Discussion on LDPC Codes and Uplink Coding

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NASA Data Standards Working Group
CCSDS Fall Meeting - Heppenheim - Oct. 2-5, 2007
Space Link Coding & Synchronization

Progress on LDPC Codes at JPL

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OVERVIEW

Working Group Objectives
• The objective is to develop and recommend new error correcting codes for near-Earth, Lunar, and deep space applications
  • The main features for which improvements are sought are: Power efficiency, bandwidth efficiency, complexity (encoding/decoding speed), latency

CCSDS Meeting goals (WG - overall)
• Discuss the three Orange Books (NASA, ESA, CNES) relative merits
• Discuss progress in the three Agencies
• Make a concerted effort to decide what should be standardized
• Plan future activities

NASA goals
• Request the start of a “white book” recommendation on LDPC codes based on the NASA Orange Book (Leading to a Red Book)
• Discuss NASA’s plans to use LDPC codes in deep space and Lunar missions, and compare with plans by ESA and CNES. Leverage on the alignment with Cx Program, which recommended an LDPC code for all uplink, downlink, and proximity links, and CMLP study, which recommends LDPC, Turbo, CC, and RS codes
• Discuss NASA’s progress in LDPC codes, testing, and infusion activities

02-03 November, 2006
• WG History
  (Jan. 07)
  • Discussed revision of NASA Orange Book to include variant of LDPC codes (AR4JA). This revision is now approved and published
  • Discussed CNES and ESA Orange Books
  • Discussed advantages and disadvantages of each proposal
  • Discussed progress of each Agency in validating each coding scheme
  • Presented new results on long erasure codes

• The overall (long-term) history is that of a rather dysfunctional WG, which cannot reach a decision since several years (three candidate recommendations on the table: NASA, ESA, CNES)
• Measured (by SW simulation) the performance loss of the AR4JA (2048,1024) LDPC code when the receiver can provide only hard decoded symbols (e.g., the Integrated Receiver)
• Performed a detailed study of the LDPC decoder sensitivity to symbol scaling errors
• Implemented advanced frame synchronizing algorithms and modified them for low-complexity implementation. Measured their performance, compared to that of some codes in use
• Performed LDPC Decoder Tests at ESTL (JSC) with the Integrated Receiver
• Provided/licensed the JPL-designed FPGA LDPC decoder to industry, NASA centers, and other agencies
• Infusion activities:
  • Low-Density Parity-Check (LDPC) code was chosen for all coded links of Constellation
  • The LDPC code was tested for Space Network (SN) compatibility and performance
  • Mars Science Lab (MSL) to Mars Reconnaissance Orbiter (MRO) link will use same code
  • TDRS K-Band Upgrade Project (TKUP-A)
  • Several new users of JPL LDPe technology
• Participated in the Space Planning Working Group (SPWG, formerly SCAWG) Coding, Modulation, and Link Protocol (CMLP) study
• Contributed to the study on the comparison of the LDPC C2 code and a TPC (Turbo Product Code) — C2 code has better error floor
• Determined a rule of thumb for the truncation length necessary in decoding punctured convolutional codes (This replaces an incorrect rule that has been in use for many years)
• Long erasure codes were presented at the Jan. 07 mtg.; New results on DSN outage statistics from MRO and WVR studies support the usefulness of these codes in conjunction with ARQ schemes; Developed new rateless codes
Simulated hard-decision decoding of the AR4JA (2048,1024) LDPC code on the Additive White Gaussian Channel to measure performance. Loss compared to soft-decision decoding is 1.8 dB.

Motivation: In the Space Network missions provide Reed-Solomon (RS) encoding/decoding and White Sands Complex (WSC) only provides Convolutional encoding/decoding or hard-quantized received symbols.

Studied through analysis and verified through simulations two methods that can circumvent the codeword miscorrection problem for the AR4JA LDPC code due to receiver symbol slips:

1. Use the recommended CCSDS randomizer PN sequence. At the receiver, the PN sequence XORed with a shifted version of itself leads to gibberish that results in an undecodable codeword. No miscorrection were observed in 10,000 decoding trials.

2. A simple reversal of the codeword parity during transmission also avoids this problem. A symbol slip would cause the information bits to shift in one direction and the parity in the other, at the input of the decoder (after undoing the parity reversals). This alters the quasi-cyclic nature of the code and prevents codeword miscorrections. No miscorrection were observed in 10,000 decoding trials.

Motivation: The AR4JA LDPC code family is quasi-cyclic. That is, a quasi-cyclic shift of the code bits leads to another codeword. Symbol slips are known to occur in the Integrated Receiver (IR) at WSC in the desired SNR operating region. A slip in receiver symbols causes a quasi-cyclic shift in the code bits of a codeword. Thus, a symbol slip could lead to a codeword miscorrection.
**Background**

Problem:
Transmit: \( x = \{+1,-1\} \)
Receive: \( y = Ax + N(0,\sigma^2) \)
Compute LLRs for decoder: \( \lambda = A/\sigma^2 y \)
However: This requires estimates of \( A \) and \( \sigma \)

How does decoder performance degrade if it is given \( \lambda' = \rho \lambda \) instead?

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**Diagram:**

- **Frame Error Rate vs. Eb/No:**
  - Eb/No=2dB
  - \( \rho = 0 \)

- **Log10(frame error rate) vs. Eb/No:**
  - JPL Proprietary Material
Frame Synchronizer Performance Study

Performance of several frame synchronizer algorithms compared to that of some good codes

Conclusions:

- Hard and soft correlators are not good synchronization strategies. Massey published the optimal algorithm in 1972!

- Matching one 64-symbol sync mark isn't good enough for modern rate-1/2 codes, even with Massey's optimal algorithm

- Matching two sync marks (128 symbols) is sufficient

- A low-complexity version implemented in FPGA hardware gives the performance shown by the black curve.
• Performed LDPC codes tests at ESTL
  • Two main sources of false measured errors:
    • False frame synchronization unlock (burst of 80 bit errors)
    • Bit slip events reduces the BER slope
  • Predicted LDPC implementation loss at 1 Mbps is 0.7 dB
  • Loss of 0.7 dB = 0.4 dB (uncoded) + 0.3 dB (LLR)
• Has endorsement from Chatwin Landsdowne @ JSC
Industry, NASA centers, and other agencies are using the JPL-designed FPGA LDPC decoders. Here are some key points:

- **Companies**
  - Efficient Channel Coding (ECC)
  - RTLogic
  - Avtec
  - L3 Communications
  - Lockheed Martin
  - Cincinnati Electronics

- **NASA centers**
  - Johnson Space Center
  - Goddard Space Flight Center
  - Several JPL projects

- **Spacecraft**
  - MSL - MRO Proximity Link (implemented; tests ongoing)
  - Constellation (baseline plan)
  - Cibola Flight Experiment (initial discussions underway)
  - AIRSAR (aircraft based)

- **LDPC encoders and decoders on FPGA**
  - 720 Msps block-circulant LDPC encoder
  - 102 Msps decoder for (4096,1/2) AR4JA LDPC code
  - 86 Msps decoder for GSFC's r=7/8 C₂ LDPC code
Infusion Accomplishments

• Low-Density Parity-Check (LDPC) code was chosen for all coded links of Constellation
  • The JPL AR4JA (k = 1024, rate = ½) LDPC code will be used for both uplink and downlink
  • Saves 1.6 dB of power and reduces latency 40 to 90%, compared to legacy code
  • Recommendation based on a comprehensive FEC study (JPL, GSFC, JSC, and led by ITT)
  • Lockheed-Martin has licensed JPL LDPC encoder/decoder technology for CEV spacecraft
  • Choice is contingent on successful TRL advancement from 5 to 9
• The LDPC code was tested for Space Network (SN) compatibility and performance
  • LDPC tests conducted 2/20/2007 to 3/2/2007, at JSC Electronic Systems Test Laboratory (ESTL)
  • Decoder operated error-free in all SNR regions the receiver could lock
  • The successful demonstration represents TRL advancement from 4, to 5 (encoder) and 6 (decoder)
• Mars Science Lab (MSL) to Mars Reconnaissance Orbiter (MRO) link will use same code
  • Feasibility study for use of AR4JA (1024,½) LDPC code is complete
  • Complete designs for MSL encoder and MRO decoder have been completed
• TDRS K-Band Upgrade Project (TKUP-A)
  • Three vendors licensed the JPL LDPC technology during proposal phase
  • Two vendors have been selected to demonstrate LDPC codes: IN-SNEC, and RT Logic
  • Demonstration of AR4JA(1024,1/2) code will occur in Jan. 2008
• Users of JPL LDPC technology
  • Cincinnati Electronics, L-3 Space Communications, MIT/LL, Lockheed Martin, RTLogic
• AOFDM-LDPC system for the Air Force
CMLP Study

- Space Planning Working Group (SPWG, formerly SCAWG) Coding, Modulation, and Link Protocol (CMLP) study
  - What the study did:
    - Created extensive catalog of all reasonable modulations and codes
    - Enumerated all communications links in NASA's strategic planning documents
    - Developed comprehensive Figures of Merit by which to compare codes and modulations
    - Created recommendations of codes and modulations for classes of links
  - CMLP recommendations
    - Modulations: PCM/PSK/PM, BPSK, QPSK, OQPSK, precoded GMSK, 8-PSK, 16-QAM
    - Codes: CC(7,1/2), RS(255,223), AR4JA LDPC, C2 LDPC
    - All codes and modulations are discussed in CCSDS documents (not all are Blue Books)
  - Final report will come out in September
# CMLP Study - Recommended Codes

<table>
<thead>
<tr>
<th>Network Parameter</th>
<th>Recommended Technique</th>
<th>Typical Application</th>
</tr>
</thead>
</table>
| CCSDS turbo codes (r = 1/6, 1/4, 1/3) | **Coding** | • For low data rate, severely power-constrained links or links which have little spectral containment requirements  
• Typical application may be a small Mars surface platform with DTE/DFE link |
| CCSDS AR4JA LDPC codes (r = 1/2, 2/3, 4/5) |  | • Code family with general applicability to most links  
• Envisioned future replacement to traditional convolutional and concatenated codes  
• Offers superior coding gain over traditional codes |
| CCSDS C2 LDPC code (r = 7/8) |  | • For links which are power-constrained and spectrum-constrained  
• Typical application may be high data rate CAT A missions |
| Convolutional codes |  | • Mid-Transition: General applicability to most links except spectrum-constrained links  
• Post-Transition: For severely latency-constrained links only  
• Offers superior heritage and reliability  
• Typical application may be a LEO mission’s TT&C link and the high rate science link |
| Legacy Reed-Solomon, BCH |  | • R-S and BCH have general applicability to most links, especially as outer codes  
• Need for an outer code is diminished with planned migration to LDPC codes as noted above  
• Typical application may be a mission which launches prior to the demonstrated operational readiness of LDPC-capable NASA infrastructure |
| Uncoded |  | • For links which are not power-constrained  
• Although a mission may not be power constrained, consideration should be given to use of a code because of the benefits to power flux density and resiliency to distortions  
• Typical application may be an X-band LEO mission downlinking at a very high data rate to the NASA GN |
Ka-band Outages

- Deep-Space Ka-band link outages were simulated using Water Vapor Radiometer (WVR) data and models for DSN antennas
  - Average outage duration of between 30 minutes and an hour depending on the complex
  - Outage duration standard deviation are larger than the average outage duration
  - Some outages could last several hours
  - Ka-band fades too deep (x4 in dB greater than X-band) to use a simple margin policy. Retransmissions and/or long erasure codes are necessary to assure data completeness

Day 2006-200, DSS-26 Ka-band Link Performance Simulation for MRO

![Graph showing G/T (dB-Ka-1) over time]

- Required G/T, 90%
- Actual G/T
- Status
Some implementers have been uncertain how to apply a de-randomizer to received soft symbols.

Solution
- Randomization of binary symbols is performed by inverting some symbols.
- De-randomization of soft symbols is performed by negating some noisy symbols.
- Implementation details were documented and distributed via memo to Constellation team members in March.

Initialize to an “all ones” state for each Codeblock or Transfer Frame during ASM period.
Convolutional Decoding – Revised Truncation Length Rule

Discovered surprising discrepancy with convolutional decoding

• Commonly used rule of thumb:
  
  "Set truncation depth in Viterbi algorithm equal to 5m, where m is the constraint length of the convolutional code."

  E.g., the CCSDS green book uses depth 60 for (7,1/2), (7,2/3), (7,3/4), (7,5/6), and (7,7/8) codes for its performance data

• New (corrected) rule of thumb:
  
  "Set truncation depth in Viterbi algorithm equal to 2 to 3 times m/(1-R), where m=constraint length and R = code rate."

  E.g., depth 60 is inadequate for (7,7/8) code, and results in about a 0.5 dB loss compared to a proper truncation depth of 120:
## Comparison of Three Proposed Coding System

<table>
<thead>
<tr>
<th></th>
<th>Power Efficiency</th>
<th>(code rate)</th>
<th>Latency (code dimension k)</th>
<th>Complexity /Speed</th>
<th>Patents</th>
<th>CCSDS 'Compatible'</th>
<th>Technology readiness/infusion</th>
<th>Baseline for Constellation Program</th>
</tr>
</thead>
<tbody>
<tr>
<td>LDPC (NASA Orange Book)</td>
<td>$&lt; 10^{-7}$ BER</td>
<td>0.5-1.0 dB imperfectness</td>
<td>1/2,...,7/8</td>
<td>1K,...,16K</td>
<td>Ex: 360 Mbps (4K:1/2) on Xilinx Virtex2 @180Mhz</td>
<td>Ex: 80 Mbps @ 14 iterations. (1K:1/12) on XCV8000 @80Mhz</td>
<td>Will be royalty free if granted</td>
<td>Orange Book easily converted to Blue Book</td>
</tr>
<tr>
<td>DVB (CNES)</td>
<td>$&lt; 10^{-7}$ BER</td>
<td>?</td>
<td>1/4,...,9/10</td>
<td>16K, 64K</td>
<td>Fast IRA encoder</td>
<td>Large protograph + BCH decoder</td>
<td>?</td>
<td>Codes coupled with modulations and protocol</td>
</tr>
<tr>
<td>SCCC (ESA)</td>
<td>$&lt; 10^{-7}$ BER</td>
<td>?</td>
<td>0.36-0.90</td>
<td>5876-43740</td>
<td>Fast convolutional encoder</td>
<td>JPL patent plus others</td>
<td>Codes coupled with modulations</td>
<td></td>
</tr>
</tbody>
</table>

**Note:** BER = Bit Error Rate