces LST data at 1-km resolution, and a day/night algorithm (product MOD11B1) (Wan and Li 1997) that produces LST&E data at ~5 km (C4) and ~6 km (C5) resolution.
The GSW algorithm extends the SST SW approach to land surfaces. In this approach the emissivity of the surface is assumed to be known based on an \textit{a priori} classification of the Earth surface into a selected number of cover types and a dual or multichannel SW algorithm is used in much the same way as with the oceans. This approach has been adopted by the MODIS and VIIRS emissivity product teams. The MODIS algorithm estimates the emissivity of each pixel by consulting the MODIS land cover product (MOD12Q1) whose values are associated with laboratory-measured emissivity spectra (Snyder et al. 1998). Adjustments are made for TIR BRDF, snow (from MOD10_L2 product), and green vs. senescent vegetation. The \textit{a priori} approach works well for surfaces whose emissivity can be correctly assigned based on the classification but less well for surfaces whose emissivities differ from the assigned emissivity. Specifically, it is best suited for land-cover types such as dense evergreen canopies, lake surfaces, snow, and most soils, all of which have stable emissivities known to within 0.01. It is significantly less reliable over arid and semi-arid regions.

The day/night approach uses pairs of daytime and nighttime observations in seven MODIS mid-infrared (MIR) and TIR bands (bands 20, 22, 23, 29, and 31–33) to simultaneously retrieve LST&E. This approach was designed to overcome the ill-posed thermal retrieval problem (where there are always more unknowns than independent equations in a given sample) by using two independent samples of the same target separated in time. The resulting system of equations can then be solved, provided several key assumptions are met. These include: a) the difference in surface temperature between the two samples must be large; b) the surface conditions (i.e., the emissivity spectrum) must not change between day and night samples; c) the geolocation of the samples must be highly accurate; and d) emissivity angular anisotropy must not be significant. In summary, it assumes that differences in the spectral radiances between the two samples are caused by surface temperature change and nothing else. In the MODIS implementation, the cloud-free day/night samples must be within 32 days of each other. The day-night approach is more complicated to implement due to data storing; however, it is considered preferable to the \textit{a priori} method in areas where emissivity is difficult to accurately predict—most notably in semi-arid and arid areas. This algorithm is not well suited for polar regions since the signal-to-noise of observations in band 20 of the MIR are unacceptably low. Similarly, this product has limitations over very warm targets (e.g., arid and semi-arid regions) due to saturation of the MIR bands.
Two methods have been used for validating MODIS LST data products; these are a conventional T-based method and an R-based method (Wan and Li 2008). The T-based method requires ground measurements over thermally homogenous sites concurrently with the satellite overpass, while the R-based method relies on a radiative closure simulation in a clear atmospheric window region to estimate the LST from top of atmosphere (TOA) observed brightness temperatures, assuming the emissivity is known from ground measurements. The MOD11_L2 LST product has been validated with a combination of T-based and R-based methods over more than 19 types of thermally homogenous surfaces such as lakes (Hook et al. 2007), at dedicated field campaign sites over agricultural fields and forests (Coll et al. 2005), playas and grasslands (Wan et al. 2004; Wan 2008), and for a range of different seasons and years. LST errors are generally within ±1 K for all sites under stable atmospheric conditions except semi-arid and arid areas that had errors of up to 5 K (Wan and Li 2008).

At the University of Wisconsin, a monthly MODIS global infrared land surface emissivity database (UWIREMIS) has been developed based on the standard MOD11B1 emissivity product (Seemann et al. 2008) at ten wavelengths (3.6, 4.3, 5.0, 5.8, 7.6, 8.3, 9.3, 10.8, 12.1, and 14.3 µm) with 5 km spatial resolution. The baseline fit method, based on a conceptual model developed from laboratory measurements of surface emissivity, is applied to fill in the spectral gaps between the six available MODIS/MYD11 bands. The ten wavelengths in the UWIREMIS emissivity database were chosen as hinge points to capture as much of the shape of the higher resolution emissivity spectra as possible, and extended by Borbas et al. (2007) to provide 416 spectral points from 3.6 to 14.3 µm. The algorithm is based on a Principal Component Analyses (PCA) regression using the eigenfunction representation of high spectral resolution laboratory measurements from the ASTER spectral library (Baldridge et al. 2009).
3 Earth Science Relevance

LST&E are key variables for explaining the biophysical processes that govern the balances of water and energy at the land surface. LST&E data are used in many research areas including ecosystem models, climate models, cryospheric research, and atmospheric retrievals schemes. Our team has been carefully selected to include expertise in these areas. The descriptions below summarize how LST&E data are typically used in these areas.

3.1 Use of LST&E in Climate/Ecosystem Models

Emissivity is a critical parameter in climate models that determine how much thermal radiation is emitted back to the atmosphere and space and therefore is needed in surface radiation budget calculations, and also to calculate important climate variables such as LST (e.g., Jin and Liang 2006; Zhou et al. 2003b). Current climate models represent the land surface emissivity by either a constant value or very simple parameterizations due to the limited amount of suitable data. Land surface emissivity is prescribed to be unity in the Global Climate Models (GCMs) of the Center for Ocean-Land-Atmosphere Studies (COLA) (Kinter et al. 1988), the Chinese Institute of Atmospheric Physics (IAP) (Zeng et al. 1989), and the US National Meteorological Center (NMC) Medium-Range Forecast (MRF). In the recently developed NCAR Community Land Model (CLM3) and its various earlier versions (Bonan et al. 2002; Oleson et al. 2004), the emissivity is set as 0.97 for snow, lakes, and glaciers, 0.96 for soil and wetlands, and vegetation is assumed to be black body. For a broadband emissivity to correctly reproduce surface energy balance statistics, it needs to be weighted both over the spectral surface blackbody radiation and over the downward spectral sky radiances and used either as a single value or a separate value for each of these terms. This weighting depends on the local surface temperatures and atmospheric composition and temperature. Most simply, as the window region dominates the determination of the appropriate single broadband emissivity, an average of emissivities over the window region may suffice.

Climate models use emissivity to determine the net radiative heating of the canopy and underlying soil and the upward (emitted and reflected) thermal radiation delivered to the atmosphere. The oversimplified representations of emissivity currently used in most models introduce significant errors in the simulations of climate. Unlike what has been included in
climate models up to now, satellite observations indicate large spatial and temporal variations in
land surface emissivity with surface type, vegetation amount, and soil moisture, especially over
deserts and semi-deserts (Ogawa 2004; Ogawa et al. 2003). This variability of emissivity can be
constructed by the appropriate combination of soil and vegetation components.

Sensitivity tests indicate that models can have an error of 5–20 Wm$^{-2}$ in their surface
energy budget for arid and semi-arid regions due to their inadequate treatment of emissivity (Jin
and Liang 2006; Zhou et al. 2003b), a much larger term than the surface radiative forcing from
greenhouse gases. The provision, through this proposal, of information on emissivity with global
spatial sampling will be used for optimal estimation of climate model parameters. A climate
model, in principle, constructs emissivity at each model grid square from four pieces of
information: a) the emissivity of the underlying soil; b) the emissivity of the surfaces of
vegetation (leaves and stems); c) the fraction of the surface that is covered by vegetation; and d)
the description of the areas and spatial distribution of the surfaces of vegetation needed to
determine what fraction of surface emission will penetrate the canopy. Previously, we have not
been able to realistically address these factors because of lack of suitable data. The emissivity
datasets developed for this project will be analyzed with optimal estimation theory that uses the
spatial and temporal variations of the emissivity data over soil and vegetation to constrain more
realistic emissivity schemes for climate models. In doing so, land surface emissivity will be
linked to other climate model parameters such as fractional vegetation cover, leaf area index,
snow cover, soil moisture, and soil albedo, as explored in Zhou et al. (2003a). Co-I Dickinson
will convert spectral band emissivities to broadband values optimized for calculation of net
longwave radiation in climate models. The use of more realistic emissivity values will greatly
improve climate simulations over sparsely vegetated regions as previously demonstrated by
various sensitivity tests (e.g., Jin and Liang 2006; Zhou et al. 2003b). In particular, both daily
mean and day-to-night temperature ranges are substantially impacted by the model’s treatment of
emissivity.

3.2 Use of LST&E in Cryospheric Research

Surface temperature is a sensitive energy-balance parameter that controls melt and energy
exchange between the surface and the atmosphere. Surface temperature is also used to monitor
melt zones on glaciers and can be related to the glacier facies of (Benson 1996), and thus to
glacier or ice sheet mass balance (Hall et al. 2006). Analysis of the surface temperature of the
Greenland Ice Sheet and the ice caps on Greenland provides a method to study trends in surface temperature as a surrogate for, and enhancement of, air-temperature records, over a period of decades (Comiso 2006). Maps of LST of the Greenland Ice Sheet have been developed using the MODIS 1-km LST standard product, and trends in mean LST have been measured (Hall et al. 2008). Much attention has been paid recently to the warming of the Arctic in the context of global warming. Comiso (2006) shows that the Arctic region, as a whole, has been warming at a rate of 0.72 ±0.10°C per decade from 1981–2005 inside the Arctic Circle, though the warming pattern is not uniform. Furthermore, various researchers have shown a steady decline in the extent of the Northern Hemisphere sea ice, both the total extent and the extent of the perennial or multiyear ice (Parkinson et al. 1999). Increased melt of the margins of the Greenland Ice Sheet has also been reported (Abdalati and Steffen 2001).

Climate models predict enhanced Arctic warming but they differ in their calculations of the magnitude of that warming. The only way to get a comprehensive measurement of surface-temperature conditions over the Polar Regions is through satellite remote sensing. Yet errors in the most surface temperature algorithms have not been well-established. Limitations include the assumed emissivity, effect of cloud cover, and calibration consistency of the longer-term satellite record.

Comparisons of LST products over snow and ice features reveal LST differences in homogeneous areas of the Greenland Ice Sheet of >2°C under some circumstances. Because there are many areas that are within a few degrees of 0°C, such as the ice-sheet margin in southern Greenland, it is of critical importance to be able to measure surface temperature from satellites accurately. Ice for which the mean annual temperature is near the freezing point is highly vulnerable to rapid melt.

3.3 Use of LST&E in Atmospheric Retrieval Schemes

The atmospheric constituent retrieval community and numerical weather prediction operational centers are expected to benefit from the development of a unified land surface emissivity product. The retrieval of vertical profiles of air temperature and water vapor mixing ratio in the atmospheric boundary layer over land is sensitive to the assumptions used about the infrared emission and reflection from the surface. Even the retrieval of clouds and aerosols over land using infrared channels is complicated by uncertainties in the spectral dependence of the land surface emission. Moreover, weather models improve their estimates of atmospheric
temperature and composition by comparisons between observed and model calculated spectral radiances, using an appropriate data assimilation (1D-Var) framework. The model generates forward calculation of radiances by use of their current best estimate of temperature profiles, atmospheric composition, and surface temperature and emissivity. If good prior estimates of infrared emissivity can be provided along with their error characterization, what would otherwise be a major source of error and bias in the use of the satellite radiances in data assimilation can be minimized.

4 Atmospheric Correction

4.1 Thermal Infrared Radiance

The at-sensor measured radiance in the TIR spectral region (7–14 µm) is a combination of three primary terms: the Earth-emitted radiance, reflected downwelling sky irradiance, and atmospheric path radiance. The Earth-emitted radiance is a function of temperature and emissivity and gets attenuated by the atmosphere on its path to the satellite. The atmosphere also emits radiation, some of which reaches the sensor directly as “path radiance,” while some gets radiated to the surface (irradiance) and reflected back to the sensor, commonly known as the reflected downwelling sky irradiance. Reflected solar radiation in the TIR region is negligible (Figure 1) and a much smaller component than the surface-emitted radiance. One effect of the sky irradiance is the reduction of the spectral contrast of the emitted radiance, due to Kirchhoff’s law. Assuming the spectral variation in emissivity is small (Lambertian assumption), and using Kirchhoff’s law to express the hemispherical-directional reflectance as directional emissivity \( \rho_\lambda = 1 - \epsilon_\lambda \), the clear-sky at-sensor radiance can be written as three terms: the Earth-emitted radiance described by Planck’s function and reduced by the emissivity factor, \( \epsilon_\lambda \); the reflected downwelling irradiance; and the path radiance.

\[
L_\lambda(\theta) = \left[ \epsilon_\lambda B_\lambda(T_s) + (1 - \epsilon_\lambda) L^1_\lambda \right] T_\lambda(\theta) + L^1_\lambda(\theta)
\]  

(1)
Figure 1. Simulated atmospheric transmittance for a US Standard Atmosphere (red) and tropical atmosphere (blue) in the 3–12 µm region. Also shown is the solar irradiance contribution W/m²/µm².

Where:

$L_\lambda(\theta) = \text{at-sensor radiance}$;

$\lambda = \text{wavelength}$;

$\theta = \text{observation angle}$;

$\varepsilon_\lambda = \text{surface emissivity}$;

$T_s = \text{surface temperature}$;

$L_\lambda^\dagger = \text{downwelling sky irradiance}$;

$\tau_\lambda(\theta) = \text{atmospheric transmittance}$;

$L_\lambda^\uparrow(\theta) = \text{atmospheric path radiance}$

$B_\lambda(T_s) = \text{Planck function, described by Planck’s law}$:

$$B_\lambda = \frac{c_1}{\pi \lambda^5} \left( \frac{1}{\exp \left( \frac{c_2}{\lambda T} \right) - 1} \right)$$

$c_1 = 2\pi hc^2 = 3.74 \times 10^{-16} \text{ W} \cdot \text{m}^2 \text{ (1st radiation constant)}$

$h = 6.63 \times 10^{-34} \text{ W} \cdot \text{s}^2 \text{ (Planck’s constant)}$

$c_2 = h \cdot c / k = 1.44 \times 10^4 \text{ µm} \cdot \text{K} \text{ (2nd radiation constant)}$

$k = 1.38 \times 10^{-23} \text{ W} \cdot \text{s} \cdot \text{K}^{-1} \text{ (Boltzmann’s constant)}$

$c = 2.99 \times 10^8 \text{ m} \cdot \text{s}^{-1} \text{ (speed of light)}$
Figure 2 shows the relative contributions from the surface-emission term, surface radiance, and at-sensor radiance for a US Standard Atmosphere, quartz emissivity spectrum, and surface temperature set to 300 K. Vertical bars show the center placement of the three MODIS TIR bands 29 (8.55 µm), 31 (11 µm), and 32 (12 µm). The reflected downwelling term adds a small contribution in the window regions but will become more significant for more humid atmospheres. The at-sensor radiance shows large departures from the surface radiance in regions where atmospheric absorption from gases such as CO₂, H₂O, and O₃ are high.

Equation (1) gives the at-sensor radiance for a single wavelength, \( \lambda \), while the measurement from a sensor is typically measured over a range of wavelengths, or band. The at-sensor radiance for a discrete band, \( i \), is obtained by weighting and normalizing the at-sensor
spectral radiance calculated by equation (1) with the sensor’s spectral response function for each band, \( S_r \), as follows:

\[
L_i(\theta) = \int \frac{S_r(i) \cdot L(\theta) \cdot d\lambda}{S_r(i) \cdot d\lambda}
\]

(3)

Using equations (1) and (2), the surface radiance for band \( i \) can be written as a combination of two terms: Earth-emitted radiance, and reflected downward irradiance from the sky and surroundings:

\[
L_{s,i} = \varepsilon_i B_i(T_s) + (1 - \varepsilon_i)L_i^\uparrow = \frac{L_i(\theta) - L_i^\uparrow(\theta)}{\tau_i(\theta)}
\]

(4)

The atmospheric parameters, \( L_i^\downarrow, \tau_i(\theta), L_i^\uparrow(\theta) \), are estimated with a radiative transfer model such as MODTRAN (Kneizys et al. 1996b) discussed in the next section, using input atmospheric fields of air temperature, relative humidity, and geopotential height. Figure 3 shows MODIS spectral response functions for bands 29 (red), 31 (green) and 32 (blue) plotted with a typical transmittance curve for a mid-latitude summer atmosphere.

Figure 3. MODIS spectral response functions for bands 29 (red), 31 (green), and 32 (blue) plotted with a typical transmittance curve for a mid-latitude summer atmosphere.
4.2 Emissivity

The emissivity of an isothermal, homogeneous emitter is defined as the ratio of the actual emitted radiance to the radiance emitted from a black body at the same thermodynamic temperature (Norman and Becker 1995), $e_\lambda = R_\lambda / B_\lambda$. The emissivity is an intrinsic property of the Earth’s surface and is an independent measurement of the surface temperature, which varies with irradiance and local atmospheric conditions. The emissivity of most natural Earth surfaces for the TIR wavelength ranges between 8 and 12 μm and, for a sensor with spatial scales <100 m, varies from ~0.7 to close to 1.0. Narrowband emissivities less than 0.85 are typical for most desert and semi-arid areas due to the strong quartz absorption feature (reststrahlen band) between the 8- and 9.5-μm range, whereas the emissivity of vegetation, water, and ice cover are generally greater than 0.95 and spectrally flat in the 8–12-μm range.

4.3 Radiative Transfer Model

The current choice of radiative transfer model for atmospherically correcting MODIS TIR data is the latest version of the Moderate Resolution Atmospheric Radiance and Transmittance Model (MODTRAN) (Berk et al. 2005). MODTRAN has been sufficiently tested and validated and meets the speed requirements necessary for high spatial resolution data processing. The most recent MODTRAN 5.2 uses an improved molecular band model, termed the Spectrally Enhanced Resolution MODTRAN (SERTRAN), which has a much finer spectroscopy (0.1 cm$^{-1}$) than its predecessors (1–2 cm$^{-1}$), resulting in more accurate modeling of band absorption features in the longwave TIR window regions (Berk et al. 2005). Furthermore, validation with Line-by-Line models (LBL) has shown good accuracy.

Older versions of MODTRAN, such as version 3.5 and 4.0, have been used extensively in the past few decades for processing multi-band and broadband TIR and short-wave/visible imaging sensors such as ASTER data on NASA’s Terra satellite. Earlier predecessors, such as MODTRAN 3.5, used a molecular band model with 2 cm$^{-1}$ resolution and traced their heritage back to previous versions of LOWTRAN (Berk 1989; Kneizys et al. 1996a). With the next generation’s state-of-the-art, mid- and longwave IR hyperspectral sensors due for launch in the next decade, there has been greater demand for higher resolution and quality radiative transfer modeling. MODTRAN 5.2 has been developed to meet this demand by reformulating the MODTRAN molecular band model line center and tail absorption algorithms. Further
improvements include the auxiliary species option, which simulates the effects of HITRAN-specific trace molecular gases, and a new multiple scattering option, which improves the accuracy of radiances in transparent window regions.

Wan and Li (2008) have compared MODTRAN 4 simulations with clear-sky radiances from a well-calibrated, advanced Bomem TIR interferometer (MR100) and found accuracies to within 0.1 K for brightness temperature-equivalent radiance values.

4.4 Atmospheric Profiles

The general methodology for atmospherically correcting the MODIS TIR data will be based largely on the methods that were developed for the ASTER instrument (Palluconi et al. 1999). However, significant improvements will be made by taking advantage of newly developed techniques and more advanced algorithms to improve accuracy. Currently two options for atmospheric profile sources are available: 1) interpolation of data assimilated from Numerical Weather Prediction (NWP) models, and 2) retrieved atmospheric geophysical profiles from remote-sensing data. The NWP models use current weather conditions, observed from various sources (e.g., radiosondes, surface observations, and weather satellites) as input to dynamic mathematical models of the atmosphere to predict the weather. Data are typically output in 6-hour increments, e.g., 00, 06, 12, and 18 UTC. Examples include: the Global Data Assimilation System (GDAS) product provided by the National Centers for Environmental Prediction (NCEP) (Kalnay et al. 1990); the Modern Era Retrospective-analysis for Research and Applications (MERRA) product provided by the Goddard Earth Observing System Data Assimilation System Version 5.2.0 (GEOS-5.2.0) (Bosilovich et al. 2008); and the European Center for Medium-Range Weather Forecasting (ECMWF), which is supported by more than 32 European states. Remote-sensing data, on the other hand, are available real-time, typically twice daily and for clear-sky conditions. The principles of inverse theory are used to estimate a geophysical state (e.g., atmospheric temperature) by measuring the spectral emission and absorption of some known chemical species such as carbon dioxide in the thermal infrared region of the electromagnetic spectrum (i.e., the observation). Examples of current remote-sensing data include the Atmospheric Infrared Sounder (AIRS) (Susskind et al. 2003) and Moderate Resolution Imaging Spectroradiometer (MODIS) (Justice and Townshend 2002), both on NASA’s Aqua satellite launched in 2002.
The standard ASTER atmospheric correction technique, which is operated at the Land Processes Distributed Active Archive Center (LP DAAC) at the EROS Center in Sioux Falls, SD, uses input atmospheric profiles from the NCEP GDAS product at 1° spatial resolution and 6-hour intervals. An interpolation scheme in both space and time is required to characterize the atmospheric conditions for an ASTER image on a pixel-by-pixel basis. This method could potentially introduce large errors in estimates of air temperature and water vapor, especially in humid regions where atmospheric water vapor can vary on smaller spatial scales than 1°. The propagation of these atmospheric correction errors would result in band-dependent surface radiance errors in both spectral shape and magnitude, which in turn would result in errors of retrieved Level-2 products such as surface emissivity and temperature.

The plan for atmospherically correcting MODIS data for the MODTES algorithm will be to use coincident profiles from the joint MODIS MOD07/MYD07 atmospheric product (Seemann et al. 2003). The MOD07 product consists of profiles of temperature and moisture produced at 20 standard levels and total precipitable water vapor (TPW), total ozone, and skin temperature, produced at 5×5 MODIS 1-km pixels. The latest MOD07 algorithm update (v5.2) includes a new and improved surface emissivity training data set, with the result that RMSE differences in TPW between MOD07 and a microwave radiometer (MWR) at the Atmospheric Radiation Measurement (ARM) Southern Great Plains (SGP) site in Oklahoma were reduced from 2.9 mm to 2.5 mm (Seemann et al. 2008). Other validation campaigns have included comparisons with ECMWF and AIRS data, radiosonde observations (RAOBS), and MWR data at ARM SGP. Figure 4 shows biases and RMS differences between Aqua MODIS MOD07 and the “best estimate of the atmosphere” at the SGP ARMS site for air temperature (two left panels) and water vapor mixing ratio (right two panels). Results show that MOD07 has a ~4 K RMSE at the surface decreasing linearly to 2 K at 700 mb and then remaining at the 2–3 K until top of atmosphere. For water vapor, the RMSE near the surface is ~2.5 g/kg and decreasing to <0.5 g/kg above 600 mb.
4.5 Radiative Transfer Sensitivity Analysis

The accuracy of the proposed atmospheric correction technique relies on the accuracy of the input variables to the model, such as air temperature, relative humidity, and ozone. The combined uncertainties of these input variables need to be known if an estimate of the radiative transfer accuracy is to be estimated. These errors can be band-dependent, since different channels have different absorbing features and they are also dependent on absolute accuracy of the input profile data at different levels. The final uncertainty introduced is the accuracy of the radiative transfer model itself; however, this is expected to be small.

To perform the analysis, four primary input geophysical parameters were input to MODTRAN 5.2, and each parameter was changed sequentially in order to estimate the corresponding percent change in radiance (Palluconi et al. 1999). These geophysical parameters were air temperature, relative humidity, ozone, and aerosol visibility. Two different atmospheres were chosen, a standard tropical atmosphere and a mid-latitude summer atmosphere. These two simulated atmospheres should capture the realistic errors that we expect to see in humid conditions.

Typical values for current infrared sounder accuracies (e.g., AIRS) of air temperature and relative humidity retrievals in the boundary layer were used for the perturbations: 1) air temperature of 2 K, 2) relative humidity of 20%, 3) ozone was doubled, and 4) aerosol visibility was changed from rural to urban class. Numerical weather models such as NCEP would most
likely have larger uncertainties in the 1–2 K range for air temperature and 10–20% for relative humidity (Kalnay et al. 1990).

Table 1 shows the results for three simulated MODIS bands 29, 31, and 32 expressed as percent change in radiance (equivalent brightness temperature change in parentheses) for two standard atmospheric regimes, tropical and mid-latitude summer. The results show that band 29 is in fact most sensitive to perturbations in air temperature, followed by band 31 and 32 for both atmospheric profiles, with the mid-latitude profile having larger changes than tropical. For a 20% change in humidity the reverse is true, band 32 having the largest change of nearly 3 K for a tropical atmosphere, followed by band 31 and 29. This is because band 32 falls closest to strong water lines above 12 µm, as shown in Figure 2. Doubling the ozone results in a much larger sensitivity for band 5, since it is closest to the strong ozone absorption feature centered around the 9.5-µm region as shown in Figure 2. Changing the aerosol visibility from rural to urban had a small effect on each band but was largest for band 5. Generally, the radiance in the thermal infrared region is insensitive to aerosols in the troposphere so, for the most part, a climatology-based estimate of aerosols would be sufficient. However, when stratospheric aerosol amounts increase substantially due to volcanic eruptions, for example, then aerosol amounts from future NASA remote-sensing missions such as ACE and GEO-CAPE would need to be taken into account.

Table 1. Percent changes in simulated at-sensor radiances for changes in input geophysical parameters for MODIS bands 29, 31, and 32, with equivalent change in brightness temperature in parentheses.

<table>
<thead>
<tr>
<th>Geophysical Parameter</th>
<th>Change in Parameter</th>
<th>% Change in Radiance (Tropical Atmosphere)</th>
<th>% Change in Radiance (Mid-lat Summer Atmosphere)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Band 29 (8.5 µm)</td>
<td>Band 31 (11 µm)</td>
</tr>
<tr>
<td>Air Temperature</td>
<td>+2 K</td>
<td>−2.8 (1.44 K)</td>
<td>−1.97 (1.31 K)</td>
</tr>
<tr>
<td>Relative Humidity</td>
<td>+20%</td>
<td>3.51 (1.76 K)</td>
<td>3.91 (2.54 K)</td>
</tr>
<tr>
<td>Ozone</td>
<td>× 2</td>
<td>0.69 (0.35 K)</td>
<td>0.00 (0 K)</td>
</tr>
<tr>
<td>Aerosol</td>
<td>Urban/Rural</td>
<td>0.42 (0.21 K)</td>
<td>0.27 (0.17 K)</td>
</tr>
</tbody>
</table>

It should also be noted, as discussed in Palluconi et al. (1999), that in reality these types of errors may have different signs, change with altitude, and/or have cross-cancelation between
the parameters. As a result, it is difficult to quantify the exact error budget for the radiative transfer calculation; however, what we do know is that the challenging cases will involve warm and humid atmospheres where distributions of atmospheric water vapor are the most uncertain.

5 Water Vapor Scaling Method

The accuracy of the TES algorithm is limited by uncertainties in the atmospheric correction, which result in a larger apparent emissivity contrast. This intrinsic weakness of the TES algorithm has been systemically analyzed by several authors (Coll et al. 2007; Gillespie et al. 1998; Gustafson et al. 2006; Hulley and Hook 2009b; Li et al. 1999), and its effect is greatest over graybody surfaces that have a true spectral contrast that approaches zero. In order to minimize atmospheric correction errors, a Water Vapor Scaling (WVS) method has been introduced to improve the accuracy of the water vapor atmospheric profiles on a band-by-band basis for each observation using an Extended Multi-Channel/Water Vapor Dependent (EMC/WVD) algorithm (Tonooka 2005), which is an extension of the Water Vapor Dependent (WVD) algorithm (Francois and Otle 1996). The EMC/WVD equation models the at-surface brightness temperature, given the at-sensor brightness temperature, along with an estimate of the total water vapor amount:

\[ T_{g,i} = \alpha_{i,0} + \sum_{k=1}^{n} \alpha_{i,k} T_k \]

where:

\( i \) Band number
\( n \) Number of bands
\( W \) Estimate of total precipitable water vapor (cm)
\( p, q, r \) Regression coefficients for each band
\( T_k \) Brightness temperature for band \( k \) (K)
\( T_{g,i} \) Brightness surface temperature for band, \( i \)

The coefficients of the EMC/WVD equation are determined using a global-based simulation model with atmospheric data from the NCEP Climate Data Assimilation System (CDAS) reanalysis project (Tonooka 2005).
The scaling factor, $\gamma$, used for improving a water profile, is based on the assumption that the transmissivity, $\tau_i$, can be express by the Pierluissi double exponential band model formulation. The scaling factor is computed for each gray pixel on a scene using $T_{g,i}$ computed from equation (4) and $\tau_i$ computed using two different $\gamma$ values that are selected \textit{a priori}:

$$
\gamma^{a_i} = \frac{\ln \left( \frac{\tau_i(\theta, \gamma_2) \gamma_1^{a_i}}{\tau_i(\theta, \gamma_1) \gamma_2^{a_i}} \right)}{\ln(\tau_i(\theta, \gamma_2)/\tau_i(\theta, \gamma_1))} \left( \frac{B_i(T_{g,i}) - L_i(\theta, \gamma_1)/(1 - \tau_i(\theta, \gamma_1))}{L_i - L_i(\theta, \gamma_1)/(1 - \tau_i(\theta, \gamma_1))} \right)^{\gamma_1^{a_i} - \gamma_2^{a_i}}
$$

(6)

where:
- $\alpha_i$ Band model parameter
- $\gamma_1, \gamma_2$ Two appropriately chosen $\gamma$ values
- $\tau_i(\theta, \gamma_1, \gamma_2)$ Transmittance calculated with water vapor profile scaled by $\gamma$
- $L_i(\theta, \gamma_1, \gamma_2)$ Path radiance calculated with water vapor profile scaled by $\gamma$

Typical values for $\gamma$ are $\gamma_1 = 1$ and $\gamma_2 = 0.7$. Tonooka (2005) found that the $\gamma$ calculated by equation (6) will not only reduce biases in the water vapor profile, but will also simultaneously reduce errors in the air temperature profiles and/or elevation. An example of the water vapor scaling factor, $\gamma$, is shown in Figure 6 for a MODIS observation on 29 August 2004.

### 5.1 Gray Pixel Computation

It is important to note that $\gamma$ is only computed for graybody pixels (e.g., vegetation, water, and some soils) with emissivities close to 1.0 and, as a result, an accurate gray-pixel estimation method is required prior to processing. Vegetation indices such as the Normalized Difference Vegetation Index (NDVI), land cover databases (e.g., MODIS MOD12), and thermal log residuals (TLR) (Hook et al. 1992), are three different approaches that can be used in combination to identify graybody pixels. In the MOD21 product all pixels with photosynthetically active vegetation are first identified using the standard MODIS MOD13A2 (16-day) vegetation index product with an NDVI threshold (NDVI > 0.3). Water, ocean, and snow/ice pixels are then classified using a land-water and snow-cover map generated from the standard MODIS MOD10A2 product (8-day).

Using these gray pixels as a first-guess estimate, a TLR approach can be used to further refine the gray-pixel map, but at present the uncertainties introduced by this approach are still too high to use operationally. The TLR approach spectrally enhances images generated from multi-
spectral data and removes dependence on band-independent parameters such as surface
temperature. All gray pixels within a TLR image will have similar spectral features, and a
correlation coefficient approach is used to further refine the gray-pixel map based on the first-
guess gray pixels. For example, TLR pixels that have a correlation coefficient higher than 0.9
with the mean TLRs of the first guess gray pixels are further classified as graybodies. Figure 5
shows an example of the various stages of classifying graybodies for a MODIS scene cutout over
parts of Arizona and southeastern California (black = graybody, white = bare) on 29 August
2004. Using the NDVI and water mask all first-guess gray pixels are first classified (top right)
and then further refined with TLRs (bottom left) to produce the final graybody-pixel map.
Figure 5. Clockwise from top left: Google Earth visible image; first guess gray-pixel map; TLR refinement; and final gray pixel map for a MODIS scene cutout over parts of Arizona and southeastern California (black = graybody, white = bare) on 29 August 2004. See text for details.

5.2 Interpolation and Smoothing

Once $\gamma$ is computed for all gray pixels, the values are horizontally interpolated to adjacent bare pixels on the scene and smoothed before computing the improved atmospheric parameters. An inverse distance-weighted interpolation method is typically used to fill in bare
pixel gaps. This is an interpolation method frequently used in numerical weather forecasting with much success. The specific steps for interpolation of $\gamma$ values are as follows:

1. First all bare pixels are set to 1; in addition, all $\gamma$ values less than 0.2 and greater than 3 are set to 1 for stability purposes and to eliminate possible cloud contamination.

2. Next, all cloudy pixels on the scene are set to not a number (NaN).

3. All bare pixels are then looped over, and optimum weights are found for all gray pixels within a given effective radius of the bare pixel. The $\gamma$ value for the pixel is then computed using the weighted $\gamma$ values surrounding the pixel and ignoring all NaN values as follows:

$$\gamma(x, y) = \sum_{i=1}^{n} w_i \gamma_i$$  \hspace{1cm} (7)

where $n$ is the number of gray pixels, and $w_i$ are the weight functions assigned to each gray pixel $\gamma$ value:

$$w_i = \frac{d_i^{-p}}{\sum_{j=1}^{n} d_j^{-p}}$$  \hspace{1cm} (8)

where $p$ is weighting factor, called the power parameter, typically set to 4. Higher values give larger weights to the closest pixels. $d_i$ is the geometrical distance from the interpolation pixel to the scattered points of interest within some effective radius (~50 km for MOD21 was ideal):

$$d_i = \sqrt{(x - x_i)^2 + (y - y_i)^2}$$  \hspace{1cm} (9)

where $x$ and $y$ are the coordinates of the interpolation point, and $x_i$ and $y_i$ are coordinates of the scattered points.

If any bare pixels remain after the first pass, the bare pixels with a valid, calculated, $\gamma$ value are considered gray pixels, and the process is repeated until $\gamma$ values for all bare pixels have been computed.

This interpolation method should not introduce large error, since gray pixels are usually widely available in any given MODIS scene and atmospheric profiles do not change significantly at the medium-range scale (~50 km). Figure 6 shows an example of a $\gamma$ image for band 29 after interpolation and smoothing for the MODIS cutout shown in Figure 5.
5.3 Scaling Atmospheric Parameters

5.3.1 Transmittance and Path Radiance

Once the MODTRAN run has completed and the γ image has been interpolated and smoothed, the atmospheric parameters transmittance $\tau_i$ and path radiance $L_i^↓$ are modified as follows:

$$\tau_i(\theta, \gamma) = \tau_i(\theta, \gamma_1)^{\gamma_i^{\alpha_i-\gamma_i^{\alpha_i}} \cdot \tau_i(\theta, \gamma_2)^{\gamma_i^{\alpha_i-\gamma_i^{\alpha_i}}}}$$  \(10\)

$$L_i^↓(\theta, \gamma) = L_i^↓(\theta, \gamma_1) \cdot \frac{1 - \tau_i(\theta, \gamma)}{1 - \tau_i(\theta, \gamma_1)}$$  \(11\)

Once the transmittance and path radiance have been adjusted using the scaling factor, the surface radiance can be computed using equation (1).

5.3.2 Downward Sky Irradiance

In the WVS simulation model, the downward sky irradiance can be modeled using the path radiance, transmittance, and view angle as parameters. To simulate the downward sky irradiance in a MODTRAN run, the sensor target is placed a few meters above the surface, with surface emission set to zero and view angle set at prescribed values, e.g., Gaussian angles ($\theta = 0^\circ, 11.6^\circ, 26.1^\circ, 40.3^\circ, 53.7^\circ, \text{and } 65^\circ$). In this way, the only radiance contribution is from
the reflected downwelling sky irradiance at a given view angle. The total sky irradiance contribution is then calculated by summing up the contribution of all view angles over the entire hemisphere:

\[
L_i^↓ = \int_0^{2\pi} \int_0^{\pi/2} L_i^↓(\theta) \cdot \sin \theta \cdot \cos \theta \cdot d\theta \cdot d\delta
\]

(12)

where \( \theta \) is the view angle and \( \delta \) is the azimuth angle. However, to minimize computational time in the MODTRAN runs, the downward sky irradiance can be modeled as a non-linear function of path radiance at nadir view:

\[
L_i^↓(\gamma) = a_i + b_i \cdot L_i^↑(0, \gamma) + c_i L_i^↑(0, \gamma)^2
\]

(13)

where \( a_i, b_i, \) and \( c_i \) are regression coefficients (Table 2), and \( L_i^↑(0, \gamma) \) is computed by:

\[
L_i^↑(0, \gamma) = L_i^↑(\theta, \gamma) \cdot \frac{1 - \tau_i(\theta, \gamma)^{\cos \theta}}{1 - \tau_i(\theta, \gamma)}
\]

(14)

Tonooka (2005) found RMSEs of less than 0.07 W/m²/sr/µm for ASTER bands 10–14 when using equation (13) as opposed to equation (12). Figure 7 shows an example of comparisons between MODIS band 29 (8.55 µm) atmospheric transmittance (top), path radiance (middle), and computed surface radiance (bottom), before and after applying the WVS scaling factor, \( \gamma \), for the MODIS cutout shown in Figure 5. A decrease in transmittance and corresponding increase in path radiance values, after scaling over an area in the south of the image, show that the original atmospheric water absorption was underestimated using input MODIS MOD07 atmospheric profiles. The result is an increase in surface radiance over the bare regions of the Mojave Desert in the south of the image due to an increase in reflected downward sky irradiance.

Table 2. Regression coefficients for equation 13.

<table>
<thead>
<tr>
<th>Band</th>
<th>a</th>
<th>b</th>
<th>c</th>
</tr>
</thead>
<tbody>
<tr>
<td>29</td>
<td>0.0020</td>
<td>0.5794</td>
<td>0.0087</td>
</tr>
<tr>
<td>31</td>
<td>0.0221</td>
<td>0.5485</td>
<td>0.0203</td>
</tr>
<tr>
<td>32</td>
<td>0.0207</td>
<td>0.5360</td>
<td>0.0361</td>
</tr>
</tbody>
</table>
Figure 7. Comparisons between the atmospheric transmittance (top), path radiance (W/m²/µm⁻¹) (middle), and computed surface radiance (W/m²/µm⁻¹) (bottom), before and after applying the WVS scaling factor $\gamma$ to a MODIS scene cutout shown in Figure 5. Results are shown for MODIS band 29 (8.55 µm).
5.4 Calculating the EMC/WVD Coefficients

The EMC/WVD coefficients, $p, q, r$, from equation (5) are determined using a global simulation model with input atmospheric parameters from either numerical weather model or radiosonde data. Radiosonde databases such as the TIGR, SeeBor, and CLAR contain uniformly distributed global atmospheric soundings acquired both day and night in order to capture the full-scale natural atmospheric variability.

Geophysical profiles of air temperature, relative humidity, and geopotential height are used in combination with surface temperature and emissivity to simulate at-sensor brightness temperatures for the global set of profiles distributed uniformly over land. The air temperature profiles are then shifted by $-2, 0, +2$ K, while the humidity profiles are scaled by factors of $0.8, 1.0, 1.2$. These types of perturbations will help simulate a full range of atmospheric conditions. Furthermore, the surface temperatures are modified by $-5, 0, 5, 10$ K, and a set of 10 surface emissivity spectra are provided. These spectra are typically from gray materials, such as water, vegetation, snow, ice, and some types of soils, and tend to have values greater than 0.95. This ensures that the simulation results are not affected by uncertainties in surface emissivity, such as Lambertian effects. The at-sensor radiance is then computed using MODTRAN for the full set of profiles and perturbations ($3 \times 3 \times 4 \times 10 = 360$). The surface elevation is taken from a global DEM (e.g., ASTER GDEM), and the view angle is assumed to be nadir. Furthermore, a noise-equivalent differential temperature ($NE\Delta T$) of 0.05 K appropriate for MODIS thermal bands was applied using a normalized random number generator. Using the simulated at-sensor $T_k$, at-surface $T_g$ brightness temperatures, and an estimate of the total precipitable water vapor, the coefficients in equation (5) were be found by using a linear least-squares method. The coefficients are shown in Table 3 for MODIS bands 29, 31, and 32 including the RMSE (K). Table 4 shows the band model parameter coefficients used in equation (6) to calculate the water vapor scaling factor.

### Table 3. EMC/WVD coefficients used for estimating the at-surface brightness temperature in equation (5).

<table>
<thead>
<tr>
<th>Band</th>
<th>$p_{i,0}$</th>
<th>$q_{i,0}$</th>
<th>$r_{i,0}$</th>
<th>$p_{i,1}$</th>
<th>$q_{i,1}$</th>
<th>$r_{i,1}$</th>
<th>$p_{i,2}$</th>
<th>$q_{i,2}$</th>
<th>$r_{i,2}$</th>
<th>$p_{i,3}$</th>
<th>$q_{i,3}$</th>
<th>$r_{i,3}$</th>
<th>RMSE (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>29 (i=1)</td>
<td>$-9.992$</td>
<td>$13.719$</td>
<td>$-4.848$</td>
<td>$0.265$</td>
<td>$-0.255$</td>
<td>$0.148$</td>
<td>$2.947$</td>
<td>$1.215$</td>
<td>$-0.345$</td>
<td>$-2.170$</td>
<td>$-1.010$</td>
<td>$0.215$</td>
<td>$1.158$</td>
</tr>
<tr>
<td>31 (i=2)</td>
<td>$-7.284$</td>
<td>$12.036$</td>
<td>$-4.854$</td>
<td>$0.091$</td>
<td>$-0.151$</td>
<td>$0.135$</td>
<td>$3.316$</td>
<td>$1.011$</td>
<td>$-0.321$</td>
<td>$-2.376$</td>
<td>$-0.904$</td>
<td>$0.204$</td>
<td>$0.542$</td>
</tr>
<tr>
<td>32 (i=3)</td>
<td>$-7.397$</td>
<td>$9.397$</td>
<td>$-4.489$</td>
<td>$0.114$</td>
<td>$-0.129$</td>
<td>$0.132$</td>
<td>$3.211$</td>
<td>$0.968$</td>
<td>$-0.313$</td>
<td>$-2.294$</td>
<td>$-0.873$</td>
<td>$0.198$</td>
<td>$0.339$</td>
</tr>
</tbody>
</table>
Table 4. Band model parameters in equation (6).

<table>
<thead>
<tr>
<th>Band</th>
<th>Parameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>29</td>
<td>1.4294</td>
</tr>
<tr>
<td>31</td>
<td>1.8212</td>
</tr>
<tr>
<td>32</td>
<td>1.8273</td>
</tr>
</tbody>
</table>

6 Temperature and Emissivity Separation Approaches

The radiance in the TIR atmospheric window (8–13 µm) is dependent on the temperature and emissivity of the surface being observed according to Planck’s law. Even if the atmospheric properties (water vapor and air temperature) are well known and can be removed from equation (1), the problem of retrieving surface temperature and emissivity from multispectral measurements is still a non-deterministic process. This is because the total number of measurements available (N bands) is always less than the number of variables to be solved for (emissivity in N bands and one surface temperature). Therefore, no retrieval will ever do a perfect job of separation, with the consequence that errors in temperature and emissivity may co-vary. If the surface can be approximated as Lambertian (isotropic) and the emissivity is assigned a priori from a land-cover classification, then the problem becomes deterministic with only the surface temperature being the unknown variable. Examples of such cases would be over ocean, ice, or densely vegetated scenes where the emissivity is known a priori and spectrally flat in all bands. Another deterministic approach is the single-band inversion approach. If the atmospheric parameters are known in equation (1), then the temperature can also be solved for using a single band assuming the emissivity is known, usually in the clearest region of the window (~11 µm). Deterministic approaches are usually employed with sensors that have one or two bands in the TIR region using an SW approach, while non-deterministic approaches are applied to multispectral sensors with three or more bands in the TIR so that spectral variations in the retrieved emissivity can be related to surface composition and cover, in addition to retrieving the surface temperature. For the MODIS MOD21 product, a non-deterministic approach will be used in order to retrieve spectral emissivity in bands 29, 31, and 32, in addition to the surface temperature.
6.1 Deterministic Approaches

6.1.1 SW Algorithms

The most common deterministic approach can be employed without having to explicitly solve the radiative transfer equation. Two or more bands are employed in the window region (typically 10.5–12 µm), and atmospheric effects are compensated for by the differential absorption characteristics from the two bands. This approach is used with much success over oceans to compute the SST (Brown and Minnett 1999), as the emissivity of water is well known (Masuda et al. 1988). Variations of this method over land include the SW approach (Coll and Caselles 1997; Prata 1994; Price 1984; Wan and Dozier 1996; Yu et al. 2008), the multichannel algorithm (Deschamps and Phulpin 1980), and the dual-angle algorithm (Barton et al. 1989). Over land, the assumption is that emissivities in the SW bands being used are stable and well known and can be assigned using a land-cover classification map (Snyder et al. 1998). However, this assumption introduces large errors over barren surfaces where much larger variations in emissivity are found due to the presence of large amounts of exposed rock or soil, often with abundant silicates (Hulley and Hook 2009a). Land cover classification maps typically use Visible Near-Infrared (VNIR) data for assignment of various classes. This method may work for most vegetation types and over water surfaces but, because VNIR reflectances correspond predominately to Fe oxides and OH\(^-\) and not to the Si-O bond over barren areas, there is little or no correlation with silicate mineralogy features in thermal infrared data. This is why, in most classification maps, only one bare land class is specified (barren).

The primary LST product for MODIS (MOD11) currently uses a generalized SW approach (Wan and Dozier 1996), where coefficients are stratified according to view angle, total column water (TCW), and surface air temperature. Emissivities are assigned \textit{a priori} based on land cover classification maps. The MOD21 LST&E product will not be based on an SW algorithm as in MOD11, but will use a non-deterministic multi-spectral approach for the following reasons:

1. An SW method based on classification is not able to retrieve spectral emissivities of geologic surfaces for compositional analysis.
2. The emissivity of the land surface is in general heterogeneous and is dependent on many factors including surface soil moisture, vegetation cover changes, and surface compositional changes, which are not characterized by land classification maps.

3. SW algorithms are inherently very sensitive to measurement noise between bands.

4. Classification leads to sharp discontinuities and contours in the data between different class types, while a physical-based multispectral retrieval will produce seamless emissivity images.

5. Temperature inaccuracies are difficult to quantify over geologic surfaces where constant emissivities are assigned.

6.1.2 Single-Band Inversion

If the atmosphere is known, along with an estimate of the emissivity, then equation (1) can be inverted to retrieve the surface temperature using one band. Theoretically, any band used should retrieve the same temperature, but uncertainties in the atmospheric correction will result in subtle differences as different bands have stronger atmospheric absorption features than others that may be imperfectly corrected for atmospheric absorption. For example, a band near 8 µm will have larger dependence on water vapor, while the 9–10-µm region will be more susceptible to ozone absorption. Jimenez-Munoz and Sobrino (2010) applied this method to ASTER data by using atmospheric functions (AFs) to account for atmospheric effects. The AFs can be computed by the radiative transfer equation or empirically given the total water vapor content. The clearest ASTER band (13 or 14) was used to retrieve the temperature, with the emissivity determined using an NDVI fractional vegetation cover approach. A similar procedure has been proposed to retrieve temperatures from the Landsat TIR band 6 on ETM+ and TM sensors (Li et al. 2004). The single-band inversion method has not been proposed for MODIS data for the following reasons:

1. Inability to retrieve spectral emissivity of geologic surfaces for compositional analysis. This will not be possible with the single-band approach, which assigns emissivity based on land cover type and vegetation fraction.

2. Estimating emissivity from an NDVI-derived vegetation cover fraction over arid and semi-arid regions will introduce errors in the LST because NDVI is responsive only to
chlorophyll-active vegetation, and does not correlate well with senescent vegetation (e.g., shrublands).

3. Only one-band emissivity is solved for the single-band inversion approach. The MODIS MOD21 product will be based on a multispectral retrieval approach.

6.1.3 Non-deterministic Approaches

In non-deterministic approaches, the temperature and spectral emissivity are solved using an additional constraint or extra degree of freedom that is independent of the data source. These types of solutions are also rarely perfect because the additional constraint will always introduce an additional level of uncertainty; however, they work well over all surfaces (including arid and semi-arid) and can automatically account for land surface changes, such as those due to wildfires or surface soil moisture. First, we introduce two well-known approaches, the day/night and TISI algorithms, followed by an examination of the algorithms and methods that led up to establishment of the TES algorithm, which will be used in the MOD21 LST&E product.

6.1.3.1 Day/Night Algorithm

The constraint in the day/night algorithm capitalizes on the fact that the emissivity is an intrinsic property of the surface and should not change from day- to nighttime observations. The day/night algorithm is currently used to retrieve temperature/emissivity from MODIS data in the MOD11B1 product (Wan and Li 1997). The method relies on two measurements (day and night), and the theory is as follows: Two observations in N bands produce 2N observations, with the unknown variables being N-band emissivities, a day- and nighttime surface temperature, four atmospheric variables (day and night air temperature and water vapor), and an anisotropic factor, giving N + 7 variables. In order to make the problem deterministic, the following conditions must be met: 2N ≥ N+7, or N ≥ 7. For the MODIS algorithm, this can be satisfied by using bands 20, 22, 23, 29, and 31–33. Although this method is theoretically sound, the retrieval is complicated by the fact that two clear, independent observations are needed (preferably close in time) and the pixels from day and night should be perfectly co-registered. Errors may be introduced when the emissivity changes from day to night observation (e.g., due to condensation or dew), and from undetected nighttime cloud. In addition, the method relies on very precise co-registration between the day- and nighttime pixel.
6.1.3.2 Temperature Emissivity Separation Approaches

During research activities leading up to the ASTER mission, the ASTER TEWG was established in order to examine the performance of existing non-deterministic algorithms and select one that would be suitable for retrieving the most accurate temperature and/or emissivity over the entire range of terrestrial surfaces. This led to the development of the TES algorithm, which ended up being a hybrid algorithm that capitalized on the strengths of previous algorithms. In Gillespie et al. (1999), ten inversion algorithms were outlined and tested, leading up to development of TES. For all ten algorithms, an independent atmospheric correction was necessary. The ten algorithms were as follows: 1) Alpha-derived emissivity (ADE) method, 2) Classification method, 3) Day-Night measurement, 4) Emissivity bounds method, 5) Graybody emissivity method, 6) Mean Min-Max Difference (MMD) method, 7) Model emissivity method, 8) Normalized emissivity method (NEM), 9) Ratio Algorithm, and 10) SW algorithm.

In this document, we will briefly discuss a few of the algorithms but will not expand upon any of them in great detail. The Day-Night measurement (3), Classification (2), and SW (10) algorithms have already been discussed in section 4.2.1. A detailed description of all ten algorithms is available in Gillespie et al. (1999). The various constraints proposed in these algorithms can: determine spectral shape but not temperature, use multiple observations (day and night), assume a value for emissivity and calculate temperature, assume a spectral shape, or assume a relationship between spectral shape and minimum emissivity.

The NEM removes the downwelling sky irradiance component by assuming an $\varepsilon_{max}$ of 0.99. Temperature is then estimated by inverting the Planck function and a new emissivity found. This process is repeated until successive changes in the estimated surface radiances are small. This method in itself was not found to be suitable for ASTER because temperature inaccuracies tended to be high (>3 K) and the emissivities had incorrect spectral shapes. Other approaches have used a model to estimate emissivity at one wavelength (Lyon 1965) or required that the emissivity be the same at two wavelengths (Barducci and Pippi 1996). This introduces problems for multispectral data with more than five bands, e.g., ASTER.

The ADE method (Hook et al. 1992; Kealy et al. 1990; Kealy and Hook 1993) is based on the alpha residual method that preserves emissivity spectral shape but not amplitude or temperature. The introduced constraint uses an empirical relationship between spectral contrast and average emissivity to restore the amplitude of the alpha-residual spectrum and to compute
temperature. The average emissivity was used in the relationship to minimize band-to-band calibration errors. The TEWG used this key feature of the ADE method in TES, although the minimum emissivity, rather than the average emissivity, was used in the empirical relationship (Matsunaga 1994). The ADE itself was not fully employed for two primary reasons as discussed in Gillespie et al. (1999): 1) ADE uses Wien’s approximation, \( \exp(x) - 1 = \exp(x) \), which introduces a noticeable “tilt” in the residual spectra that gets transferred to the final emissivity spectra; and 2) This issue was easily fixed in the hybrid version of TES.

Lastly, the temperature-independent spectral indices (TISI) approach (Becker and Li 1990) computes relative emissivities from power-scaled brightness temperatures. TISI, however, is band-dependent and only recovers spectral shape; furthermore, the values are non-unique. To retrieve actual emissivities, additional information or assumptions are needed. Other algorithms, which only retrieve spectral shape, are the thermal log and alpha residual approach (Hook et al. 1992) and spectral emissivity ratios (Watson 1992; Watson et al. 1990). Neither of these was considered because they do not recover temperature or actual emissivity values.

### 6.2 TES Algorithm

The final TES algorithm proposed by the ASTER TEWG combined some core features from previous algorithms and, at the same time, improved on them. TES combines the NEM, the ratio, and the MMD algorithm to retrieve temperature and a full emissivity spectrum. The NEM algorithm is used to estimate temperature and iteratively remove the sky irradiance, from which an emissivity spectrum is calculated, and then ratioed to their mean value in the ratio algorithm. At this point, only the shape of the emissivity spectrum is preserved, but not the amplitude. In order to compute an accurate temperature, the correct amplitude is then found by relating the minimum emissivity to the spectral contrast (MMD). Once the correct emissivities are found, a final temperature can be calculated with the maximum emissivity value. Additional improvements involve a refinement of \( \epsilon_{max} \) in the NEM module and refining the correction for sky irradiance using the \( \epsilon_{min} \)-MMD final emissivity and temperature values. Finally, a quality assurance (QA) data image is produced that partly depends on outputs from TES such as convergence, final \( \epsilon_{max} \), atmospheric humidity, and proximity to clouds. More detailed discussion of QA is included later in this document.
Numerical modeling studies performed by the ASTER TEWG showed that TES can recover temperatures to within 1.5 K and emissivities to within 0.015 over most scenes, assuming well-calibrated, accurate radiometric measurements (Gillespie et al. 1998).

6.2.1 TES Data Inputs

Inputs to the TES algorithm are the surface radiance, $L_{s,i}$, given by equation (4) (at-sensor radiance corrected for transmittance and path radiance), and downwelling sky irradiance term, $L_{\lambda}^{\downarrow}$, which is computed from the atmospheric correction algorithm using a radiative transfer model such as MODTRAN. Both the surface radiance and sky irradiance will be output as a separate product. The surface radiance is primarily used as a diagnostic tool for monitoring changes in Earth’s surface composition. Before the surface radiance is estimated using equation (4), the accuracy of the atmospheric parameters, $L_{\lambda}^{\uparrow}(\theta)$, is improved upon using a WVS method (Tonooka 2005) on a band-by-band basis for each observation using an extended multi-channel/water vapor dependent (EMC/WVD) algorithm.

6.2.2 TES Limitations

As with any retrieval algorithm, limitations exist that depend on measurement accuracy, model errors, and incomplete characterization of atmospheric effects. Currently, the largest source of uncertainty for ASTER data is the residual effect of incomplete atmospheric correction. Measurement accuracy and precision contribute to a lesser degree. This problem is compounded for graybodies, which have low spectral contrast and are therefore more prone to errors in “apparent” MMD, which is overestimated due to residual sensor noise and incomplete atmospheric correction. A threshold classifier was introduced by the TEWG to partly solve this problem over graybody surfaces. Instead of using the calibration curve to estimate $\varepsilon_{\text{min}}$ from MMD, a value of $\varepsilon_{\text{min}} = 0.983$ was automatically assigned when the spectral contrast or MMD in emissivity was smaller than 0.03 for graybody surfaces (e.g., water, vegetation). However, this caused artificial step discontinuities in emissivity between vegetated and arid areas.

At the request of users, two parameter changes were made to the ASTER TES algorithm on 1 August 2007, first described in Gustafson et al. (2006). Firstly, the threshold classifier was removed as it caused contours and artificial boundaries in the images, which users could not tolerate in their analyses. The consequence of removing the threshold classifier was a smoother appearance for all images but at the cost of TES underestimating the emissivity of graybody
scenes, such as water by up to 3% and vegetation by up to 2% (Hulley et al. 2008). The second parameter change removed the iterative correction for reflected downwelling radiation, which also frequently failed due to inaccurate atmospheric corrections (Gustafson et al. 2006). Using only the first iteration resulted in improved spectral shape and performance of TES.

Figure 8 shows the distribution of LST uncertainties for the MODIS and ASTER TES algorithm with respect to TCW and simulated LST for TES+atm (atmospheric uncertainty) and TES+atm+wvs (atmospheric uncertainty with WVS) simulation cases. In general the TES+atm uncertainties increase with TCW and simulated LST for both types of surfaces and range from 4–6 K for TCW values greater than 4 cm and LSTs greater than 300 K. The TES+atm+wvs results show that applying the WVS method reduces the LST uncertainty at higher TCW contents by more than a factor of two, with uncertainties not exceeding 2 K for either type of surface type or sensor.

![Figure 8. ASTER (left panels) and MODIS (right panels) LST uncertainty distributions plotted versus TCW and simulated LST for all end-member surface types (graybody, soils, sands, and rocks), for the TES algorithm including atmospheric error (TES+atm) and with the WVS method applied (TES+atm+wvs).](image-url)
6.2.3 TES Processing Flow

Figure 9 shows the processing flow diagram for the generation of the cloud masks, land-leaving radiance, VNIR reflectances, and TES temperature and emissivity, while Figure 10 shows a more detailed processing flow of the TES algorithm itself. Each of the steps will be presented in sufficient detail in the following section, allowing users to regenerate the code. TES uses input image data of surface radiance, $L_{s,t}$, and sky irradiance, $L_{d,t}$, to solve the TIR radiative transfer equation. The output images will consist of three emissivity images ($\varepsilon_t$) corresponding to MODIS bands 29, 31, 32, and one surface temperature image ($T$).

Figure 9. Flow diagram showing all steps in the retrieval process in generating the MODIS MOD21 LST&E product starting with TIR at-sensor radiances and progressing through atmospheric correction, cloud detection, and the TES algorithm.
Figure 10. Flow diagram of the TES algorithm in its entirety, including the NEM, RATIO, and MMD modules. Details are included in the text, including information about the refinement of $\epsilon_{max}$. 
6.2.4 NEM Module

The NEM builds upon the model emissivity algorithm (Lyon 1965) by allowing the initial $\epsilon_{\text{max}}$ value to be consistent for all wavelengths. The role of NEM is to compute the surface kinetic temperature, $T$, and a correct shape for the emissivity spectrum. An initial value of 0.99 is set for $\epsilon_{\text{max}}$, which is typical for most vegetated surfaces, snow, and water. For geologic materials such as rocks and sand, $\epsilon_{\text{max}}$ values are set lower than this, typically 0.96, and this value remains fixed. For all other surface types, a modification to the original NEM allows for optimization of $\epsilon_{\text{max}}$ using an empirically based process. For the majority of materials in the ASTER spectral library, a typical range for $\epsilon_{\text{max}}$ is $0.94 < \epsilon_{\text{max}} < 1.0$. Therefore, for a material at 300 K, the maximum errors that NEM temperatures should have are $\sim \pm 1.5$ K, assuming the reflected sky irradiance has been estimated correctly.

6.2.5 Subtracting Downwelling Sky Irradiance

Generally the effects of sky irradiance are small with typical corrections of $<1$ K (Gillespie et al. 1998). However, the contribution becomes larger for pixels with low emissivity (high reflectance) or in humid conditions when the sky is warmer than the surface. Over graybody surfaces (water and vegetation), the effects are small because of their low reflectivity in all bands. The first step of the NEM module is to estimate ground-emitted radiance, which is found by subtracting the reflected sky irradiance from the surface radiance term:

\[
R_i = L_{s,i} - (1 - \epsilon_{\text{max}}) L_{\lambda}^1
\]  

(15)

The NEM temperature, which we call $T_{\text{NEM}}$, is then estimated by inverting the Planck function for each band using $\epsilon_{\text{max}}$ and the ground-emitted radiance and then taking the maximum of those temperatures. The maximum temperature will most likely be closest to the actual surface temperature in the presence of uncompensated atmospheric effects.

\[
T_i = \frac{c_2}{\lambda_i} \left( \ln \left( \frac{c_1 \epsilon_{\text{max}}}{\pi R_i \lambda_i^5} + 1 \right) \right)^{-1}
\]  

(16)

\[
T_{\text{NEM}} = \max(T_i)
\]  

(17)

The NEM emissivity spectrum is then calculated as the ratio of emitted radiance to that of a blackbody with a temperature estimated by $T_{\text{NEM}}$:

\[
\epsilon_i' = \frac{R_i}{B_i(T_{\text{NEM}})}
\]  

(18)
The new emissivity spectrum is then used to re-calculate \( R'_i = L'_{s,i} - (1 - \epsilon'_i) L'_1 \), and the process is repeated until convergence, which is determined if the change in \( R_i \) between steps is less than a set threshold, \( t_2 \), which is set as the radiance equivalent to NE\( \Delta T \) of the sensor. The process is stopped if the number of iterations exceeds a limit \( N \), set to 12. Execution of the NEM module is also aborted if the slope of \( R_i \) versus iteration, \( c \), increases such that \( |\Delta^2 R'/\Delta c^2| > t_1 \), where \( t_1 \) is also set to radiance equivalent of NE\( \Delta T \) for the sensor (0.05 K for MODIS). In this case, correction is not possible, TES is aborted, and NEM values of \( \epsilon_i \) and \( T_{NEM} \) are reported in the QA data plane, along with an error flag. TES is also aborted and an error flag recorded if, for any iteration, the values of \( \epsilon_i \) fall out of reasonable limits, set to \( 0.5 < \epsilon_i < 1.0 \). See Figure 10 for a detailed description of these steps.

### 6.2.6 Refinement of \( \epsilon_{max} \)

Most pixels at MODIS resolution (1 km) will contain a mixed cover type consisting of vegetation and soil, rock and water. The effective maximum emissivity for such pixels will therefore vary across the scene and depend on the fractional contribution of each cover type. For these cases, the initial \( \epsilon_{max} = 0.99 \) may be set to high and refinement of \( \epsilon_{max} \) is necessary to improve accuracy of \( T_{NEM} \). The optimal value for \( \epsilon_{max} \) minimizes the variance, \( \nu \), of the NEM calculated emissivities, \( \epsilon_i \). The optimization of \( \epsilon_{max} \) is only useful for pixels with low emissivity contrast (near graybody surfaces) and therefore is only executed if the variance for \( \epsilon_{max} = 0.99 \) is less than an empirically determined threshold (e.g., \( V_1 = 1.7 \times 10^{-4} \) for ASTER) (Gillespie et al. 1998). If the variance is greater than \( V_1 \), then the pixel is assumed to predominately consist of either rock or soil. For this case, \( \epsilon_{max} \) is reset to 0.96, which is a good first guess for most rocks and soils in the ASTER spectral library, which typically fall between the 0.94 and 0.99 range. For MODIS the \( \epsilon_{max} \) values is set to 0.97, a typical value for bare surfaces in the 12 \( \mu \)m range. If the first condition is met, and the pixel is a near-graybody, then values for \( \epsilon_{max} \) of 0.92, 0.95, 0.97, and 0.99 are used to compute the variance for each corresponding NEM emissivity spectrum. A plot of variance \( \nu \) versus each \( \epsilon_{max} \) value results in an upward-facing parabola with the optimal \( \epsilon_{max} \) value determined by the minimum of the parabola curve in the range \( 0.9 < \epsilon_{max} < 1.0 \). This minimum is set to a new \( \epsilon_{max} \) value, and the NEM module is executed again to compute a new \( T_{NEM} \). Further tests are used to see if a reliable solution can be found for the refined \( \epsilon_{max} \). If the parabola is too flat, or too steep, then refinement is aborted and the original
$\epsilon_{max}$ value is used. The steepness condition is met if the first derivative (slope of $\nu$ vs. $\epsilon_{max}$) is greater than a set threshold (e.g., $V_2 = 1.0 \times 10^{-3}$ for ASTER) and the flatness conditions is met if the second derivative is less than a set threshold (e.g., $V_3 = 1.0 \times 10^{-3}$ for ASTER). Finally, if the minimum $\epsilon_{max}$ corresponds to a very low $\nu$, then the spectrum is essentially flat (graybody) and the original $\epsilon_{max} = 0.99$ is used. This condition is met if $\nu_{min} < V_4$ (e.g., $V_2 = 1.0 \times 10^{-4}$).

Table 5 shows typical output from various stages of the TES algorithm for pixels representing three different surface types: sand dunes, vegetated cropland, and semi-vegetated cropland for a MODIS scene on 29 August 2004 over the Imperial Valley, southeastern California. Note the different $\epsilon_{max}$ value for each of these surface types. The dune pixel was set to 0.97 because of high variance in the NEM spectrum; the Salton Sea and shrubland pixels were set to 0.983, due to a lower spectral contrast.

Table 5. Output from various stages of the MODTES algorithm for three surface types: sand dunes, Salton Sea, and shrubland transition zone for a MODIS test scene over the Imperial Valley, southeastern California.

<table>
<thead>
<tr>
<th></th>
<th>Algodones Dunes</th>
<th>Salton Sea</th>
<th>Shrubland (transition zone)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\epsilon_{max}$</td>
<td>0.97</td>
<td>0.983</td>
<td>0.97</td>
</tr>
<tr>
<td>MMD</td>
<td>0.166</td>
<td>0.006</td>
<td>0.088</td>
</tr>
<tr>
<td>$\epsilon_{min}$</td>
<td>0.817</td>
<td>0.975</td>
<td>0.886</td>
</tr>
<tr>
<td>$T_{NEM}$</td>
<td>327.27 K</td>
<td>304.76 K</td>
<td>325.61 K</td>
</tr>
<tr>
<td>$T_{TES}$</td>
<td>326.51 K</td>
<td>304.95 K</td>
<td>325.75 K</td>
</tr>
</tbody>
</table>

6.2.7 Ratio Module

In the ratio module, the NEM emissivities are ratioed to their average value to calculate a $\beta_i$ spectrum as follows:

$$\beta_i = \frac{\epsilon_i}{\bar{\epsilon}}$$  \hspace{1cm} (19)

Typical ranges for the $\beta_i$ emissivities are $0.75 < \beta_i < 1.32$, given that typical emissivities range from 0.7 to 1.0. Errors in the $\beta_i$ spectrum due to incorrect NEM temperatures are systematic.

6.2.8 MMD Module

In the MMD module, the $\beta_i$ emissivities are scaled to an actual emissivity spectrum using information from the spectral contrast or MMD of the $\beta_i$ spectrum. The MMD can then be related to the minimum emissivity, $\epsilon_{min}$, in the spectrum using an empirical relationship
determined from lab measurements of a variety of different spectra, including rocks, soils, vegetation, water, and snow/ice. From $\epsilon_{\text{min}}$, the actual emissivity spectrum can be found by re-scaling the $\beta_i$ spectrum. First, the MMD of the $\beta_i$ spectrum is found by:

$$MMD = \max(\beta_i) - \min(\beta_i)$$

(20)

Then MMD can be related to $\epsilon_{\text{min}}$ using a power-law relationship:

$$\epsilon_{\text{min}} = \alpha_1 - \alpha_2 \cdot MMD^{\alpha_3},$$

(21)

where $\alpha_i$ are coefficients that are obtained by regression using lab measurements. For the three MODIS TIR bands between 8 and 12 µm (shown in Figure 2), the values for the coefficients were calculated as $\alpha_1 = 0.985$, $\alpha_2 = 0.7503$, and $\alpha_3 = 0.8321$. The TES emissivities are then calculated by re-scaling the $\beta_i$ emissivities:

$$\epsilon^{\text{TES}}_i = \beta_i \left( \frac{\epsilon_{\text{min}}}{\min(\beta_i)} \right)$$

(22)

An example MODTES emissivity output image for band 29 (8.55 µm) is shown in Figure 11 for an MODIS cutout on 29 August 2004 over the Imperial Valley, southeastern California. Bare areas, such as the Algodones Dunes running diagonally across the southeast corner, generally have emissivity $<0.85$, while graybody surfaces such as the Imperial Valley croplands and Salton Sea in the southwest corner of the image have higher emissivities, $>0.95$. Figure 12 shows the differences in emissivity spectra between the NEM and TES output for pixels over three different surface types (sand dunes, Salton Sea water, and mixed shrubland) for the Imperial Valley cutout. Note that, although both NEM and TES have similar spectral shape, the emissivities of NEM are generally higher than TES because of the initial estimate of $\epsilon_{\text{max}}$ in the NEM module. The Algodones Dunes spectrum has high spectral contrast, which is typical for a quartz spectrum that has the characteristic quartz doublet in the 8–10-µm region, while the emissivity of water is usually spectrally flat, and high.
Figure 11. Clockwise from top left: MODIS cutouts of land surface emissivity for band 29 (8.55 µm); band 31 (11 µm); band 32 (12 µm); and surface temperature products output from the TES algorithm over the Imperial Valley, southeastern California on 29 August 2004.

Figure 12. MODIS derived TES and NEM emissivity spectra for three different surface types for the MODIS cutout shown in Figure 11: Algodones Dunes, Salton Sea, and shrublands (mixed soil and vegetation). Details of the TES and NEM outputs from these spectra are shown in Table 5.
For pixels with low spectral contrast (e.g., graybody surfaces), the accuracy of MMD calculated from TES is compromised and approaches a value that depends on measurement error and residual errors from incomplete atmospheric correction. For ASTER, which has a NEΔT of 0.3 K at 300 K, measurement error contributes to the apparent contrast, and a method was explored to correct the apparent MMD using Monte Carlo simulations. For MODIS (NEΔT of 0.05 K), we expect measurement errors to be minimal and atmospheric effects to be the largest contribution to MMD errors. A further problem for graybody surfaces is a loss of precision for low MMD values. This is due to the shape of the power-law curve of $\epsilon_{min}$ vs. MMD at low MMD values, where small changes in MMD can lead to large changes in $\epsilon_{min}$. To address these issues, the ASTER TEWG initially proposed a threshold classifier for graybody surfaces.

If MMD < 0.03, the value of $\epsilon_{min}$ in equation (12) was set to 0.983, a value typical for water and most vegetated surfaces. However, this classification was later abandoned as it introduced large step discontinuities in most images (e.g., from vegetation to mixed-cover types). The consequence of removing the threshold classifier was that, over graybody surfaces, errors in emissivity could range from 0.01 to 0.05 (0.5 K to 3 K) due to measurement error and residuals errors from atmospheric correction (Gustafson et al. 2006; Hulley and Hook 2009b). For MOD21, we use original TES without classification and the WVS method to correct the atmospheric parameters on a pixel-by-pixel basis.

For bare surfaces (rocks, soils, and sand), the error in NEM-calculated T may be as much as 2–3 K, assuming a surface at 340 K due to the fixed assumption of $\epsilon_{max} = 0.96$. This error can be corrected by recalculating T using the TES retrieved maximum emissivity, $\epsilon_{max}^{TES}$, and the atmospherically corrected radiances, $R_i$. The maximum emissivity used as correction for reflected $L^1_\lambda$ will be minimal.

$$T^{TES} = \frac{c_2}{\lambda_{max}} \left( \ln \left( \frac{c_1 \epsilon_{max}^{TES}}{\pi R_i \lambda_{max}^5} + 1 \right) \right)^{-1}$$

An example MODTES surface temperature output image is shown in Figure 11. Bare areas of the Mojave desert generally have the highest temperatures with $T > 330$ K, while graybody surfaces such as the Imperial Valley croplands and Salton Sea in the southwest corner have the coolest temperatures with $T < 310$ K.

In the original ASTER TES algorithm, a final correction is made for sky irradiance using the TES temperature and emissivities; however, this was later removed, as correction was
minimal and influenced by atmospheric correction errors. This additional correction is not used for the MODTES algorithm.

6.2.9 MMD vs. $\epsilon_{min}$ Regression

The relationship between MMD and $\epsilon_{min}$ is physically reasonable and is determined using a set of laboratory spectra in the ASTER spectral library v2.0 (Baldrige et al. 2009) and referred to as the calibration curve. The original ASTER regression coefficients were determined from a set of 86 laboratory reflectance spectra of rocks, soils, water, vegetation, and snow supplied by J.W. Salisbury from Johns Hopkins University. One question that needed to be answered was whether using a smaller or larger subset of this original set of spectra changed the results in any manner. Establishing a reliable MMD vs. $\epsilon_{min}$ relationship with a subset of spectral representing all types of surfaces is a critical assumption for the calibration curve. This assumption was tested using various combinations and numbers of different spectra (e.g., Australian rocks, airborne data, and a subset of 31 spectra from Salisbury), and all yielded very similar results to the original 86 spectra.

For MODIS, the original 86 spectra were updated to include additional sand spectra used to validate the North American ASTER Land Surface Emissivity Database (NAALSED) (Hulley and Hook 2009b) and additional spectra for vegetation from the MODIS spectral library and ASTER spectral library v2.0, giving a total of 150 spectra. The data were convolved to the three MODIS TIR bands and $\epsilon_{min}$ and $\beta_t$ spectra calculated using equation (9) for each sample. The MMD for each spectrum was then calculated from the $\beta_t$ spectra and regressed to the $\epsilon_{min}$ values. The relationship follows a simple power law given by equation (11), with regression coefficients $\alpha_1 = 0.997$, $\alpha_2 = 0.7050$, and $\alpha_3 = 0.7430$, and $R^2 = 0.987$. Figure 13 shows the power-law relationship between MMD and $\epsilon_{min}$ using the 150 lab spectra.
6.2.10 Atmospheric Effects

The accuracy of the atmospheric correction technique used to estimate the surface radiance relies on the accuracy of the variables input to the radiative transfer model (e.g., air temperature, relative humidity, and ozone). A sensitivity analysis has shown (Table 1) that a change in atmospheric water vapor of 20% leads to a 4.43% change in radiance for MODIS band 12 (12 µm), which is the most susceptible to atmospheric absorption and emission of the three MODIS TIR bands, while a change in air temperature of 2 K leads to a \(-1.6\%\) change in radiance for a tropical atmosphere. Changes in ozone and aerosol amount had much smaller effects, except for MODIS band 29 (8.55 µm), which falls closer to the ozone absorption region at 9.6 µm. These atmospheric errors tend to be highly correlated from band to band, since each channel has a characteristic absorbing feature. As a result, the effect on TES output is usually relatively small, but if these errors are uncorrelated from band to band then much larger errors can occur, particularly for graybodies, where small changes in MMD can significantly alter the shape of the emissivity spectrum. For example, over water bodies, errors in emissivity of up to 3\% (0.03) have been found due to uncompensated atmospheric effects (Hulley and Hook 2009b; Tonooka and Palluconi 2005).

One method for improving the accuracy of the surface radiance product is to apply the WVS method (Tonooka 2005). Using 183 ASTER scenes over lakes, rivers, and sea surfaces, it was found that using the WVS method instead of the standard atmospheric correction improved
estimates of surface temperature from 3 to 8 K in regions of high humidity (Tonooka 2005). These are substantial errors when considering that the required accuracy of the TES algorithm is ~1 K (Gillespie et al. 1998).

Figure 14 shows emissivity spectra over the Salton Sea, showing the effects of applying the WVS atmospheric correction method on the shape of the emissivity spectrum when compared to using the standard (STD) correction method without WVS. The emissivity spectrum of water is high (~0.98) and flat and the results in Figure 14 show a dramatic improvement in emissivity accuracy in both magnitude (up to 0.06 for ASTER band 11, and 0.09 for MODIS band 29) and spectral shape when using the WVS as opposed to the STD method. Because of the humid day, where MOD07 precipitable water vapor (PWV) values were around 4 cm over the water, the spectral contrast of the STD emissivity results are overestimated for ASTER and MODIS data. However, when applying the WVS method, the ASTER emissivity spectra fall within 0.015 of the lab-measured spectrum, while MODIS emissivity spectra are within 0.005 at all wavelengths. Differences between the 3- and 5-band TES algorithm applied to ASTER data were small.
Figure 14. Emissivity spectra comparisons on June 15, 2000 over the Salton Sea between ASTER (3-band), ASTER (5-band), and MODTES, using the TES algorithm along with lab spectra of water from the ASTER spectral library. Results from the WVS method and the STD atmospheric correction are also shown. An estimate of the PWV from the MOD07 atmospheric product indicates very high humidity on this day.

7 Advantages of TES over SW approaches

The LST accuracy of SW algorithms is strongly dependent on emissivity variability (Wan and Dozier 1996; Yu et al. 2005). Any errors in the assigned SW classification emissivities can translate into large errors in LST. For example, Galve et al. (2008) showed that, on average, a band emissivity error of 0.005 (0.5%) will result in an LST error of 0.7 K using the SW approach. The sensitivity of the current MODIS GSW algorithm to the view zenith angle is of roughly the same magnitude as emissivity, but can be compensated for by introducing an atmospheric path-length term, while sensitivity to differences in surface and air temperature are typically much smaller, but can be large over bare areas.

Classification emissivity errors can stem from three main sources: 1) misclassification in the original cover type, 2) errors in emissivity within the cover-type map, or 3) a dynamic change in the cover-type map. A misclassification in cover type will occur when the land class algorithm does not classify the true cover type correctly. According to a validation study on MODIS land
cover product, it was found that the accuracy of individual classes ranged from 60–90% (Strahler et al. 2002). Emissivity errors within a cover-type map occur when a class (e.g., barren) does not represent the range in emissivities within that class. And lastly, dynamic errors occur after sudden natural surface changes, e.g., rainfall, wildfires, or phenological changes, resulting in emissivity changes within the land cover type. Error sources 1) and 3) can be grouped together since they both arise due to misclassification.

7.1 Land Cover Misclassification

The first emissivity error source we investigate arises from land cover misclassification. We looked at the effects of a dynamic land cover change on emissivity and LST retrieved values after the Station fire in Los Angeles, which burned nearly 161,000 acres of land in the Angeles National Forest region from 26 August–19 September 2009. Figure 15 shows emissivity (left panels) and LST images (right panels) for ASTER and MODIS data on 10 October 2009. Top and middle panels show ASTER and MODIS (MOD TES) results using the TES algorithm, and bottom panels show the MOD11 band 31 (11 µm) emissivity classification (left) and MOD11 LST (right).
Figure 15. Emissivity images (left) and surface temperature images (right) for ASTER (top), MODIS TES (MODTES) (center) and MODIS SW (MOD11_L2) (bottom) products over the Station Fire burn scar just north of Pasadena, CA. Location of JPL in Pasadena and burn scar area indicated at top right. MODTES and ASTER results match closely; however, the MOD11_L2 temperatures are underestimated by as much as 12 K, due to an incorrect emissivity classification.

The Station fire burn area is clearly seen in the center of the ASTER and MODTES results as an area of lower emissivity in the longwave region, and is roughly 0.04 (4%) lower than a typical value for vegetation of 0.98. This decrease in emissivity is not evident in the MODIS GSW results in which the emissivity has been assigned to a forest land cover type with a value of 0.981. The ASTER and MODIS TES results show corresponding high LSTs (320–325 K) over the burn region, while MOD11 LSTs are 5–12 K lower and range from 312–316 K over the burn scar area as shown in Figure 1–4. This is a direct consequence of not taking the
change in emissivity into account. This error far exceeds the specification for the MODIS product (1 K) (Wan 1999) and the VIIRS product (2.5K) (Yu et al. 2005).

### 7.2 Emissivity Error within Cover Type

The second major emissivity error in land-cover–type algorithms occurs when the classification is correct, but the emissivities assigned to the class are incorrect. Here we show an example over Mauna Loa caldera in Hawaii (Figure 16). The caldera is approximately 5×3 km in size and consists of flat, smooth pahoehoe basalt with minimal vegetation (Sabol et al. 2009). Figure 16 shows an ASTER emissivity image (9.1 µm) of the Mauna Loa region on the 5 June 2000 with the caldera indicated on the map. The accompanying emissivity spectra show ASTER, MODTES and MOD11 classification-based emissivities for bands 31 and 32. It is clear the ASTER and MODTES spectra match closely and show the characteristic basalt emissivity minima in the 10.5–11.5 µm region, while the MOD11 classification emissivities are too high by almost 0.1 in band 31, and 0.04 in band 32. Consequently there is a large discrepancy of up to 12 K between the MODTES and the MOD11 LST product as a result of MOD11 misclassification. This far exceeds the specification for the MOD11 product accuracy (1 K) (Wan 1999) and the VIIRS product (2.5 K) (Yu et al. 2005).

![Figure 16](image)

Figure 16. (left) ASTER band 12 (9.1 µm) emissivity image over Mauna Loa caldera, Hawaii on 5 June 2000, and (right) emissivity spectra from ASTER, MODTES, and MOD11 emissivity classification. While ASTER and MODTES agree closely, MOD11 emissivities are too high, resulting in large LST discrepancies between MODTES and MOD1 (12 K) due to misclassification in bands 31 (11 µm) and 32 (12 µm).
7.3 Soil Moisture Effects

LST errors of this magnitude will occur in a systematic fashion any time that the classification emissivities do not reflect the true spectral shape of the surface being measured. Other factors contributing to emissivity variability include rainfall, which increases the surface soil moisture, and therefore the emissivity due to lower reflectance over bare surfaces.

An example of the effects of rainfall on the emissivity is shown in Figure 17. Hulley et al. (2010) used a case study over the Namib desert to show that the emissivity of bare soils retrieved from physical algorithms such as TES and the MODIS day/night algorithm increased by up to 0.03 due to soil moisture changes in the thermal bands used by SW algorithms (11 µm), while the SW emissivity values were held constant throughout the rainfall period (19–23 April). The MODIS SW product had cooler mean temperatures of more than 2 K as a result of not taking into account these emissivity changes. Again, a 0.5–1 K LST error can lead to a 10% error in sensible heat flux and evapotranspiration, and a 1–3 K error can lead to surface flux errors of up to 100 W/m² (Yu et al. 2005). Other examples of emissivity misclassification could occur due to intra-annual crop rotation, where fields may go from bare to fully vegetated over short time periods.

Figure 17. (top) Emissivity variation for a rainfall event over the Namib desert showing results from MOD11B1 v4 (day/night algorithm), MOD11_L2 (SW), and MODIS TES (MODTES). (bottom) Corresponding soil moisture variation from AMSR-E and rainfall estimates from the Tropical Rainfall Measuring Mission (TRMM). It is clear that the physical retrievals, show increases in emissivity due to soil moisture, whereas the SW values are held constant throughout the rainfall period from 15–21 April. From Hulley et al. (2010).
8 Quality Assessment and Diagnostics

The T and $\varepsilon$ products will need to be assessed using a set of quality control (QC) flags. These QC flags will involve automatic tests processed internally for each pixel and will depend on various retrieval conditions such as whether the pixel is over land or ocean surface, the atmospheric water vapor content (dry, moist, very humid, etc.), and cloud cover. The data quality attributes will be set automatically according to parameters set on data conditions during algorithm processing and will be assigned as either “bad,” “suspect,” or “good.” Estimates of the accuracy and precision of the T and $\varepsilon$ product will be reported in a separate data plane. At each step in the TES algorithm, a variety of performance information will be output, which will give the user a summary of algorithm statistics in a spatial context. This type of information will be useful for determining surface type, atmospheric conditions, and overall performance of TES.

The architecture of the MODIS T and $\varepsilon$ QA data plane will closely resemble that of ASTER (Gillespie et al. 1998). It will consist of header information followed by three 8-bit QA data planes. The structure of the first QA data plane will consist of three primary fields, which are detailed in Table 6:

1. Data Quality Field: “bad,” “suspect,” or “good,” to be assigned to specific bit patterns.
2. Cloud Mask Field: Outputs from cloud mask statistics, e.g., optically thick or thin cloud, cirrus or contrails, clear, or snow/ice determined from NDSI threshold.
3. Cloud Adjacency: Clear pixels defined in the cloud mask will be assigned an adjacency category dependent on distance to the nearest cloud defined quantitatively by the number of pixels (e.g., very close, close, far, very far).

The structure of the second QA data plane will consist of performance metrics output from various stages of the TES algorithm, detailed in Table 7:

1. The final value of $\varepsilon_{max}$ used in the NEM module after optimization (if necessary).
2. Number of iterations needed to remove reflected downwelling sky irradiance.
3. Atmospheric opacity test for humid scenes, using $L_\lambda^1/L'\lambda$ test.
4. MMD regime: MMD < 0.3 (near-graybody) or MMD > 0.3 (likely bare).
Table 6. Quality assurance (QA) data plane 1 description of the three data fields: data quality, cloud mask, and cloud adjacency.

<table>
<thead>
<tr>
<th>Data Field</th>
<th>Category</th>
<th>Bits</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data Quality</td>
<td>“Excellent”</td>
<td>11</td>
<td>Good quality, no further QA info necessary</td>
</tr>
<tr>
<td></td>
<td>“Good”</td>
<td>10</td>
<td>Good quality, but possible cloud adjacency effects; further QA examination necessary.</td>
</tr>
<tr>
<td></td>
<td>“Suspect”</td>
<td>01</td>
<td>Out of range data values</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Suspect input quality data flag</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Perimeter effects from thick/thin cloud</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Humid scene</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Fairly calibrated</td>
</tr>
<tr>
<td></td>
<td>“Bad”</td>
<td>00</td>
<td>Bad pixel labeled in L1A data</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>TES algorithm abort flag</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>TES algorithm divergence flag</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>TES convergence issues (only NEM values output)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Poorly calibrated, or ocean pixel</td>
</tr>
<tr>
<td>Cloud Mask</td>
<td>Thick cloud</td>
<td>11</td>
<td>Optically thick cloud detected with high reflectance</td>
</tr>
<tr>
<td></td>
<td>Thin cloud</td>
<td>10</td>
<td>Optically thin cloud detected with medium or low reflectance</td>
</tr>
<tr>
<td></td>
<td>Cirrus</td>
<td>01</td>
<td>Cirrus test indicated cirrus, haze, or jet contrails present</td>
</tr>
<tr>
<td></td>
<td>Clear</td>
<td>00</td>
<td>No clouds detected</td>
</tr>
<tr>
<td>Cloud Adjacency</td>
<td>Very near</td>
<td>11</td>
<td>Pixel is &lt;5 pixels from nearest cloud</td>
</tr>
<tr>
<td></td>
<td>Near</td>
<td>10</td>
<td>Pixel within 5–15 pixels of nearest cloud</td>
</tr>
<tr>
<td></td>
<td>Far</td>
<td>01</td>
<td>Pixel within 15–30 pixels of nearest cloud</td>
</tr>
<tr>
<td></td>
<td>Very far</td>
<td>00</td>
<td>Pixel &gt;30 pixels from nearest cloud</td>
</tr>
</tbody>
</table>

Table 7. Quality assurance (QA) data plane 2 description of output diagnostics from the TES algorithm.

<table>
<thead>
<tr>
<th>Data Field</th>
<th>Category</th>
<th>Bits</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon_{\text{max}}$</td>
<td>&gt;0.98</td>
<td>11</td>
<td>Graybodies (water, vegetation, snow)</td>
</tr>
<tr>
<td></td>
<td>0.96–0.98</td>
<td>10</td>
<td>Nominal value</td>
</tr>
<tr>
<td></td>
<td>0.94–0.96</td>
<td>01</td>
<td>Bare surfaces, silicate rocks</td>
</tr>
<tr>
<td></td>
<td>&lt;0.94</td>
<td>00</td>
<td>Error condition (atmospheric correction)</td>
</tr>
<tr>
<td>Iterations</td>
<td>≥7</td>
<td>11</td>
<td>Slow convergence</td>
</tr>
<tr>
<td></td>
<td>6</td>
<td>10</td>
<td>Nominal performance</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>01</td>
<td>Nominal performance</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>00</td>
<td>Fast convergence</td>
</tr>
<tr>
<td>$L_j/L'$</td>
<td>≥0.3</td>
<td>11</td>
<td>Warm, humid air; or cold land</td>
</tr>
<tr>
<td></td>
<td>0.2–0.3</td>
<td>10</td>
<td>Nominal value</td>
</tr>
<tr>
<td></td>
<td>0.1–0.2</td>
<td>01</td>
<td>Nominal value</td>
</tr>
<tr>
<td></td>
<td>≥0.1</td>
<td>00</td>
<td>Dry conditions, or high altitude scene</td>
</tr>
<tr>
<td>MMD</td>
<td>≥0.3</td>
<td>10</td>
<td>Low spectral contrast, graybody surface</td>
</tr>
<tr>
<td></td>
<td>&gt;0.3</td>
<td>00</td>
<td>High spectral contrast, most bare surfaces</td>
</tr>
</tbody>
</table>
9 Uncertainty Analysis

NASA has identified a major need to develop long-term, consistent products valid across multiple missions, with well-defined uncertainty statistics addressing specific Earth-science questions. These products are termed Earth System Data Records (ESDRs), and LST&E has been identified as an important ESDR. Currently a lack of understanding of LST&E uncertainties limits their usefulness in land surface and climate models. In this section we present results from an LST&E uncertainty simulator that has been developed to quantify and model uncertainties for a variety of TIR sensors and LST algorithms (Hulley et al. 2012). Using the simulator, uncertainties were estimated for the MOD21 LST&E product, including WVS. These uncertainties are parameterized according to view angle and estimated total column water vapor for application to real MODIS data.

9.1 The Temperature and Emissivity Uncertainty Simulator

A Temperature Emissivity Uncertainty Simulator (TEUSim) has been developed for simulating LST&E uncertainties from various sources of error for the TES and SW algorithms in a rigorous manner for any appropriate TIR sensor. These include random errors (noise), systematic errors (calibration), and spatio-temporally correlated errors (atmospheric). The MODTRAN 5.2 radiative transfer model is used for the simulations with a global set of radiosonde profiles and surface emissivity spectra representing a broad range of atmospheric conditions and a wide variety of surface types. This approach allows the retrieval algorithm to be easily evaluated under realistic but challenging combinations of surface/atmospheric conditions. The TEUSim is designed to separately quantify error contributions from the following potential sources:

- Noise
- Model
- Atmospheric correction
- Undetected cloud
- Calibration

The results presented in this study will focus on the first three of these error sources: noise, model, and atmosphere.
9.2 Atmospheric Profiles

The TEUSim uses a global set of atmospheric radiosoundings constructed from the University of Wyoming Atmospheric Science Department’s CLAR database (Galve et al. 2008). CLAR contains 382 globally distributed radiosoundings for both day and night in 65 layers from the surface to 100 km. The CLAR database includes a wide range of TCW estimates up to 7 cm and surface air temperature ranging from $-20^\circ$ C to $40^\circ$ C. Radiosondes acquired from 2003 to 2006 were distributed over three latitude ranges (40% from 0º–30º, 40% from 30º–60º, 20% above 60º) and screened for cloud and fog contamination using a procedure described by Francois et al. (2002).

9.3 Radiative Transfer Model

In TEUSim the latest version of MODTRAN (v5.2) was used for the radiative transfer calculations. MODTRAN 5.2 uses an improved molecular band model, termed the Spectrally Enhanced Resolution MODTRAN (SERTRAN), which has a much finer spectroscopy (0.1 cm$^{-1}$) than previous versions (1–2 cm$^{-1}$). This results in higher accuracy in modeling of band absorption features in the longwave TIR window regions, and comparisons with line-by-line models has shown good accuracy (Berk et al. 2005).

9.4 Surface End-Member Selection

A selection of emissivity spectra from the ASTER Spectral Library v2.0 (ASTlib) (Baldridge et al. 2009) were used to define the surface spectral emission term in MODTRAN. A total of 59 spectra were chosen based on certain criteria and grouped into four surface classifications: rocks (20), soils (26), sands (9), and graybodies (4). The doublets between 8–9.5 µm and 12.5–13 µm are the result of Si-O stretching, and the exact position of the feature at 11.2 µm is dependent on the size of the cation paired with the carbonate (CO$_3$) molecule. Spectra were chosen to represent the most realistic effective emissivities observed at the remote sensing scales of ASTER (90 m) and MODIS (1 km) using the following methodology.

For rocks, certain spectra were removed prior to processing based on two considerations. First, samples that rarely exist as kilometer-scale, sub-aerial end-member exposures on the Earth’s surface such as pyroxenite or serpentinite were eliminated. Second, and in parallel, spectrally similar samples were eliminated. Spectral similarity was defined by the location,
shape, and magnitude of spectral features between 7 and 13 µm. All eliminated samples are represented in the final selection through spectrally-similar end-member types. The final rock set included 20 spectra.

ASTlib includes 49 soil spectra classified according to their taxonomy, such as Alfisol (9), Aridisol (14), Entisol (10), Inceptisol (7) and Mollisol (9). Filtering in this case was based solely on spectral similarity between each taxonomy type. The final soils set included 26 soil spectra.

A set of nine emissivity spectra collected in separate field campaigns during 2008 over large homogeneous sand dune sites in the southwestern United States in support of validation for the NAALSED v2.0 (Hulley et al. 2009a) were used for sands. The sand samples consist of a wide variety of different minerals including quartz, magnetite, feldspars, gypsum, and basalt mixed in various amounts, and represent a broad range of emissivities in the TIR as detailed in Hulley et al. (2009a).

To represent graybody surfaces, spectra of distilled water, ice, snow, and conifer were chosen from ASTlib. Four spectra were sufficient to represent this class since graybody surfaces exhibit low contrast and high emissivities. It should be noted that certain types of man-made materials were not included, such as aluminum roofs that do not occur at the spatial resolution of these sensors, but should be included for higher-spatial-resolution data sets such as those provided by airborne instruments.

9.5 Radiative Transfer Simulations

In the TEUSim, each CLAR radiosonde profile for each set of end-member spectra was used as an input to MODTRAN 5.2. A seasonal rural aerosol was assumed with standard profiles for fixed gases within MODTRAN. For MODIS, five viewing angles were used, representing the Gaussian angles proposed by Wan and Dozier (1996): 0°, 11.6°, 26.1°, 40.3°, and 53.7°. In the WVS simulation model, the downward sky irradiance, \( I_\lambda(\theta) \), can be modeled using the path radiance, transmittance, and view angle. To simulate the downward sky irradiance in MODTRAN, the sensor target is placed a few meters above the surface, with surface emission set to zero, and view angle set at the prescribed angles above. In this configuration, the reflected downwelling sky irradiance is estimated for a given view angle. The total sky irradiance...
contribution for band $i$ is then calculated by summing the contribution of all view angles over the entire hemisphere:

$$L_i = \int_0^{\frac{2\pi}{2}} \int_0^\pi L_i^1(\theta) \cdot \sin\theta \cdot \cos\theta \cdot d\theta \cdot d\delta$$  

(24)

where $\theta$ is the view angle and $\delta$ is the azimuth angle. To minimize computational time, the downward sky irradiance is first modeled as a non-linear function of path radiance at nadir view using (1) (Tonooka 2001):

$$L_i^1(\gamma) = a_i + b_i \cdot L_i(0, \gamma) + c_i L_i^1(0, \gamma)^2$$  

(25)

where $a_i$, $b_i$, and $c_i$ are regression coefficients, and $L_i^1(0, \gamma)$ is computed by:

$$L_i^1(0, \gamma) = L_i^1(\theta, \gamma) \cdot \frac{1 - \tau_i(\theta, \gamma) \cos\theta}{1 - \tau_i(\theta, \gamma)}$$  

(26)

Equations (2) and (3) were used to estimate the downwelling sky irradiance in the TEUSim results using pre-calculated regression coefficients for MODIS bands 29, 31, and 32. The reflected sky irradiance term is generally smaller in magnitude than the surface-emitted radiance, but needs to be taken into account, particularly on humid days when the total atmospheric water vapor content is high. The simulated LST is based on the surface air temperature in the CLAR database as follows:

$$LST_{sim} = T_{air} + \delta T$$  

(27)

where $LST_{sim}$ and $T_{air}$ are the simulated LST and surface air temperature. Galve et al. (2008) found a mean $\delta T$ of +3 K and standard deviation of 9 K from a global study of surface-air temperature differences over land in the MODIS MOD08 and MOD11 products. We therefore defined $\delta T$ as a random distribution with a mean of 3 K and a standard deviation of 9 K for each profile input to MODTRAN.

The TES algorithm uses surface radiance as input, which can be derived from the atmospheric transmittance $\tau_\lambda(\theta)$, TOA radiance $L_\lambda(\theta)$, path radiance $L_\lambda^1(\theta)$, and downward sky irradiance $L_\lambda^1(\theta)$. To calculate the various sources of error in LST&E retrievals from TES, these variables were simulated for the following conditions:

1. Perfect atmosphere (i.e., exact inputs): $L_\lambda(\theta)$ and atmospheric parameters $\tau_\lambda(\theta)$, $L_\lambda^1(\theta)$, and $L_\lambda^1(\theta)$ calculated using a given profile, surface type and viewing angle;
2. \( L_a(\theta) \) and adjusted atmosphere (i.e., imperfect inputs): \( \tau_a' (\theta) \), \( L_a^0 (\theta) \), and \( L_a^1 (\theta) \) calculated using perturbed temperature and humidity profiles to simulate real input data;

3. Adjusted atmosphere as in (2) but with humidity scaled by a factor of 0.7 for deriving inputs to the WVS method; and

4. \( L_a(\theta) \) calculated using a graybody surface type (conifer was chosen with emissivity close to 0.99), as the scaling factors in the WVS method are initialized over graybody surfaces.

The above conditions were run for 'perfect' \( L_a(\theta) \) and also with adding random noise to the radiances based on the sensor’s noise equivalent delta temperature NE\( \Delta T \) (0.05 K for MODIS).

The WVS method is used for improving the accuracy of the atmospheric parameters output from MODTRAN using an EMC/WVD algorithm that models the surface brightness temperature (BT) given the at-sensor brightness temperature along with an estimate of the total water vapor (Tonooka 2001, 2005). The modeled surface BT is then used to determine a WVS correction factor, which for real data is first calculated over all graybody pixels on a given scene and then spatially interpolated using an inverse distance method over the remaining non-graybody pixels within the scene. Simulation Steps (3) and (4) are needed to simulate the input for the WVS method.

### 9.6 Error Propagation

The set of 382 CLAR radiosonde profiles were adjusted to simulate real data by applying estimated uncertainties from the MODIS MOD07 atmospheric product (Seemann et al. 2006; Seemann et al. 2003). Using a dataset of 80 clear sky cases over the SGP ARM site (Tobin et al. 2006), MOD07 air temperature RMS errors showed a linearly decreasing trend from 4 K at the surface to 2 K at 700 mb, and a constant 2 K above 700 mb (Seemann et al. 2006). These reported values were used to perturb the air temperature profiles at each associated level using a random number generator with a mean centered on the RMS error. The uncertainty of the water vapor retrievals were estimated to be between 10–20% (Seemann et al. 2006). Accordingly, the relative humidity profiles were adjusted by scaling factors ranging from 0.8 to 1.2 in MODTRAN using a uniformly distributed random number generator.

The total LST uncertainty for the TES algorithm based on model, atmospheric and measurement noise contributions can be written as:
\[ \delta LST_{TES} = [\delta LST_M + \delta LST_A + \delta LST_N]^{1/2} \]  
(28)

where \( \delta LST_M \) is the model error due to assumptions made in the TES calibration curve, \( \delta LST_A \) is the atmospheric error, and \( \delta LST_N \) is the error associated with measurement noise. These errors are assumed to be independent.

To calculate the separate contributions from each of these errors let us first denote the simulated atmospheric parameters as \( x = [t_A(\theta), L_\downarrow^1(\theta), L_\uparrow^1(\theta)] \) and simulated observed radiance parameter as \( y = L_A(\theta) \). Both \( x \) and \( y \) are required to estimate the surface radiance that is input to the TES algorithm. In reality, however, the input parameters \( x \) are not known explicitly, but are associated with some error, \( \delta x \), which we write as \( \hat{x} = x + \delta x \). Similarly, the observed radiances have an associated noise based on the NEAT of the specific sensor, which we will denote by \( \hat{y} \). To characterize the model error, we express the TES algorithm as a function based on perfect input parameters \( x \) and \( y \) such that \( LST_{TES} = f(x, y) \). The model error, \( \delta LST_M \), i.e., due to assumptions in the TES algorithm alone, can then be written as:

\[ \delta LST_M = E[ (f(x, y) - LST_{sim})^2 | x, y ]^{1/2} \]  
(29)

where \( LST_{sim} \) is the simulated LST used in the MODTRAN simulations, and \( E[\cdot | x, y ] \) denotes the mean-square error between the retrieved and simulated LST for inputs \( x \) and \( y \). The atmospheric error can be written as the difference between TES with perfect simulated TOA radiances, \( y \) and TES with noisy radiances, \( \hat{y} \):

\[ \delta LST_A = E \left[ \left( f(\hat{x}, y) - f(x, y) \right)^2 | x, y \right]^{1/2} \]  
(30)

And lastly the error due to measurement noise can be written as the difference between TES with perfect simulated TOA radiances, \( y \) and TES with noisy radiances, \( \hat{y} \):

\[ \delta LST_N = E \left[ \left( f(x, \hat{y}) - f(x, y) \right)^2 | x, y \right]^{1/2} \]  
(31)

Since the TES algorithm simultaneously retrieves the LST and spectral emissivity, the above equations also apply to the corresponding emissivity retrieval for each band.

The effects of sensor view angle on the accuracy of MODIS TES retrievals of LST are shown in Figure 18. LST uncertainties are plotted against TCW for four simulated Gaussian view angles of 0°, 26.1°, 40.3°, and 53.7°. It is clear that the uncertainties become larger with both TCW and view angle; however, this is due to TCW in both cases. A TCW amount of 4 cm at a 53.7° view angle has an effective TCW of 6.2 cm, due to an increase in atmospheric path length increases by a factor of \( \cos^{-1}(53.7°) \). The LSTs are underestimated at higher view angles.
by as much as 10 K, most likely due to unaccounted-for non-linear effects in the radiative transfer process due to longer atmospheric pathlengths. For real data, angular anisotropy of surface emissivity will also result in higher uncertainties at view angles above ~40° due to non-Lambertian behavior of certain types of soils and sands (Snyder et al. 1997), and also from highly structured (3-D) surfaces such as shrublands, savannas, woodlands and forests. This variability primarily arises from the changing proportions of scene endmembers visible at different view zenith angles (Yu et al. 2006).

Figure 18. MODIS LST uncertainties using the TES algorithm versus TCW for four viewing Gaussian angles of 0°, 26.1°, 40.3°, and 53.7°. The value \( n \) represents the number of data points used for a specific land surface type, in this case bare surfaces (rocks, soils, sands).

9.7 Parameterization of Uncertainties

A key requirement for generating LST&E ESDR from either multiple sensors or algorithms is accurate knowledge of uncertainties from the contributing products. Uncertainties for each input product must be rigorously estimated for a variety of different conditions on a pixel-by-pixel basis before they can be merged and incorporated into a time series of measurements of sufficient length, consistency, and continuity to adequately meet the science
requirements of an ESDR. Current LST&E datasets are available with quality control information, but do not include a full set of uncertainty statistics. For example, the standard ASTER and MODIS LST product QC data planes specify qualitative uncertainty information, and MODIS includes a rough estimate of LST&E error, but no uncertainty data-planes exist on a pixel-by-pixel basis dependent upon factors such as land cover type, view angle, and total column water vapor.

The next logical step is to apply the uncertainty statistics produced from the TEUSim to real data from MOD21 retrievals. To achieve this the total uncertainty, taken as the RMSE of the differences between simulated (truth) and retrieved LST&E including atmospheric error, was modeled according to view angle, total water vapor column amount, and land surface type using a least-squares method fit to a quadratic function. Three surface types were classified: graybody, transitional, and bare. The transitional surface represents a mixed cover type, and was calculated by varying the vegetation fraction cover percentage, $f_v$, by 25, 50, and 75% for the set of bare surface spectra (rocks, soils, sand) as follows:

$$\varepsilon_{trans} = \varepsilon_{gray} \cdot f_v + \varepsilon_{bare} \cdot (1 - f_v)$$  

where $\varepsilon_{trans}$ is the transition emissivity, $\varepsilon_{gray}$ is a graybody emissivity spectrum (e.g., conifer), and $\varepsilon_{bare}$ are the lab emissivities for bare surfaces.

For MODIS, the total uncertainty includes both a sensor view angle (SVA) and TCW dependence. The total uncertainty for MODIS LST can be expressed as:

$$\delta LST_{MODIS} = a_0 + a_1 TCW + a_2 SVA + a_3 TCW \cdot SVA + a_4 TCW^2 + a_5 SVA^2$$  

Similarly, the band-dependent emissivity uncertainties can be expressed as:

$$\delta \varepsilon_i_{MODIS} = a_{i,0} + a_{i,1} TCW + a_{i,2} SVA + a_{i,3} TCW \cdot SVA + a_{i,4} TCW^2 + a_{i,5} SVA^2$$

where $\delta LST$ is the LST uncertainty (K) calculated as the difference between the simulated and retrieved LST, $\delta \varepsilon_i$ is the band-dependent emissivity uncertainty for band $i$, calculated as the difference between the input lab emissivity and retrieved emissivity, and $a_i$ and $a_{i,j}$ are the LST and emissivity regression coefficients and depend on surface type (graybody, transition, bare).

A sensitivity study showed that the parameterizations given by equations 10–13 provided the best fit to the simulation results in terms of RMSE, with fits of ~0.1 K. Once the coefficients are established they can be applied on a pixel-by-pixel basis across any scene given estimates of TCW from either a retrieval (e.g., MODIS MOD07 or AIRS) or a numerical weather model (e.g., ECMWF, NCEP), and the SVA from the product metadata. A simple emissivity threshold using a
band with large spectral variation can be used to discriminate between graybody, transition, and bare types in any given scene for application of the relevant coefficients.

Figure 19(a) shows the retrieved LST using the TES algorithm with WVS correction and corresponding uncertainty in Figure 19(c), while Figure 19(b) shows the retrieved emissivity for band 29 and corresponding uncertainty in Figure 19(d). The highest LST uncertainties range from 2–3 K in the monsoonal region to over 5 K on the edges of cloudy regions, where uncertainties are highest as expected. Over most of the scene where TCW values are <2 cm, the LST uncertainties are generally <1.5 K. Similar to the LST results, the uncertainties in band 29 emissivity are highest over the monsoonal region, ranging from 0.03–0.05, and along the edges of clouds. Over drier regions of California and Nevada, there is a stronger uncertainty correlation with cover type, with lowest uncertainties over the denser forests of the Sierra Nevadas (~0.015) and slightly higher over bare and mixed regions (~0.02). For this scene, retrievals were restricted to view angles <40º, so uncertainty dependencies related to view angle are not evident; however, at angles >40º the uncertainties for both LST and emissivity increase noticeably due to reasons discussed earlier.
Figure 19. MODIS TES retrievals including WVS correction over the southwestern United States on 7 August 2004: (a) (top left) LST, (b) (top right) emissivity for band 29 (8.55 µm), (c) (bottom left) LST uncertainty, and (d) (bottom right) emissivity uncertainty for band 29 (8.55 µm). White areas over land indicate areas of cloud that have been masked out using the MOD35 cloud mask product.
10 Validation

Two methods have been established for validating MODIS LST data: a conventional T-based method and an R-based method (Wan and Li 2008). The T-based method requires ground measurements over thermally homogenous sites concurrent with the satellite overpass, while the R-based method relies on a radiative closure simulation in a clear atmospheric window region to estimate the LST from top of atmosphere (TOA) observed brightness temperatures, assuming the emissivity is known from ground measurements. The T-based method is the preferred method, but it requires accurate in-situ measurements that are only available from a small number of thermally homogeneous sites concurrently with the satellite overpass. The R-based method is not a true validation in the classical sense, but it does not require simultaneous in-situ measurements and is therefore easier to implement both day and night over a larger number of global sites; however, it is susceptible to errors in the atmospheric correction and emissivity uncertainties. The MOD11_L2 LST product has been validated with a combination of T-based and R-based methods over more than 19 types of thermally homogenous surfaces including lakes (Hook et al. 2007), dedicated field campaign sites over agricultural fields and forests (Coll et al. 2005), playas and grasslands (Wan et al. 2004; Wan 2008), and for a range of different seasons and years. LST errors are generally within ±1 K for all sites under stable atmospheric conditions except semi-arid and arid areas, which had errors of up to 5 K (Wan and Li 2008).

Initial testing and validation of the MOD21 emissivity product has shown good agreement with the North American ASTER Land Surface Database (NAALSED) v2.0 emissivity product (Hulley et al. 2009a) and in-situ data over nine pseudo-invariant sand dune sites in the southwestern United States to <0.02 (2%) (Hulley and Hook 2011). NAALSED was validated over arid/semi-arid regions using nine pseudo-invariant sand dune sites in the western/southwestern United States. The emissivity of samples collected at each of the nine sites was determined in the laboratory using a Nicolet 520 FT-IR spectrometer and convolved with the appropriate ASTER system response functions. Validation of emissivity data from space ideally requires a site that is homogeneous in emissivity at the scale of the imagery, allowing several image pixels to be validated over the target site. The nine sand dune validation sites chosen for the ASTER study and planned for use with the MOD21 product are: Great Sands National Park, Colorado; White Sands National Monument, New Mexico; Kelso Dunes, California; Algodones

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Dunes, California; Stovepipe Wells Dunes, California; Coral Pink Sand Dunes, Utah; Little Sahara Dunes, Utah; Killpecker Dunes, Wyoming; and Moses Lake Basalt Dunes, Washington.

A validation study at the Land Surface Analysis–Satellite Application Facility (LSA-SAF) Gobabeb validation site in Namibia showed that MOD21 LSEs matched closely with in-situ emissivity data (~1%), while emissivities based on land cover classification products (e.g., SEVIRI, MOD11) overestimated emissivities over the sand dunes by as much as 3.5% (Gottsche and Hulley 2012). R-based validation of the MOD21 product is currently underway over nine pseudo-invariant sites in southwestern United States, and the Lake Tahoe and Salton Sea cal/val sites.

For the MOD21 product we plan to use in-situ data from a variety of ground sites covering the majority of different land-cover types defined in the International Geosphere-Biosphere Programme (IGBP). The sites will consist of water, vegetation (forest, grassland, and crops), and barren areas (Table 8).

### Table 8. The core set of global validation sites according to IGBP class to be used for validation and calibration of the MODIS MOD21 land surface temperature and emissivity product.

<table>
<thead>
<tr>
<th>IGBP Class</th>
<th>Sites</th>
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| 0           | Water | Tahoe, Salton Sea, CA  
| 1,2         | Needle-leaf forest | Krasnoyarsk, Russia; Tharandt, Germany; Fairhope, Alaska  
| 3,4,5       | Broad-leaf/mixed forest | Chang Baisan, China; Hainich, Germany; Hilo, Hawaii  
| 6,7         | Open/closed shrublands | Desert Rock, NV; Stovepipe Wells, CA  
| 8,9,10      | Savannas/Grasslands | Boulder, CO; Fort Peck, MT  
| 12          | Croplands | Bondville, IL; Penn State, PA; Sioux Falls, SD; Goodwin Creek, MS  
| 16          | Barren | Algodones Dunes, CA; Great Sands, CO; White Sands, NM; Kelso Dunes, CA; Namib Desert, Namibia; Kalahari Desert, Botswana  

### 10.1 Water Sites

For water surfaces, we will use the Lake Tahoe, California/Nevada, automated validation site where measurements of skin temperature have been made every two minutes since 1999 and are used to validate the mid and thermal infrared data and products from ASTER and MODIS (Hook et al. 2007). Water targets are ideal for cal/val activities because they are thermally homogeneous and the emissivity is generally well known. A further advantage of Tahoe is that the lake is located at high altitude, which minimizes atmospheric correction errors, and is large
enough to validate sensors from pixel ranges of tens of meters to several kilometers. Figure 20 shows an example of differences between the standard MODIS (MOD11_L2) and ASTER (AST08) LST products and in-situ measurements at Lake Tahoe. The MODIS product is accurate to ±0.2 K, while the ASTER product has a bias of 1 K due to residual atmospheric correction effects. The typical range of temperatures at Tahoe is from 5°C to 25°C. More recently in 2008, an additional cal/val site at the Salton Sea was established. Salton Sea is a low-altitude site with significantly warmer temperatures than Lake Tahoe (up to 35°C), and together they provide a wide range of different conditions.

Figure 20. Difference between the MODIS (MOD11_L2) and ASTER (AST08) LST products and in-situ measurements at Lake Tahoe. The MODIS product is accurate to ±0.2 K, while the ASTER product has a bias of 1 K due to residual atmospheric correction effects.

10.2 Vegetated Sites

For vegetated surfaces (forest, grassland, savanna, and crops), we will use a combination of data from the Surface Radiation Budget Network (SURFRAD), FLUXNET, and NOAA-CRN sites. For SURFRAD, we will use a set of six sites established in 1993 for the continuous, long-term measurements of the surface radiation budget over the United States through the support of NOAA’s Office of Global Programs (http://www.srrb.noaa.gov/surfrad/). The six sites (Bondville, IL; Boulder, CO; Fort Peck, MT; Goodwin Creek, MS; Penn State, PA; and Sioux Falls, SD) are situated in large, flat agricultural areas consisting of crops and grasslands and have previously been used to assess the MODIS and ASTER LST&E products with some success (Augustine et al. 2000; Wang and Liang 2009). From FLUXNET and the Carbon Europe Integrated Project (http://www.carboeurope.org/), we will include an additional four sites to
cover the broadleaf and needleleaf forest biomes (e.g., Hainich and Tharandt, Germany; Chang Baisan, China; Krasnoyarsk, Russia), using data from the FLUXNET as well as data from the EOS Land Validation Core sites (http://landval.gsfc.nasa.gov/coresite_gen.html). Furthermore, the U.S. Climate Reference Network (USCRN) has been established to monitor present and future long-term climate data records (http://www.ncdc.noaa.gov/crn/). The network consists of 114 stations in the continental United States and is monitored by NOAA’s National Climatic Data Center (NCDC). Initially, we plan to use the Fairhope, Alaska, and Hilo, Hawaii, sites from this network.

10.3 Pseudo-invariant Sand Dune Sites

For LST validation over arid regions, we will use a set of nine pseudo-invariant, homogeneous sand dune sites in the southwestern United States (Hulley et al. 2009a) that were used for validating ASTER and MODIS products, and two sites over large sand dune seas in the Namib and Kalahari deserts in Southern Africa (Hulley et al. 2009b) for validating AIRS. The emissivity and mineralogy of samples collected at these sites have been well characterized and are described by Hulley et al. (2009a).

Pseudo-invariant ground sites such as playas, salt flats, and claypans have been increasingly recognized as optimal targets for the long-term validation and calibration of visible, shortwave, and thermal infrared data (Bannari et al. 2005; Cosnefroy et al. 1996; de Vries et al. 2007; Teillet et al. 1998). We have found that large sand dune fields are particularly useful for the validation of TIR emissivity data (Hulley and Hook 2009a). Sand dunes have consistent and homogeneous mineralogy and physical properties over long time periods. They do not collect water for long periods as playas and pans might, and drying of the surface does not lead to cracks and fissures, typical in any site with a large clay component, which could raise the emissivity due to cavity radiation effects (Mushkin and Gillespie 2005). Furthermore, the mineralogy and composition of sand samples collected in the field can be accurately determined in the laboratory using reflectance and x-ray diffraction (XRD) measurements. In general, the dune sites should be spatially uniform and any temporal variability due to changes in soil moisture and vegetation cover should be minimal. Ideally, the surface should always be dry, since any water on the surface can increase the emissivity by up to 0.16 (16%) in the 8.2–9.2-μm range depending on the type of soil (Mira et al. 2007).
10.3.1 Emissivity Validation

Seasonal changes in vegetation cover, aeolian processes such as wind erosion, deposition and transport, and daily variations in surface soil moisture from precipitation, dew, and snowmelt are the primary factors that could potentially affect the temporal stability and spatial uniformity of the dune sites. Field observations during the spring and early summer of 2008 revealed that the major portion of the dune sites was bare, with the exception of Kelso and Little Sahara, which contained sparse desert grasses and reeds on the outer perimeter of the dune field and in some interdunal areas. Nonetheless, this does not mean the other seven dune sites did not have vegetation in the past, since 2000. The presence of soil moisture would result in a significant increase in TIR emissivity at the dune sites, caused by the water film on the sand particles decreasing its reflectivity (Mira et al. 2007; Ogawa et al. 2006), particularly for MODIS band 29 in the quartz Reststrahlen band. However, given that the majority of dune validation sites are aeolian (high winds), at high altitude (low humidity), and in semi-arid regions (high skin temperatures), the lifetime of soil moisture in the first few micrometers of the surface skin layer as measured in the TIR is most likely small due to large sensible heat fluxes and, therefore, high evaporation rates, in addition to rapid infiltration. Consequently, we hypothesize that it would most likely take a very recent precipitation event to have any noticeable effect on remote-sensing observations of TIR emissivity over these types of areas.

Figure 21 shows emissivity spectra from sand dune samples collected at ten sand dune sites in the southwestern United States. The spectra cover a wide range of emissivities in the TIR region. These sites will be the core sites used to validate the emissivity and LST products from MODIS. Figure 22 shows ASTER false-color visible images of each dune site and comparisons between the emissivity spectra from NAALSED and lab measurements. The lab spectra in Figure 21 show the mean and standard deviation (spatial) in emissivity for all sand samples collected at the site, while the NAALSED spectra give the mean emissivity and combined spatial and temporal standard deviation for all observations acquired during the summer (July–September) time periods. The results show that TES-derived emissivity from ASTER data captures the spectral shape of all the dune sands very well. The quartz doublet centered around ASTER band 11 (8.6 µm) is clearly visible for Algodones Dunes samples, and the characteristic gypsum minimum in ASTER band 11 (8.6 µm) is evident from the White Sands samples.
Figure 21. Laboratory-measured emissivity spectra of sand samples collected at ten pseudo-invariant sand dune validation sites in the southwestern United States. The sites cover a wide range of emissivities in the TIR region.

Figure 22. ASTER false-color visible images (top) and emissivity spectra comparisons between ASTER TES and lab results for Algodones Dunes, California; White Sands, New Mexico; and Great Sands, Colorado (bottom). Squares with blue dots indicate the sampling areas. ASTER error bars show temporal and spatial variation, whereas lab spectra show spatial variation.
10.3.2 LST Validation

For LST validation over the sand dune sites, we will use a recently established R-based validation method (Coll et al. 2009b; Wan and Li 2008). The advantage of this method is that it does not require in-situ measurements, but instead relies on atmospheric profiles of temperature and water vapor over the site and an accurate estimation of the emissivity. The R-based method is based on a ‘radiative closure simulation’ with input surface emissivity spectra from either lab or field measurements, atmospheric profiles from an external source (e.g., model or radiosonde), and the retrieved LST product as input. A radiative transfer model is used to forward model these parameters to simulate at-sensor BTs in a clear window region of the atmosphere (11–12 µm). The input LST product is then adjusted in 2-K steps until two calculated at-sensor BTs bracket the observed BT value. An estimate of the ‘true’ temperature (\(LST_{R-based}\)) is then found by interpolation between the two calculated BTs, the observed BT, and the initial retrieved LST used in the simulation. The LST error, or uncertainty in the LST retrieval is simply found by taking the difference between the retrieved LST product and the estimate of \(LST_{R-based}\). This method has been successfully applied to MODIS LST products in previous studies (Coll et al. 2009a; Wan and Li 2008; Wan 2008). For MODIS data, band 31 (10.78–11.28 µm) is typically used for the simulation since it is the least sensitive to atmospheric absorption in the longwave region. The advantage of the R-based method is that it can be applied to a large number of global sites where the emissivity is known (e.g., from field measurements) and during night- and daytime observations to define the diurnal temperature range.

The archive of all North American MODIS data, as defined by the bounding box 22° to 71° N and 55° to 169° W, was used in this process for each pseudo-invariant site. Each scene was tested to see if it contained the location of interest. Scenes that did not contain the point of interest were eliminated, as were scenes in which the point was located either along scene margins (the first or last row or column of pixels) or whose viewing angle exceeded 40°. Finally, scenes in which the pixel of interest was cloudy, or had greater than three neighboring pixels that were cloudy, were eliminated. Cloudiness was defined as less than a 66% certainty that a pixel was clear in the M*D35 data. Any scene remaining at this point was used for determination of LST. LST data were derived either directly from the M*D11_L2 product or calculated locally using the algorithm for the M*D21 product. In the latter case, these calculations were performed using the M*D021KM, M*D03, M*D07_L2, M*D10A2, M*D13A2, and M*D35_L2 data as
input, as described in Hulley and Hook (2011). In addition to LST, the uncertainty of the value was read from the M*D11_L2 data or calculated for the M*D21 data using the values given in Hulley et al. (2012). Following LST retrieval, atmospheric profiles over the pseudo-invariant site were obtained from either the measurements of the AIRS instrument or from the NCEP GDAS model. Both methods were used for MODIS-Aqua data, while only NCEP GDAS data were used for MODIS-Terra data. Data retrieved for atmospheric profiles were the geopotential heights, temperatures, relative humidities, ozone, and pressure for each geopotential height level of the profile, and the PWV for the column as a whole. Together with the original land surface temperature from M*D11, these values were then used as input to MODTRAN 5.2 to calculate the Top Of Atmosphere Radiance.

Wan and Li (2008) proposed a quality check to assess the suitability of the atmospheric profiles by looking at differences between observed and calculated BTs in two nearby window regions with different absorption features. For example, the quality check for MODIS bands 31 and 32 at 11 and 12 µm is:

$$\delta(T_{11} - T_{12}) = (T_{11}^{obs} - T_{12}^{obs}) - (T_{11}^{calc} - T_{12}^{calc})$$  \hspace{1cm} (35)$$

where: $T_{11}^{obs}$ and $T_{12}^{obs}$ are the observed brightness temperatures at 11 and 12 µm respectively, and $T_{11}^{calc}$ and $T_{12}^{calc}$ are the calculated brightness temperatures from the R-based simulation at 11 and 12 µm respectively. If $\delta(T_{11} - T_{12})$ is close to zero, then the assumption is that the atmospheric temperature and water vapor profiles are accurately representing the true atmospheric conditions at the time of the observation, granted the emissivity is already well known. Because water vapor absorption is higher in the 12-µm region, negative residual values of $\delta(T_{11} - T_{12})$ imply the R-based profiles are overestimating the atmospheric effect, while positives values imply an underestimation of atmospheric effects. A simple threshold can be applied to filter out any unsuitable candidate profiles for validation. Although Wan and Li (2008) proposed a threshold of ±0.3 K for MODIS data, we performed a sensitivity analysis and found that a threshold of ±0.5 K resulted in a good balance between the numbers of profiles accepted and accuracy of the final R-based LST.

Figure 23 shows scatterplots of MODIS retrieved LST (MOD11 in red and MOD21 in blue) versus the R-based LST for six pseudo-invariant sites using all MODIS data from 2005. The results show that the MOD11 SW LST algorithm underestimates the LST by 3–4 K at all sites except White Sands, while the MOD21 algorithm has biases of less than 0.5 K. The
statistics of the results in including bias and RMSE are shown in Table 9. MOD11 RMSEs are as high as ~5 K at Great Sands, while MOD21 RMSEs are mostly at the 1.6 K level. The reason for the MOD11 cold bias is that the emissivity for barren surfaces is assigned one value that is fixed (~0.96 at 11 µm). This causes large LST errors over bare sites where the mineralogy results in emissivities lower than that fixed value. The MOD21 algorithm, on the other hand, physically retrieves the spectral emissivity in MODIS bands 29, 31, and 32, along with the LST, and this results in more accurate LST results, particularly over bare regions where emissivity variations can be large, both spatially and spectrally. Table 10 shows comparisons between the laboratory-derived emissivities at each site, along with the mean MOD11 and MOD21 emissivities for band 31 (11 µm).

Table 9. R-based LST validation statistics from six pseudo-invariant sand dune sites using all MOD11 and MOD21 LST retrievals during 2005.

<table>
<thead>
<tr>
<th>Site</th>
<th>MOD11 Bias</th>
<th>MOD11 RMSE</th>
<th>MOD21 Bias</th>
<th>MOD21 RMSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Algodones (197 scenes)</td>
<td>-2.6587</td>
<td>2.7871</td>
<td>0.5018</td>
<td>1.6004</td>
</tr>
<tr>
<td>Great Sands (123 Scenes)</td>
<td>-4.708</td>
<td>4.7417</td>
<td>0.4333</td>
<td>1.5237</td>
</tr>
<tr>
<td>Kelso (210 scenes)</td>
<td>-4.5234</td>
<td>4.5892</td>
<td>-0.6574</td>
<td>1.6494</td>
</tr>
<tr>
<td>Killpecker (147 scenes)</td>
<td>-4.072</td>
<td>4.1629</td>
<td>-0.0866</td>
<td>1.6845</td>
</tr>
<tr>
<td>Little Sahara (159 scenes)</td>
<td>-3.4255</td>
<td>3.4680</td>
<td>0.5274</td>
<td>1.6335</td>
</tr>
<tr>
<td>White Sands (102 scenes)</td>
<td>-0.0583</td>
<td>0.5455</td>
<td>0.4843</td>
<td>1.3441</td>
</tr>
</tbody>
</table>

Table 10. Emissivity comparisons between lab, MOD11, and MOD21 at six pseudo-invariant sand sites.

<table>
<thead>
<tr>
<th>Site</th>
<th>Lab</th>
<th>MOD11</th>
<th>MOD21</th>
</tr>
</thead>
<tbody>
<tr>
<td>Algodones (197 scenes)</td>
<td>0.963</td>
<td>0.966</td>
<td>0.954</td>
</tr>
<tr>
<td>Great Sands (123 Scenes)</td>
<td>0.944</td>
<td>0.970</td>
<td>0.949</td>
</tr>
<tr>
<td>Kelso (210 scenes)</td>
<td>0.942</td>
<td>0.966</td>
<td>0.949</td>
</tr>
<tr>
<td>Killpecker (147 scenes)</td>
<td>0.942</td>
<td>0.968</td>
<td>0.946</td>
</tr>
<tr>
<td>Little Sahara (159 scenes)</td>
<td>0.953</td>
<td>0.972</td>
<td>0.952</td>
</tr>
<tr>
<td>White Sands (102 scenes)</td>
<td>0.976</td>
<td>0.974</td>
<td>0.967</td>
</tr>
</tbody>
</table>
Figure 23. An example of the R-based validation method applied to the MODIS Aqua MOD11 and MOD21 LST products over six pseudo-invariant sand dune sites using all data during 2005. AIRS profiles and lab-measured emissivities from samples collected at the sites were used for the R-based calculations.
11 References


Ogawa, K., Schmugge, T., Jacob, F., & French, A. (2003). Estimation of land surface window (8-12 mu m) emissivity from multispectral thermal infrared remote sensing - A case study in a part of Sahara Desert. *Geophysical Research Letters, 30*, -


