

***Simulations of  
Relativistic Jet Formation  
In Microquasars***

David L. Meier

Jet Propulsion Laboratory

California Institute of Technology

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## *Talk Outline*

- Introduction: observed Lorentz factors
- Review of steady state simulations
- Pseudo-relativistic simulations and the “magnetic switch”
- General relativistic jet production and rotating black holes
- Possible scenarios for Microquasars

# *Acknowledgements*

- Collaborators
  - General Relativistic simulations: S. Koide (Toyama University), K. Shibata, T. Kudoh (National Astron. Obs, Japan)
  - Pseudo-relativistic simulations: D. Payne (Intel), K. Lind (Silicon Graphics), S. Edgington (Caltech), P. Godon (Space Telescope)

# *Observed Lorentz Factors*

- Component proper motions:  $\Gamma \equiv (1-v^2/c^2)^{-1/2} = 5-10$   
(NOTE: this may measure a pattern speed only)

- Brightness temperature measurements of Doppler boosting:

$$\Gamma \geq 0.5 T_{B,\text{measured}} / T_{B,\text{rest frame}}$$

–  $T_{B,\text{rest frame}} \approx 10^{11}$  K for an equipartition synchrotron plasma

– Some measured brightness temperatures and inferred Lorentz factors:

- Ground Radio VLBI:  $T_{B,\text{measured}} \geq 10^{12}$  K  $\Rightarrow$
- Space VLBI (VSOP):  $T_{B,\text{measured}} \geq 7 \times 10^{12}$  K  $\Rightarrow$
- Intra-day variable sources:  $T_{B,\text{estimated}} \sim 5 \times 10^{14}$  K (?)  $\Rightarrow$  (?)

# Conclusions

- The magnetically-driven outflow has two main components:
  - A slowly-collimating wind from the surface of the accretion disk
  - A highly-collimated jet from the inner edge of the disk or torus
- Both types of outflow are subject to “magnetic switching”:
 

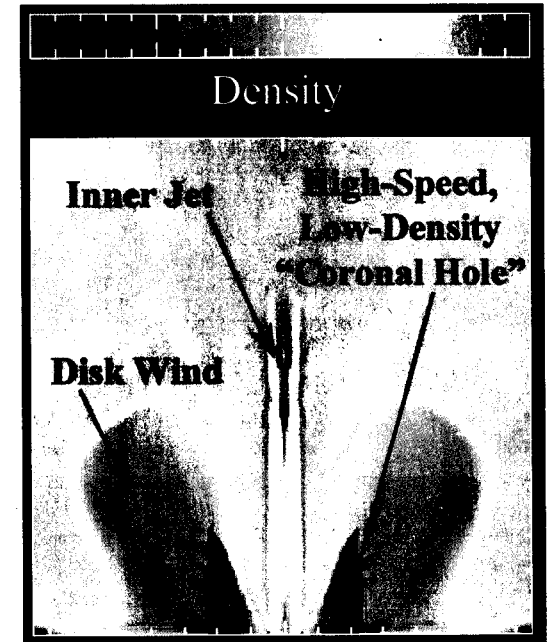
There exists a critical MHD power  $L_{\text{crit}} \equiv E_{\text{escape}}/\tau_{\text{free-fall}}$  (analogous to the Eddington limit) such that

  - When the MHD power in the rotating magnetic field  $L_{\text{MHD}} < L_{\text{crit}}$ , gravity is important, and the jet/wind speed is limited to  $V_{\text{jet}} \sim V_{\text{escape}}$

$$L_{\text{MHD}} > L_{\text{crit}}$$

$$\dot{M} V_{\text{jet}}^2 \sim L_{\text{MHD}}$$

$$\Gamma_{\text{jet}} \dot{M} c^2 \sim L_{\text{MHD}}$$

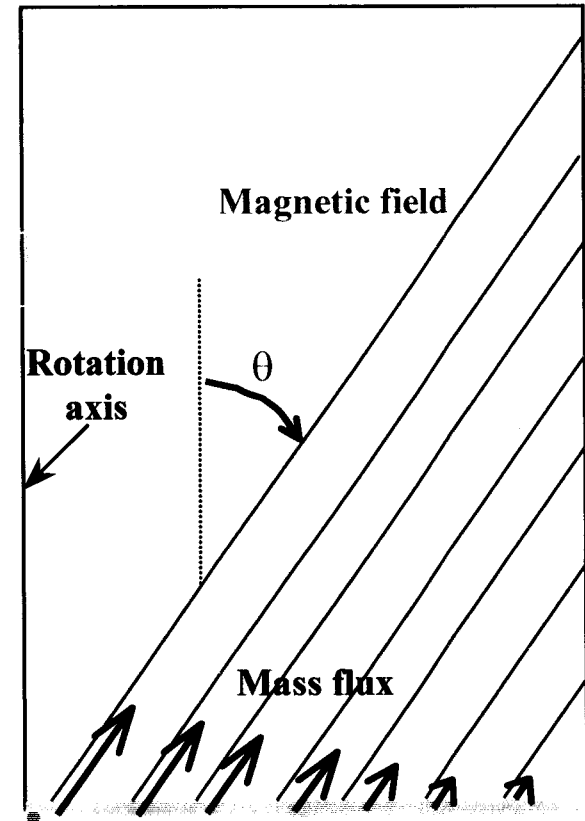


## *Conclusions (continued)*

- When the accreting object is a rotating black hole:
  - The jet is accelerated from the “frame-dragged” accreting matter inside the ergosphere
  - Recall:
    - The horizon is much smaller than one Schwarzschild radius ( $GM/c^2$  for maximal Kerr)
    - All matter in the region  $R < 2 GM/c^2$  (the “ergosphere”) must rotate with the black hole
  - The strongest and fastest jets occur when:
    - The black hole is rotating rapidly
    - The accreting material plunges rapidly into the ergosphere
      - *E.g.*, when the accretion is an **Advection-Dominated Accretion Flow [ADAF]** or
      - *E.g.*, when the accretion disk counter-rotates relative to the black hole

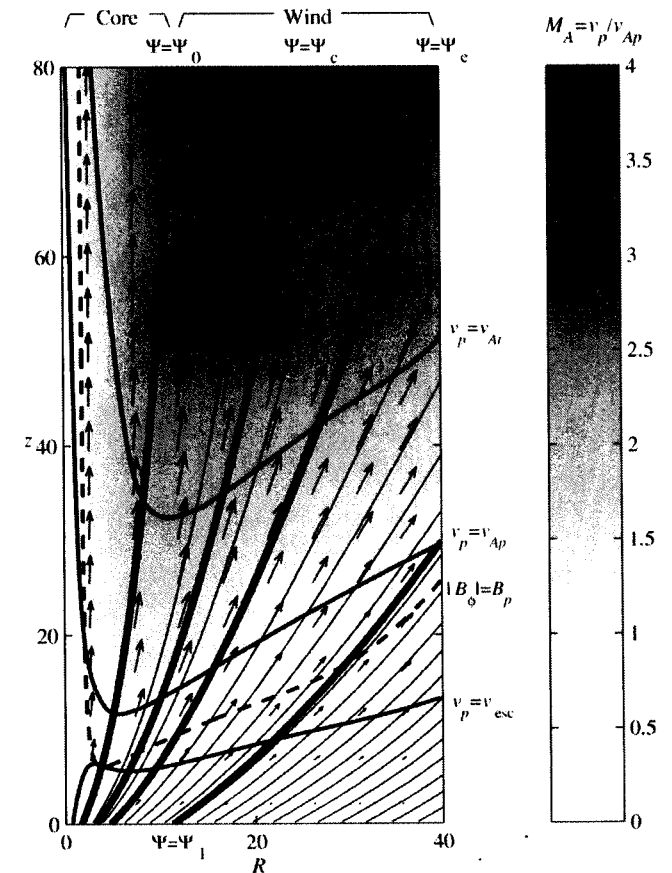
# *Review of Steady State Simulations*

- Some numerical simulations have attempted to reproduce the Blandford & Payne solutions (Ustyugova et al. 1995, 1999; Ouyed et al. 1997; Krasnopolsky et al. 1999)
- - An infinitely-thin accretion disk at  $R=0$
  - A central mass gravitational potential with a small “smoothing radius”
  - Keplerian rotation
  - Fixed vertical magnetic field  $B_z$
  - Fixed mass flux along the field lines
  - : the following quantities on the boundary are allowed to vary: radial  $B_R$  and toroidal  $B_\phi$  magnetic field strength, and radial velocity  $V_R$



# *Review of Steady State Simulations (continued)*

- (e.g., Krasnopolsky, Li, & Blandford 1999):
  - Simulations run out to late times to achieve a steady state
  - Results similar to Blandford & Payne's self-similar solutions are produced
  - For magnetically-driven outflow, the magnetic field polar angle ( $\tan \theta = B_R/B_Z$ ) must be larger than  $\theta > 30^\circ$  at the disk boundary
  - Flow accelerates smoothly, reaching escape velocity and then the local Alfvén speed(s)
  - Collimation is slow but steady, reaching a jet-like state far away from the disk
  - Outflow speed is of order the escape velocity at the base of the flow



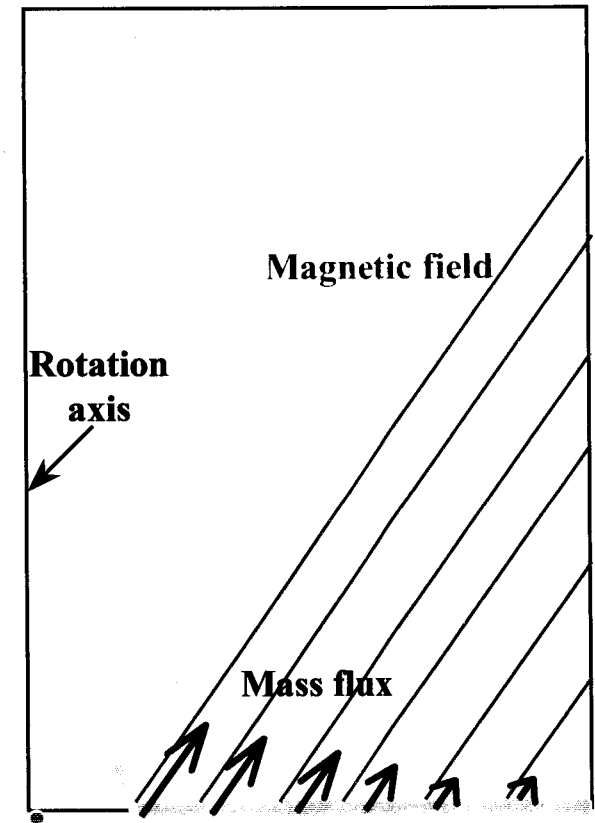


# *Pseudo-Relativistic Simulations of Black Hole Accretion Disks*

- When the disk coronal material is not a relativistic gas ( $c_{\text{sound}} < c$ ;  $V_{\text{Alfvén}} < c$ ), the non-relativistic MHD equations are nearly identical to the relativistic ones, IF we replace the velocity  $V$  with the proper velocity  $U$

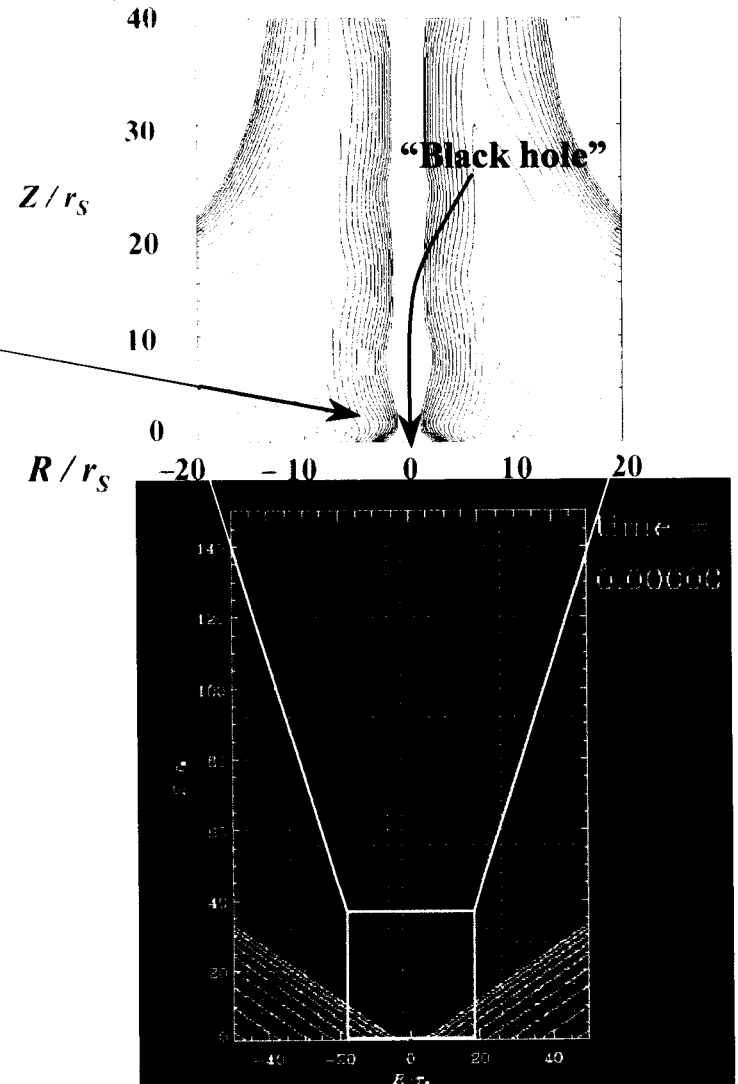
$$V \rightarrow U = \Gamma V$$

- In these simulations,  $\Gamma = 1$
- $\Gamma = 1$  in these pseudo-relativistic simulations (Lind, Meier, & Payne 1994; Meier *et al.* 1997; Meier *et al.* 2000):
  - Similar to previous “disk as boundary” simulations, but
  - Infinitely-thin  $\Gamma = 1$  at  $R = 6GM/c^2$
  - $B_R$ ,  $B_\phi$ , and  $V_R$  are all zero on the boundary (as would be the case in an actual accretion disk)



# *Pseudo-Relativistic Simulations of Black Hole Accretion Disks (continued)*

- (Meier et al. 1997; 2000):
  - This and create a new magnetic field structure:
    - Gravitational and magnetic forces cause injected , above the disk
    - This , creating a substantial  $B_R$
    - Differential rotation winds  $B_R$  up into  $B_\phi$ , which expels and collimates a narrow jet
  - This inner jet in the accreting corona case is similar to that in the accreting torus case shown by Shibata-san
  - A slowly-collimated disk wind (like the Blandford-Payne solutions) also occurs occasionally, but usually only when the inner jet is weak

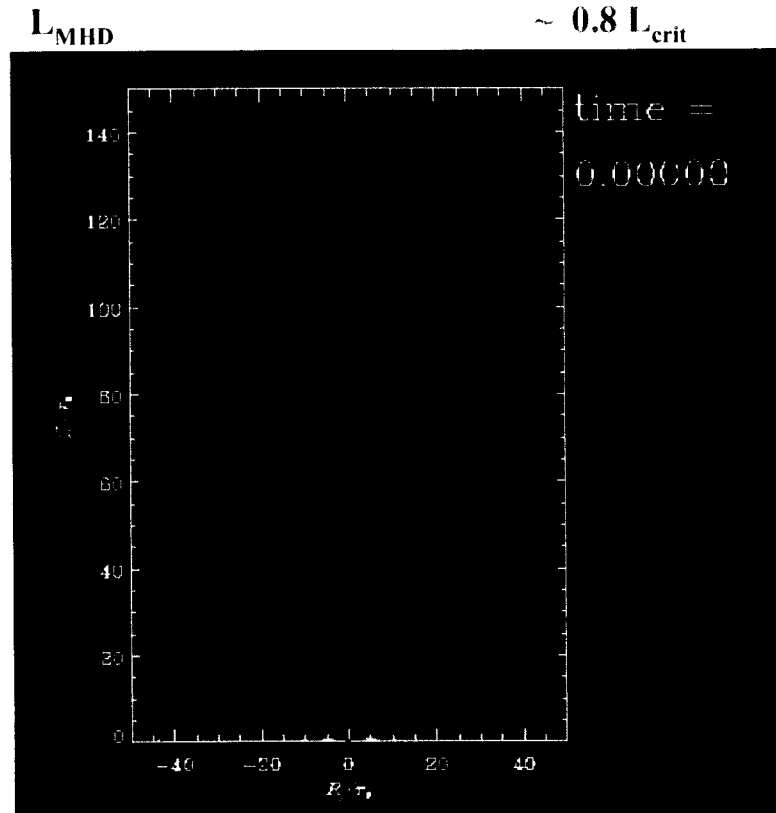


# *Pseudo-Relativistic Simulations of Black Hole Accretion Disks (continued)*

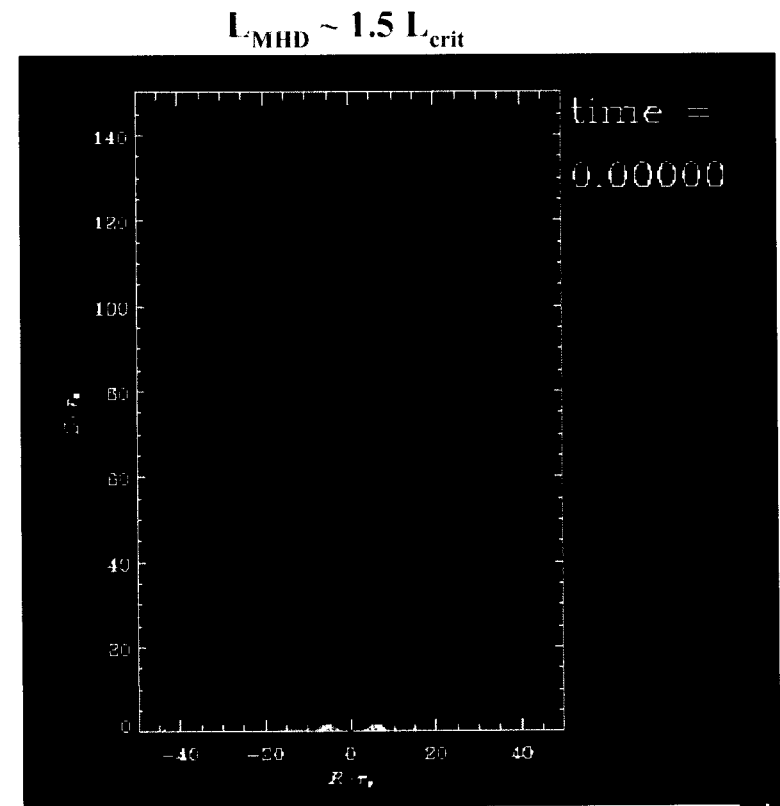
(Meier *et al.* 1997; Meier 1999):

- There appears to be a critical MHD luminosity (analogous to the Eddington limit)

$$L_{\text{crit}} \equiv E_{\text{escape}} / \tau_{\text{free-fall}} =$$

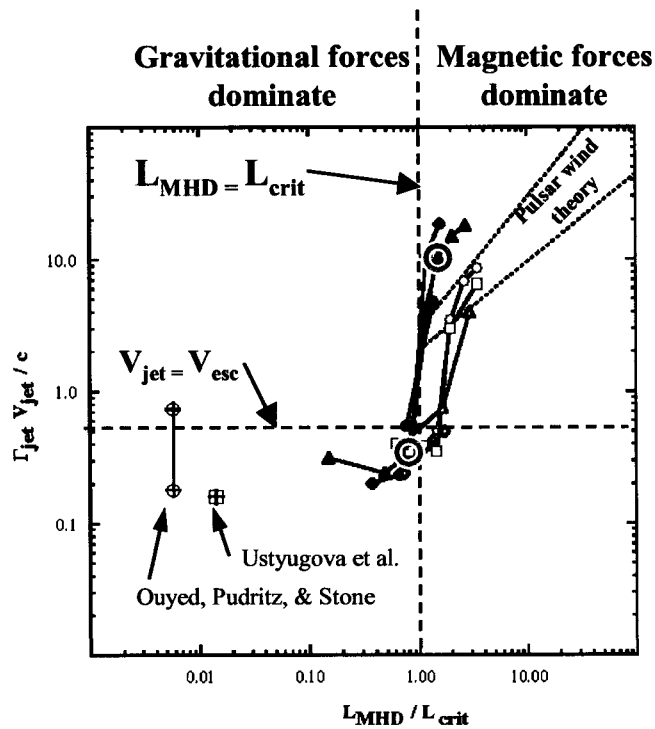


When  $L_{\text{MHD}} < L_{\text{crit}}$ ,  $V_{\text{jet}} \sim V_{\text{esc}}$   
resulting in a relatively



When  $L_{\text{MHD}} > L_{\text{crit}}$ ,  $V_{\text{jet}}$  is determined by  $L_{\text{MHD}} \sim \Gamma_{\text{jet}} M c^2$ ,  
resulting in a relatively

# *Pseudo-Relativistic Simulations of Black Hole Accretion Disks (continued)*



Jets with high MHD power and low mass flux (“Poynting flux dominated”) have the potential for reaching high Lorentz factors ( $\Gamma \gg 10$ )

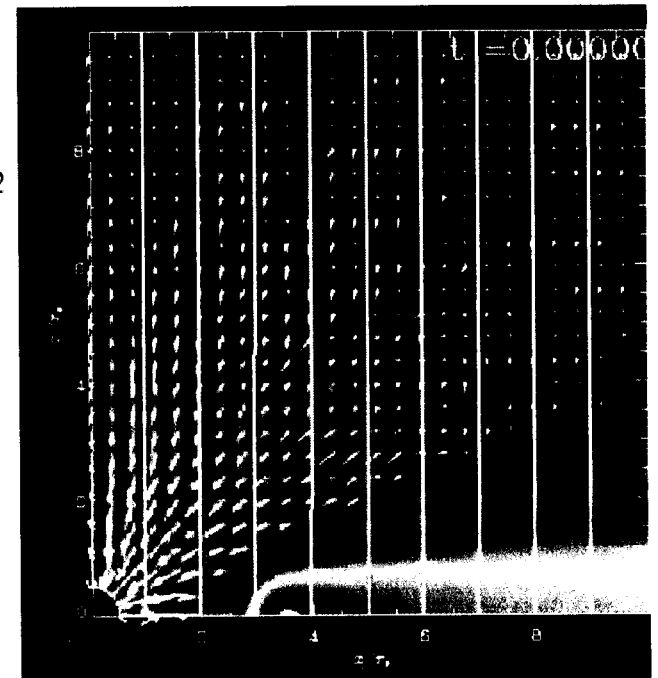
However  $L_{\text{MHD}} > L_{\text{crit}}$  can happen where the magnetic field can be strong and the density low

In the accretion disk itself  $L_{\text{MHD}} < L_{\text{crit}}$ , or the magnetic forces will dynamically destroy the disk

Jets with low MHD power or high mass flux are initially bound and can only reach the disk escape velocity

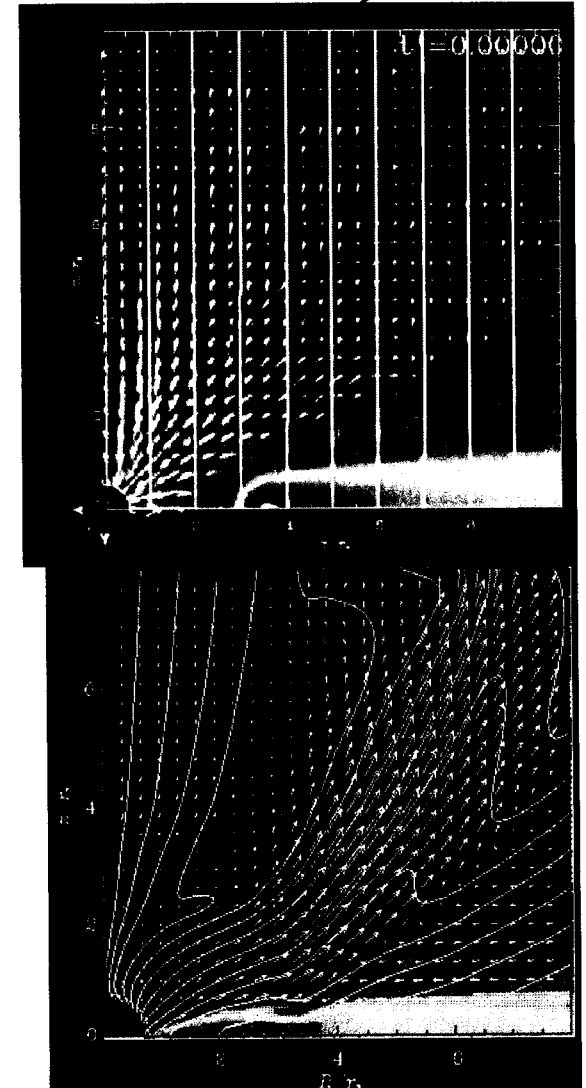
# General Relativistic Simulations of Black Hole Accretion Disks

- **Thick accretion disk** : Koide, Shibata, & Kudoh (1998); Koide, Meier, Shibata, & Kudoh (1999a,b)
  - Thick accretion disk with inner edge at  $R = 4.5 GM/c^2$
  - Initial vertical magnetic field ( $V_{\text{Alfvén}} = 0.01c$ )
  - Fixed inflow velocity and inflow flow
- **Thin accretion disk**
  - Schwarzschild (Schwarzschild), (ADAF-like)
  - Kerr (Kerr) ( $a/M=0.95$ ), (ADAF-like)
  - Co-rotating with the black hole rotation
  - Counter-rotating against the black hole rotation



# *General Relativistic Simulations of Black Hole Accretion Disks (continued)*

- *General Relativistic Simulation of a Disk Plunging into a Black Hole*
  - Disk plunges rapidly toward black hole (counter-rotating orbits are unstable!)
  - Dragging of inertial frames by rotating black hole reverses spin of disk
  - A jet is generated from the inner disk edge in a manner similar to non-relativistic simulations
  - A very low density region forms inside the jet --- potentially the beginning of a magnetically-switched, high Lorentz factor flow
- *General Relativistic Simulation of a Disk Falling into a Rotating Black Hole*
  - Disk free-falls rapidly into ergosphere
  - Rotation of black hole contributes significantly to acceleration of jet
  - Highest jet velocities achieved so far are of order the ergospheric escape velocity:





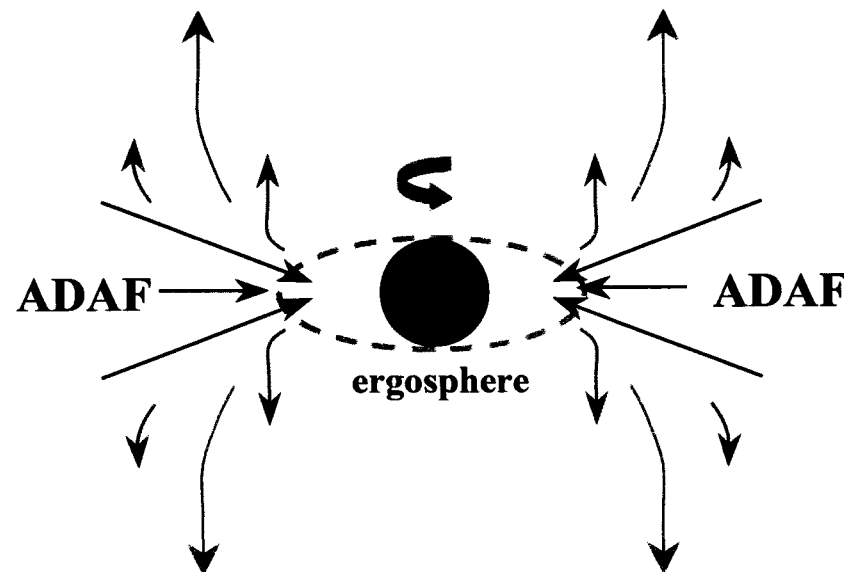
# *Summary of All Simulations Performed*

- - The central black hole rotates rapidly
  - The accreting material falls rapidly into the ergosphere
  - The material accelerated in the jet is of very low density  
(*i.e.*,  $L_{\text{MHD}} > L_{\text{crit}}$  or, for Keplerian rotation,  $V_{\text{Alfvén}} > V_{\text{esc}}$ )



# *The Association of Advection-Dominated Accretion Flow (ADAFs) with Jet Production in Microquasars*

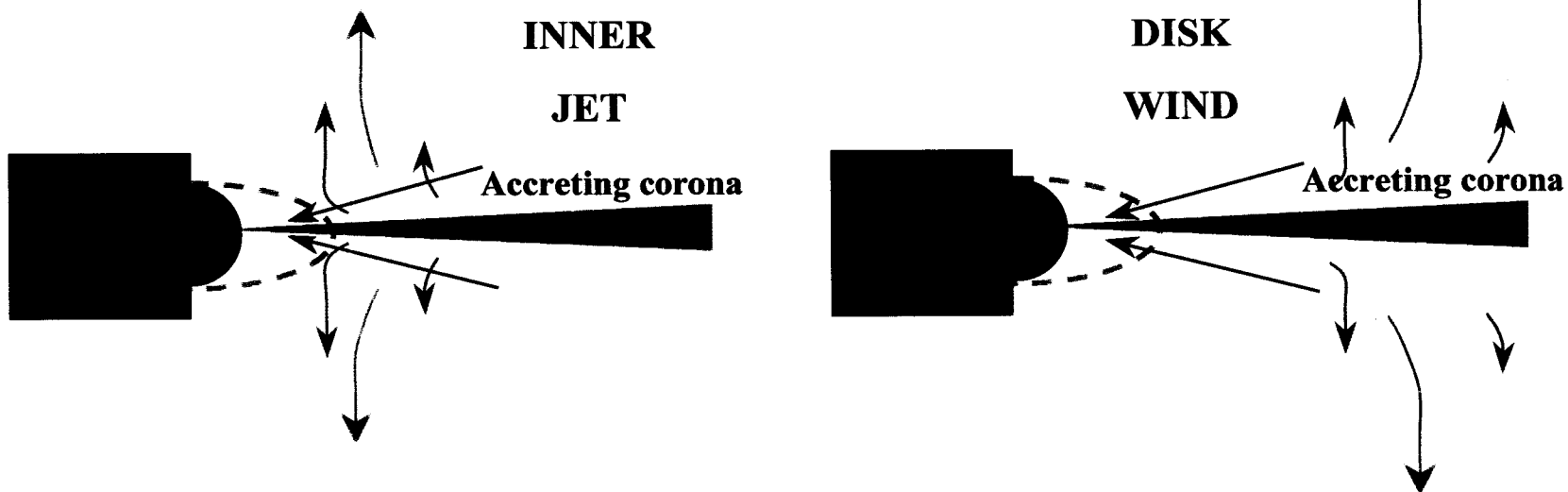
- Rapid infall toward black hole
- Little rotation in the accretion flow until it plunges into the ergosphere
- Jet is produced and collimated very near the black hole
- Much of the outflow is at the escape velocity ( $\Gamma < 3$ )
- Highest Lorentz-factor flow ( $\Gamma \gg 10$ ) can occur in low-density, Poynting-flux-dominated, “coronal holes”



# *The Association of Advection-Dominated Accretion Flow (ADAFs) with Jet Production in Microquasars*

## *(continued)*

- Magnetic field is anchored in thin Keplerian-rotating accretion disk
- Rotating disk can accelerate or
- Again, much of the outflow is at the escape velocity ( $\Gamma < 3$ )
- But, high Lorentz-factor flow ( $\Gamma \gg 10$ ) can occur in low-density, Poynting-flux-dominated, “coronal holes”
- Jet can be collimated far from the black hole and still have a high Lorentz factor (cf. )



## *The Future*

- General relativistic MHD simulations
  - Improve GRMHD code to handle very low-density flows
  - Investigate magnetic switching in fully-relativistic, finite-thickness accretion disk situations
- Accretion disk structure calculations
  - Investigate the structure of a rotating black hole magnetosphere and its implications for MHD-driven outflow