

# Surface Clutter Due to Antenna Sidelobes for Spaceborne Atmospheric Radar

S. L. Durden<sup>1</sup>, F. K. Li<sup>1</sup>, E. Im<sup>1</sup>, and R. Girard<sup>2</sup>

<sup>1</sup>Jet Propulsion Laboratory

<sup>2</sup>Canadian Space Agency

## 1. Introduction

- Spaceborne atmospheric radars must detect relatively weak targets (clouds and rain) in the presence of both thermal noise and clutter.
- Clutter is primarily from the surface through antenna sidelobes.
- Because of the brightness of the surface relative to atmospheric targets, surface clutter must be accurately calculated for proper system design.
- Previous work in this area has dealt with clutter due to the same pulse as that illuminating the atmosphere.
- The method presented here includes effects of all contributing transmit pulses, Doppler shifting, finite receiver bandwidth, and curved earth's surface.

## 2. Atmospheric Signal

- The atmospheric backscatter power is calculated by the Probert-Jones equation:

$$P_a(r) = \frac{P_t \lambda^2 G^2 \theta_1^2 \Delta \eta}{512 \pi^2 \ln 2 r_a^2}$$

- $P_t$  is the transmitter power,  $\lambda$  is the wavelength,  $G$  is the antenna gain,  $\theta_1$  is the antenna half-power beamwidth,  $\Delta$  is range resolution,  $r_a$  is the range to the atmospheric target, and  $\eta$  is the reflectivity.
- In this equation and our subsequent derivations, we assume that the pulse shape is nearly constant over the resolution  $\Delta$  and zero outside.
- This equation also assumes a Gaussian-shaped antenna pattern.

### 3. Clutter Signal

- In addition to the signal from the atmosphere, the radar will simultaneously receive echoes from all targets which differ in range by  $nc/2PRF$ .
- Here,  $n$  is an integer,  $c$  is the speed of light, and  $PRF$  is the pulse repetition frequency.
- $n$  corresponds to the pulse number relative to the pulse being received from the atmospheric target, with positive  $n$  denoting previous pulses and negative  $n$  denoting subsequent pulses.
- The surface return  $P_s$  for a particular  $n$  is given by the following expression:

$$P_s(r) = \frac{P_t \lambda^2 G^2}{64\pi^3} \int_S \frac{g^2 \sigma^0}{r_s^4} dS$$

- $S$  denotes the surface illuminated by the pulse,  $\sigma^0$  is the normalized radar cross section of the surface, and  $g$  is the antenna pattern.
- The range to the surface  $r_s$  is equal to  $r_a + nc/2PRF$ .
- For a rectangular pulse, the surface clutter through sidelobes for a given  $n$  is due to an annulus on the earth's surface.

#### 4. Signal-to-Clutter Ratio

- The previous expression for  $P_s$  can be simplified by writing  $dS$  as  $\sin \gamma d\gamma d\phi$ , where  $\gamma$  is the angle subtended by the earth's surface from nadir to the annulus.
- Then  $g^2$ ,  $\sigma^o$ , and  $r_s$  are assumed constant over the width of the annulus and brought outside the  $\gamma$  integral.
- The signal-to-clutter ratio (SCR) can be found as the ratio of the atmospheric power to the sum of the clutter power over all pulses (or annuli):

$$SCR = \frac{\pi \theta_1^2 \eta \Delta (R_e + h)}{4 \ln 2 r_a^2 R_e \Sigma}$$

$$\Sigma \equiv \sum_n \frac{\sigma^o (r_2^2 - r_1^2)}{r_s^4} \int_0^{2\pi} g^2(\theta_n, \phi) w(\phi) d\phi$$

- $r_1 \equiv r_s - \Delta/2$ , the distance to the inner annulus edge, and  $r_2 \equiv r_s + \Delta/2$ , the distance to the annulus outer edge.
- $R_e$  is the earth's radius, and  $h$  is the spacecraft altitude.
- $\theta_n$  is the angle between nadir and the  $n$ th annulus.

## 5. Computational Details

- Since the receiver has a finite bandwidth, the return from a direction  $\phi$  must also be weighted by  $w(\phi)$  the receiver output for a Doppler shifted input.
- An antenna pattern  $g$  is also needed; we use a Gaussian shaped mainbeam with sidelobes which fall off at a user-specified rate.
- For the surface backscatter  $\sigma^o$ , we use a function which decreases linearly in the log-domain.
- For a spherical earth, the maximum  $n$  corresponds to a propagation vector that is tangent to the earth's surface.
- The minimum  $n$  is 0 for a nadir looking system but can be negative when the antenna is scanned off-nadir.
- Rather than computing SCR, it is more convenient to solve for the reflectivity giving an SCR of unity:

$$\eta_m = \frac{r_a^2 4 \ln 2 R_e \Sigma}{\pi \theta_1^2 \Delta (R_e + h)}$$

- The minimum detectable reflectivity factor,  $Z_m \equiv \lambda^4 \eta_m 10^{18} / \pi^5 |K|^2$ , is then found.
- $K$  is the dielectric constant factor for the atmospheric target.

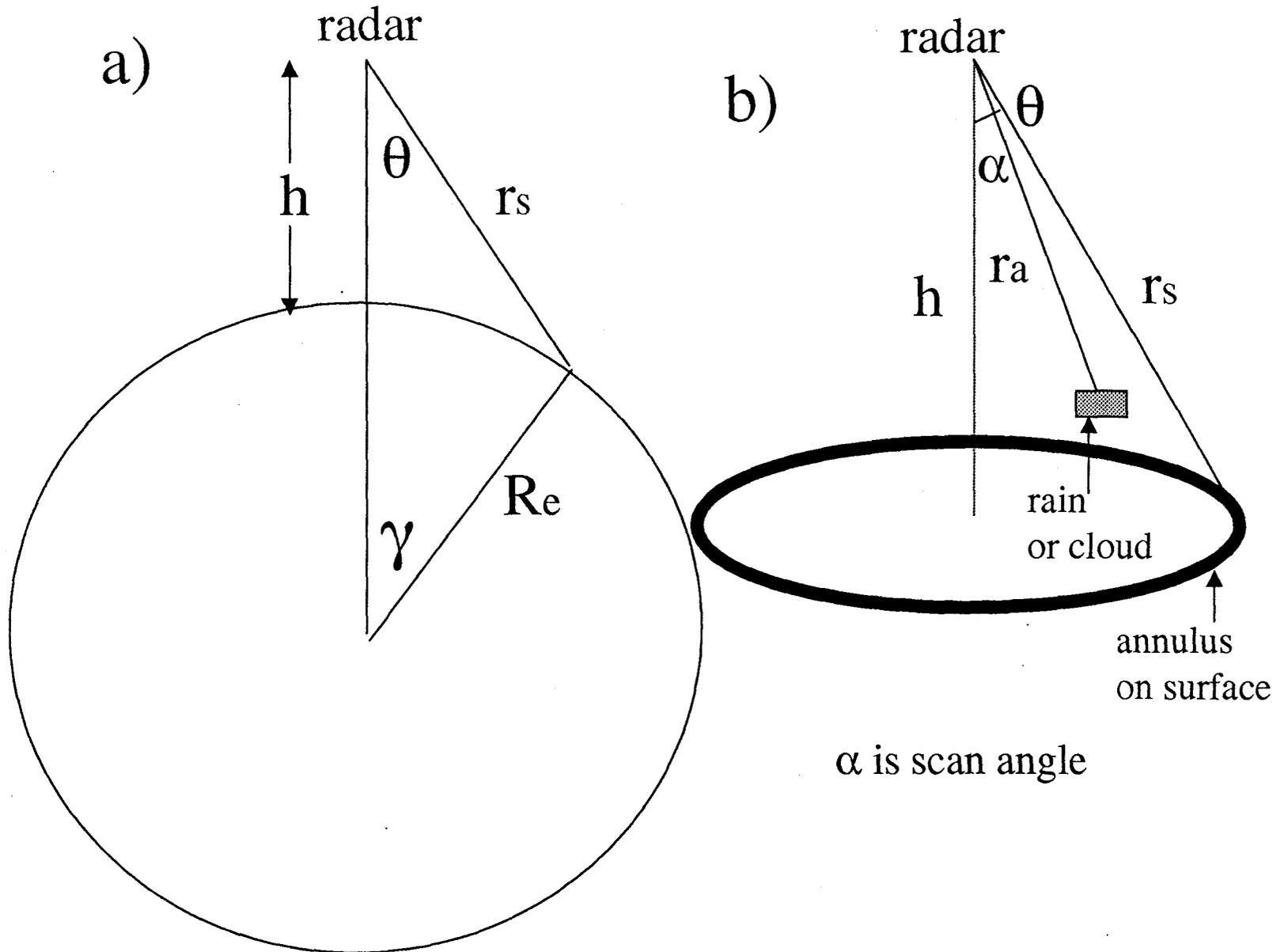
## 6. Application to TRMM

- The TRMM Precipitation Radar (PR) has been in operation since late 1997.
- The figure shows clutter data acquired by the TRMM PR over the Indian ocean at  $17^\circ$  incidence angle (clear conditions).
- Also shown in the figure are calculations of  $Z_m$  due to clutter using the method developed here.
- Agreement between the calculated and observed  $Z_m$  is generally good; differences are most likely due to differences between the ocean  $\sigma^o$  model and the actual ocean  $\sigma^o$  and between the antenna pattern model and the actual pattern.
- The clutter contribution to atmospheric targets from just above the surface to a slant altitude of about 15 km is dominated by same-pulse clutter (i.e.,  $n = 0$ ).
- At nadir (not shown) the  $n = 0$  pulse does not contribute to range bins above the surface; we find that  $Z_m$  due to  $n \geq 1$  is nearly constant with altitude, having a value near -3 dBZ.
- This value is well below the TRMM PR sensitivity due to thermal noise and cannot be observed.

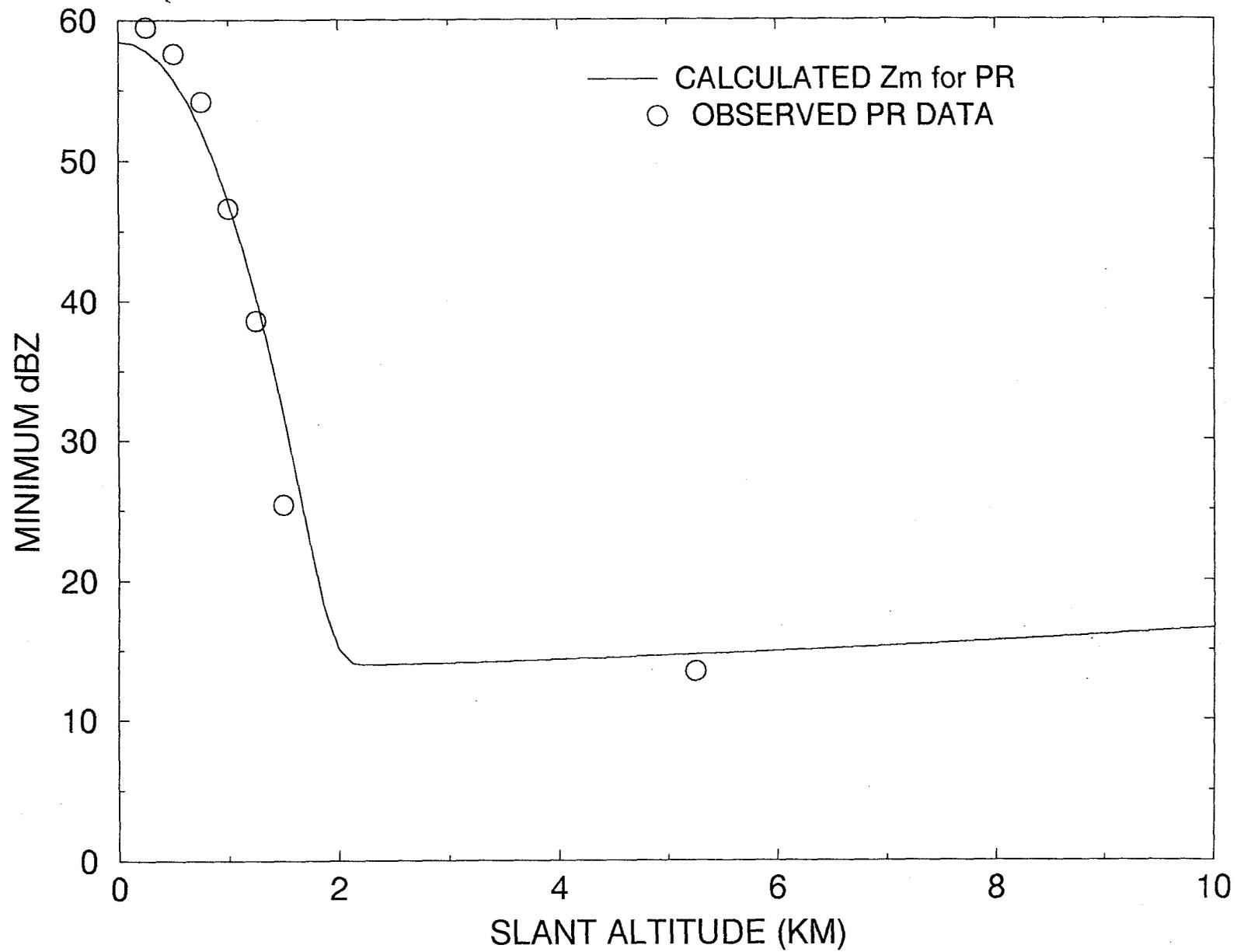
## 7. Application to Cloud Radar

- Cloud radars must measure targets substantially weaker than precipitation (e.g., -25 dBZ versus +25 dBZ).
- The figure shows a calculation for a 94 GHz cloud radar with antenna sidelobes of -38 dB; the resulting  $Z_m$  is near -20 dBZ.
- Improvement can be found by using frequency diversity; a sequence of transmit frequencies is used, varying pulse-to-pulse.
- The receiver tracks the transmit frequency with a delay corresponding to the pulse roundtrip time.
- The figure shows results with the same antenna but using 2 MHz spacing between frequencies and 16 frequencies;  $Z_m$  is lowered to -34 dBZ.
- The next figure shows the contribution of each annulus to the received clutter at 25 km altitude, both without and with frequency diversity.
- For the case without frequency diversity, the Doppler spectra of all annuli are centered on the receiver passband.
- When frequency diversity is used, the annuli have center frequencies shifted by 2 to 30 MHz, reducing the power in the receiver passband.

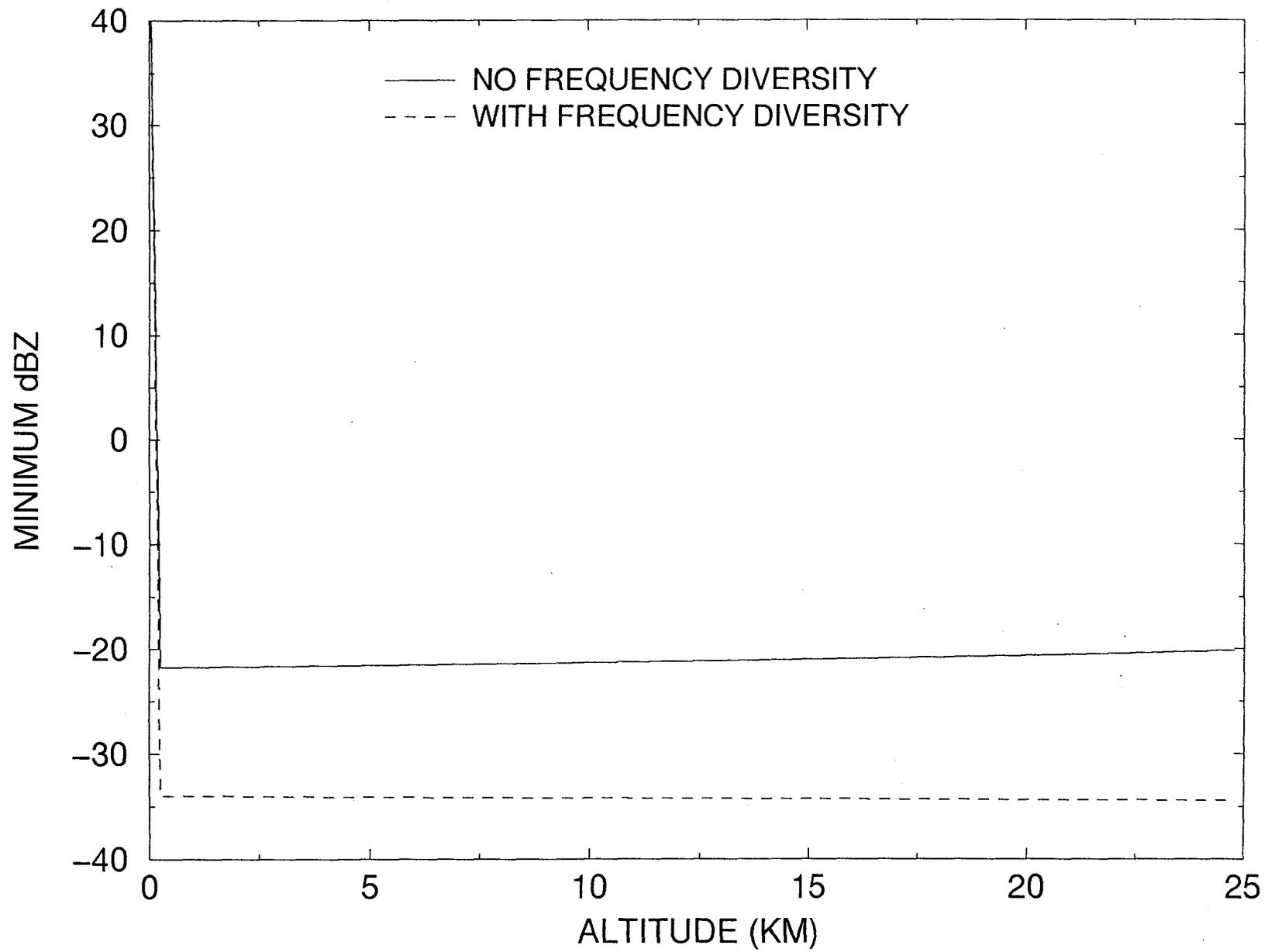
# Geometry for Clutter Calculations



# OBSERVED AND CALCULATED $Z_m$ for TRMM PR



# Calculated Zm for 94 GHz Cloud Radar



# Contributions from individual annuli

94 GHz spaceborne cloud radar

