

## VECTOR FINITE ELEMENT MODELING OF PURELY PHYSICAL MODES IN A FERRITE-FILLED CYLINDRICAL CAVITY

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Mocks of a fictitious ferrite-filled perfectly conducting cavity are obtained by modeling the fully 3-D electric fields using Whitney edge elements. The cavity is modeled by a tetrahedral mesh with unknowns linked with each lattice edge representing the component of the field tangential to that edge. The perfectly conducting walls are represented by setting the included tangential electric field values explicitly to zero. A Hermitian matrix  $[S]$  is computed by combining the curl of the testing function, curl of electric field, and the Hermitian magnetization tensor. We solve the generalized eigenvalue problem  $[S]d = k^2 [T]d$  (I, for eigenvalues  $k^2$  and electric field coefficient eigenvectors  $d$ , where  $[T]$  is the positive definite matrix formed by combining the testing function and the electric field directly.

The 20 lowest order physical eigenvalues ( $5 < k^2 < 25$ ) differ from an analytic/transcendental solution by  $< 3\%$  for the case where the cavity is an axially magnetized cylinder of unit radius, two units altitude, with unit relative permeability on the diagonal,  $\pm 0.1$  off diagonal, for finite elements with typical edge length 0.3 units (1700 unknowns). In addition, a finite number of  $k^2 = 0$  modes are computed, corresponding to the infinite-dimensional space of zero-frequency zero-curl divergence-free fields admitted by the curl-curl operator. It is notable that these modes compute 10 values of  $k^2 < 10^{-5}$ , demonstrating that Whitney elements may be used to represent fields in ferrite media with near-perfect separation of physical and spurious modes. This indicates the ability to model fields in ferrite device and scattering problems with no corruption from vector parasites.